

# Experimental bit commitment based on quantum communication and special relativity

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[[arXiv:1306.4801](https://arxiv.org/abs/1306.4801)]

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- **binding:** If Alice is honest then there is at most one bit that Bob can successfully open.
- **hiding:** If Bob is honest then Alice learns nothing about his commitment until the open phase.

## Bit commitment – the no-go

- Quantum mechanics does not allow for a bit commitment that gives perfect (or close to perfect) security to both parties [Lo,Chau'96; Mayers'96].
- There exist protocols that give partial security to both parties, the trade-offs are known [Spekkens,Rudolph'01; Chailloux,Kerenidis'11].

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**RELATIVISTIC BIT COMMITMENT**

# Relativistic bit commitment protocols

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# Security

Proven **secure** in

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Secure you say, **mhhmmmm**, but what's the security model?



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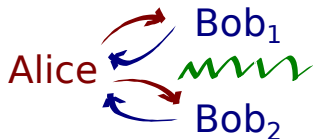
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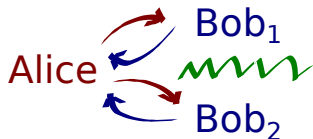
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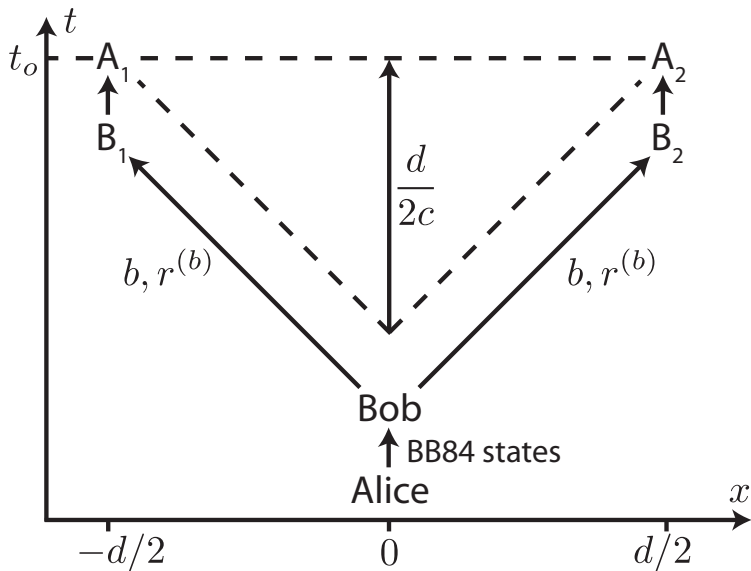


Open phase



*not possible classically*  
*[quantum advantage]*

# Relativistic realisation



# Implementation issues

**Source:** We **do not** use a single photon source. We use a **weak coherent source** with **phase randomisation**:

$$\rho = \sum_{r=0}^{\infty} p_r |r\rangle\langle r|,$$

$$\text{where } p_r = e^{-\mu} \cdot \frac{\mu^r}{r!},$$

$\mu$  is the average number of photons per pulse and  $|r\rangle$  is the Fock state of  $r$  photons.

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**Channel and Bob's detectors:** They are **not perfect**. They introduce **bit-flip errors** and **losses**.

# Implementation issues and fixes...



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*need to try a bit harder...*

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# A fault-tolerant protocol - Security

One-commitment steps (honest execution):

- Alice sends  $N$  pulses, Bob reports detecting  $n$  of them
- Let

$$p_{\text{det}} = n/N$$

- After Bob revealed the commitment, Alice calculates the **QBER**:

$$\text{QBER} = n_{\text{err}}/n'$$

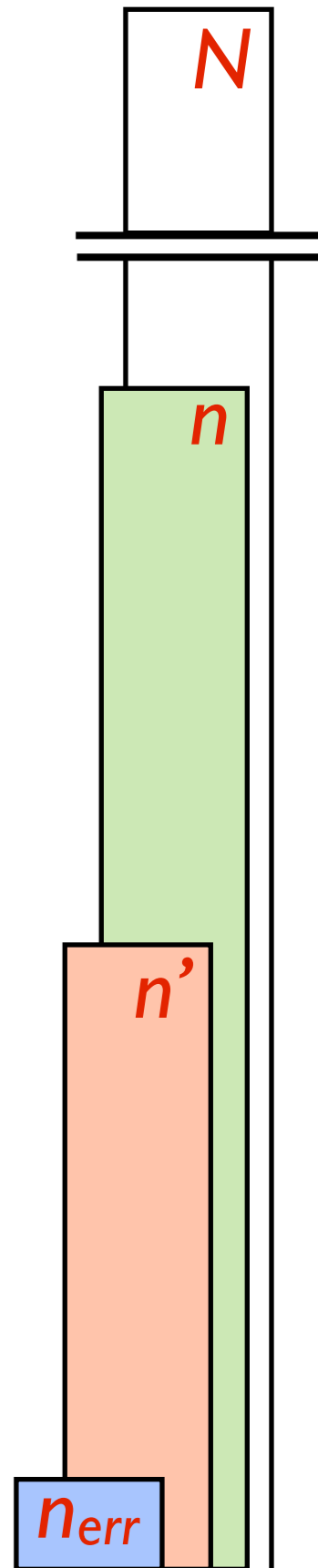
Number of errors within  $n'$

Number of detections with same basis for preparation and measurement

- Security is possible only if

$$p_{\text{det}} > \frac{1 - e^{-\mu}(1 + \mu)}{1 - \frac{\text{QBER}}{\lambda}} \quad \lambda \approx 14.6\%$$

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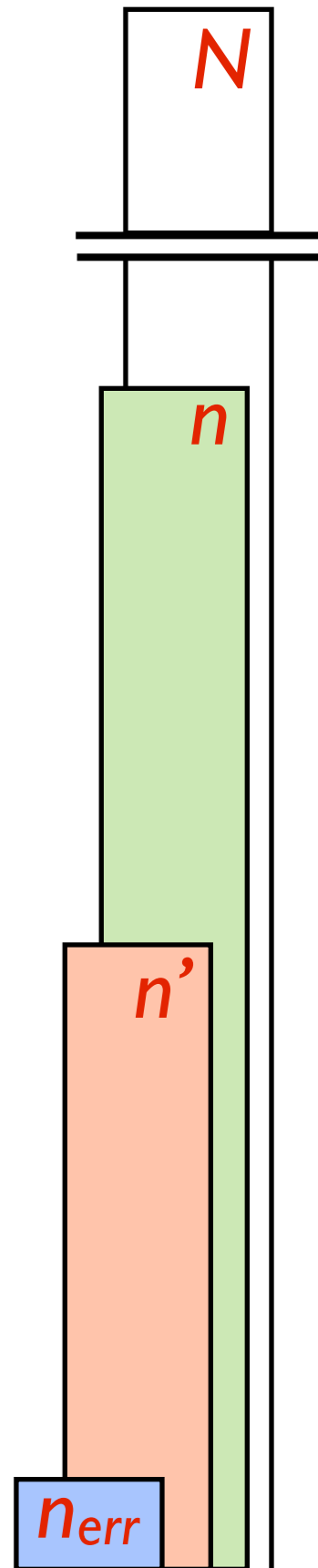
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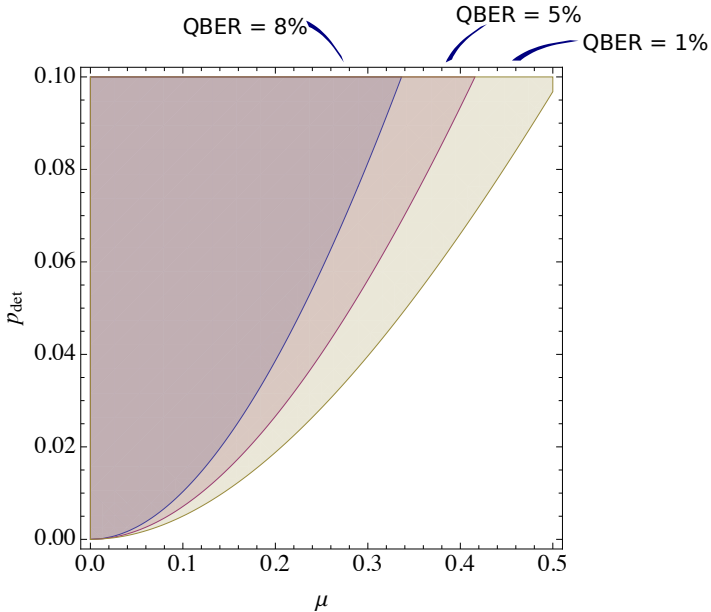
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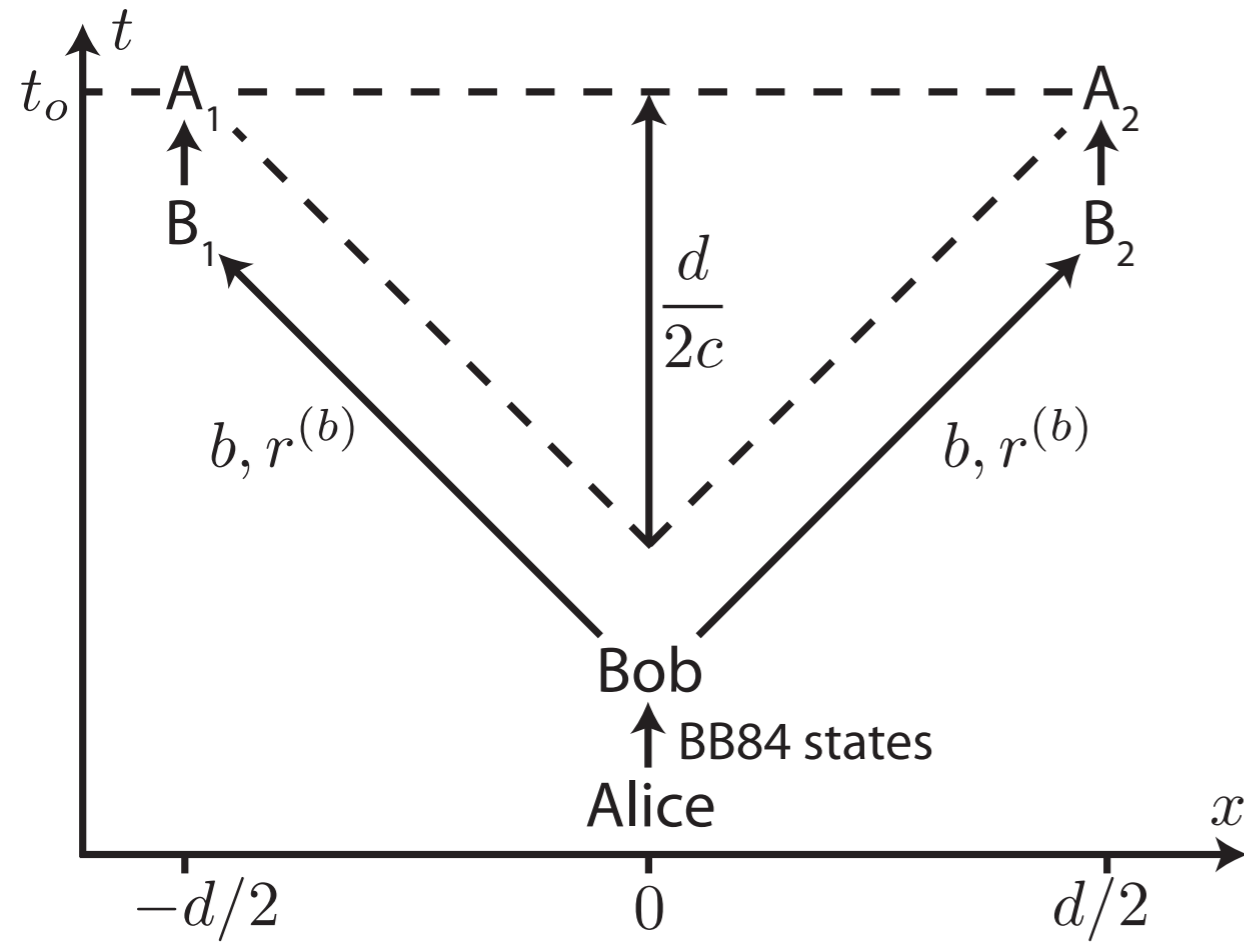
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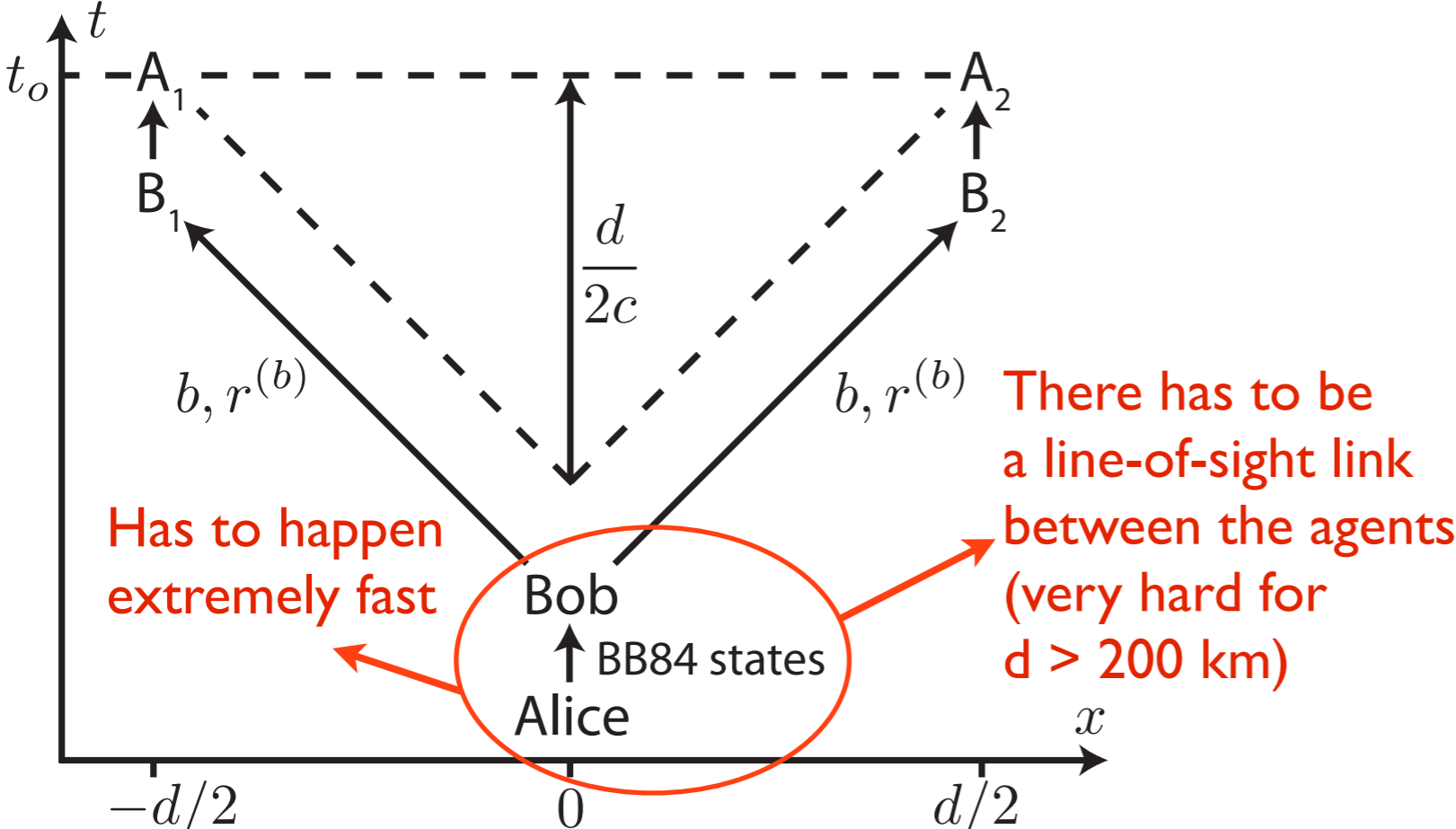
# Feasibility plot



# A more practical version of Kent's 12 protocol



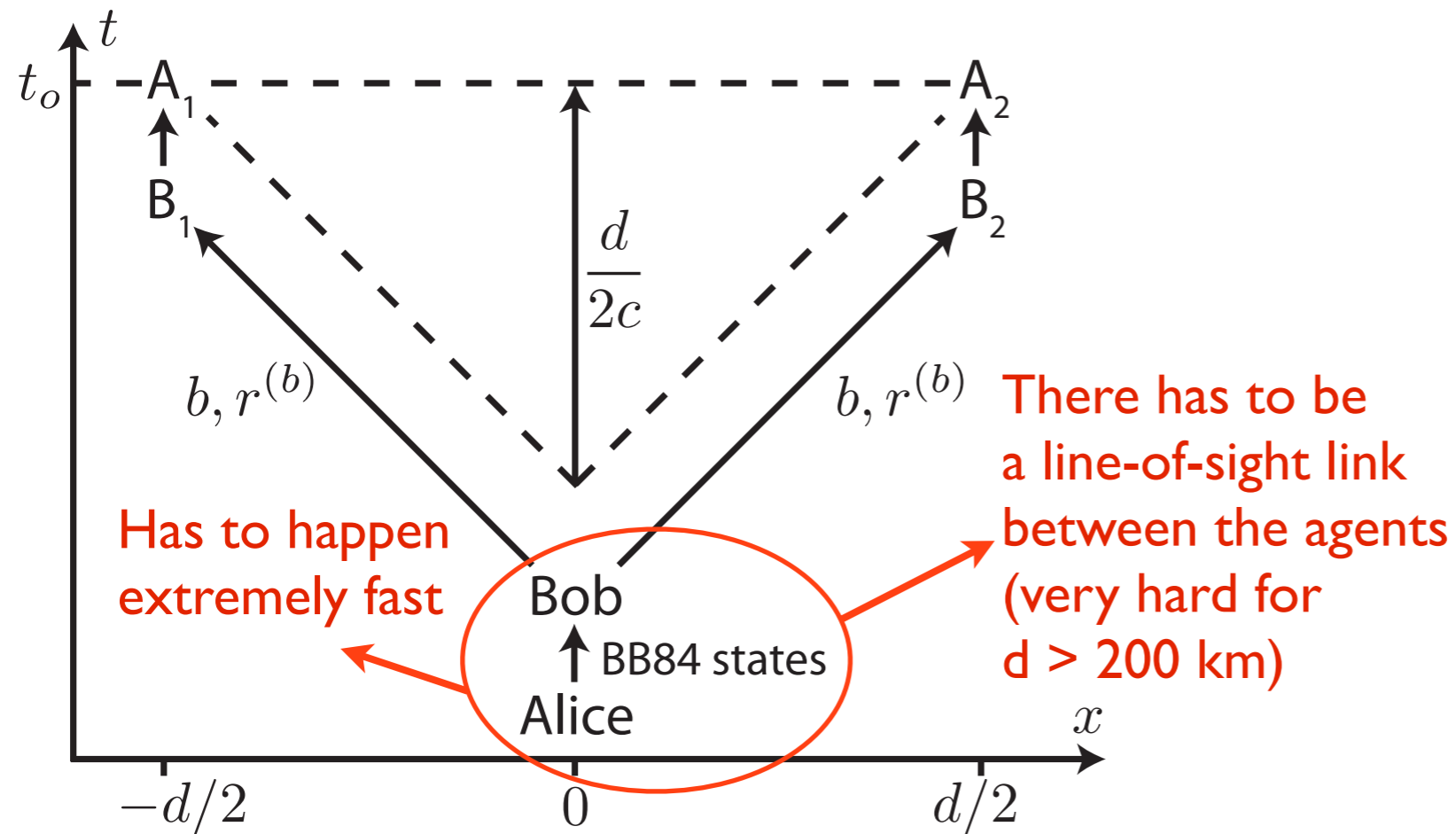
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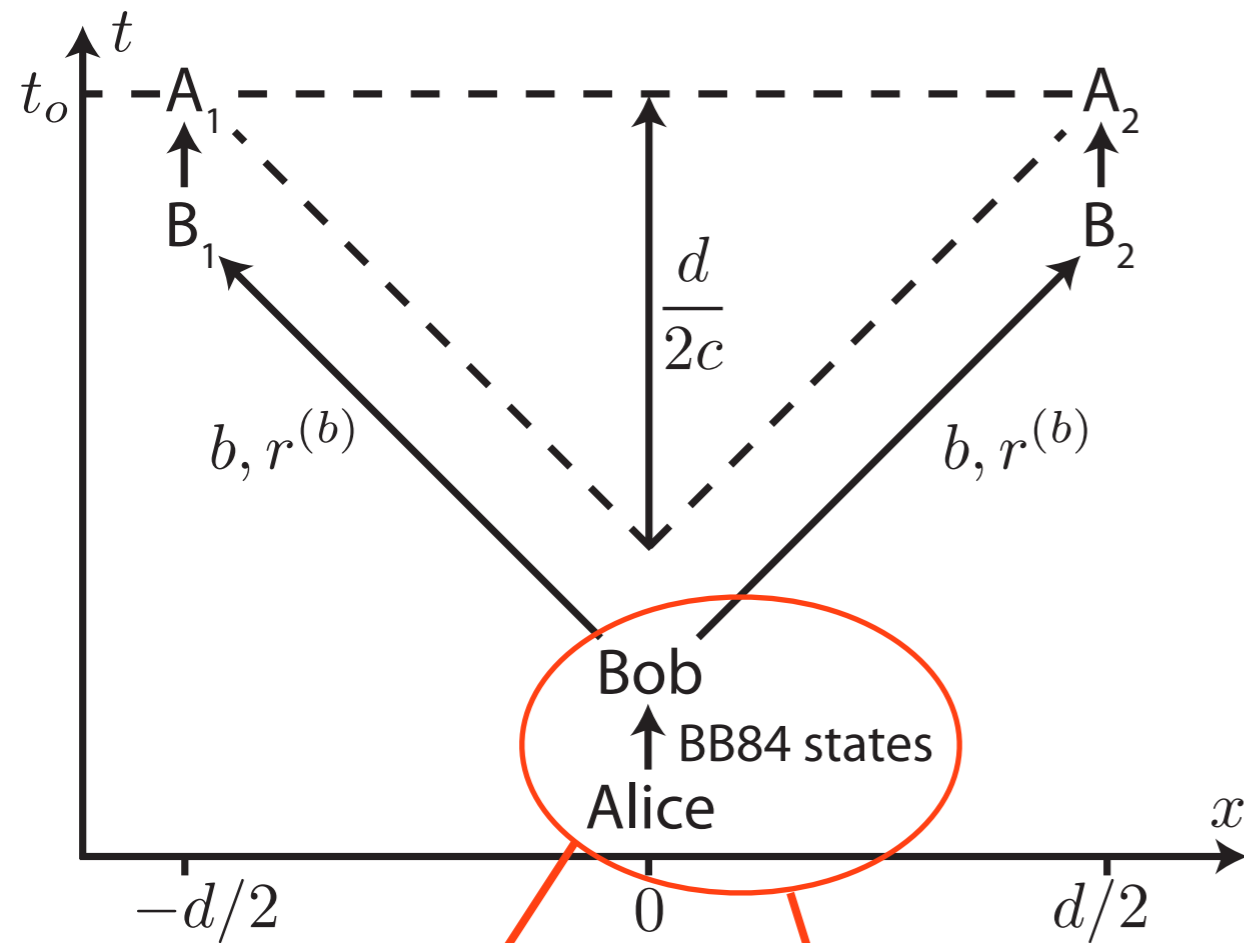
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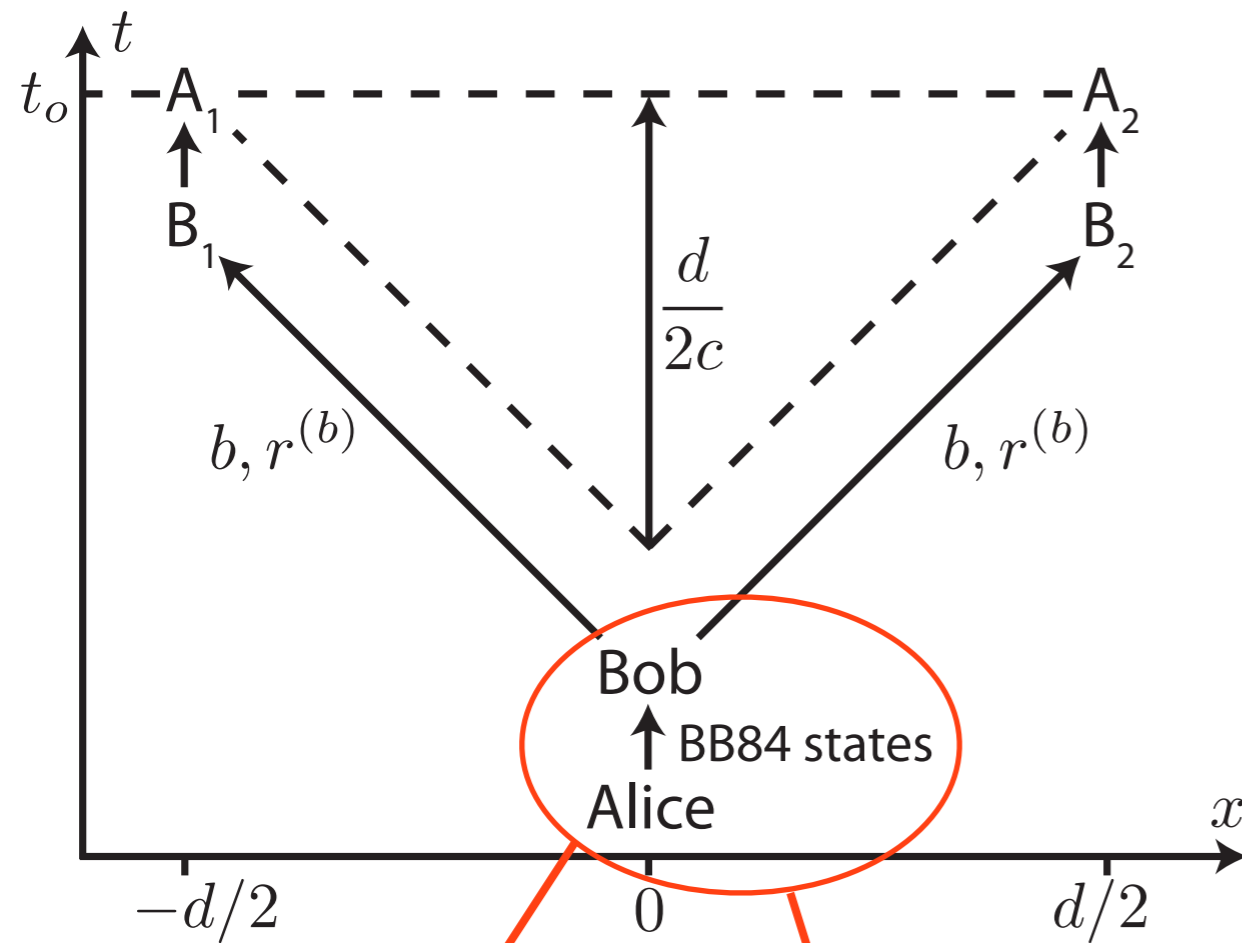
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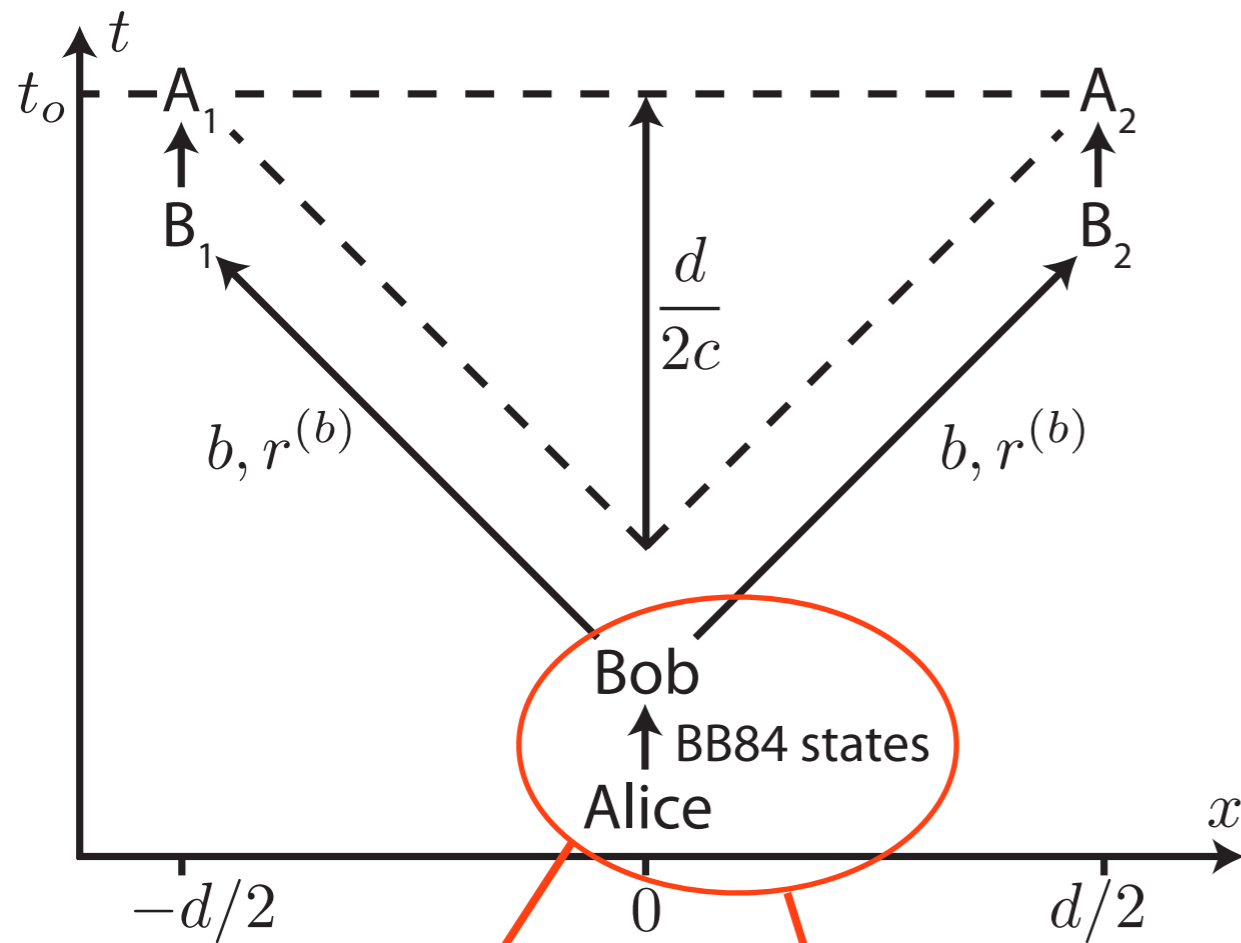


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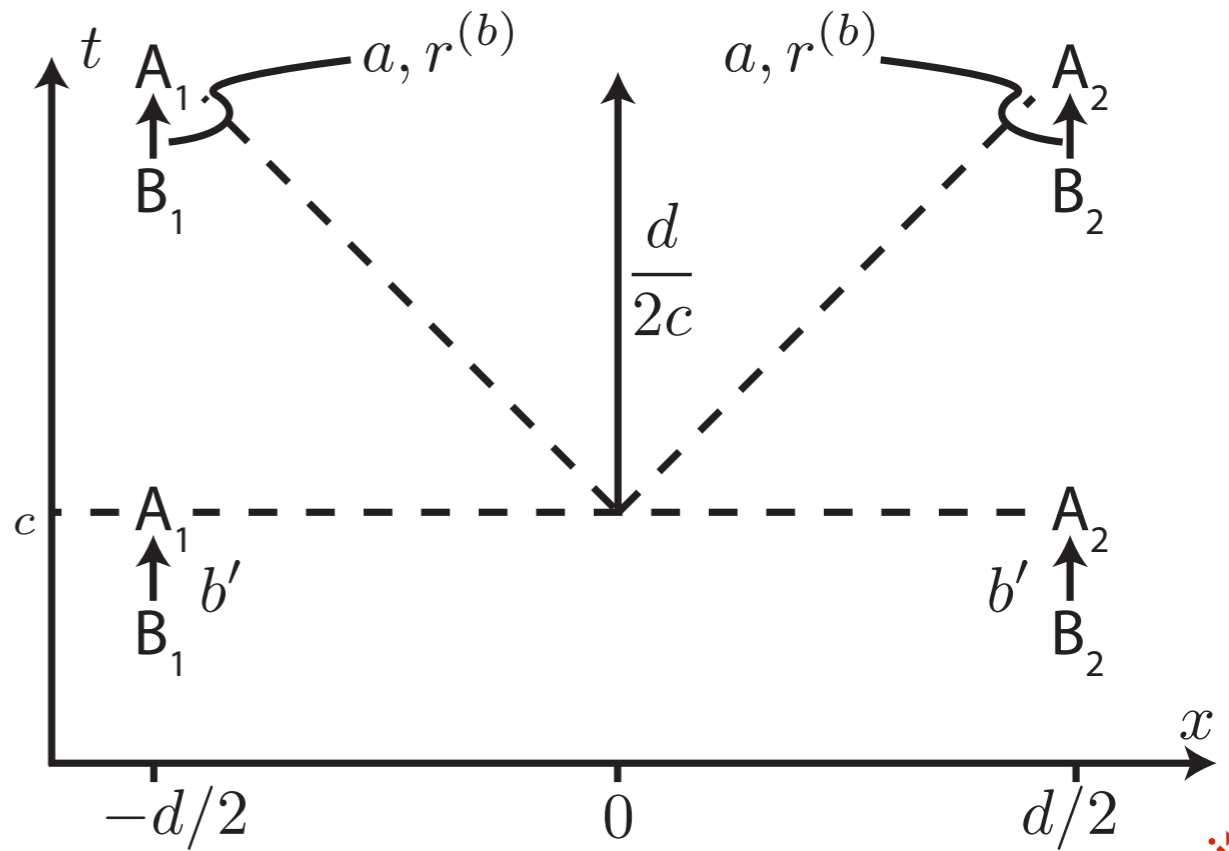
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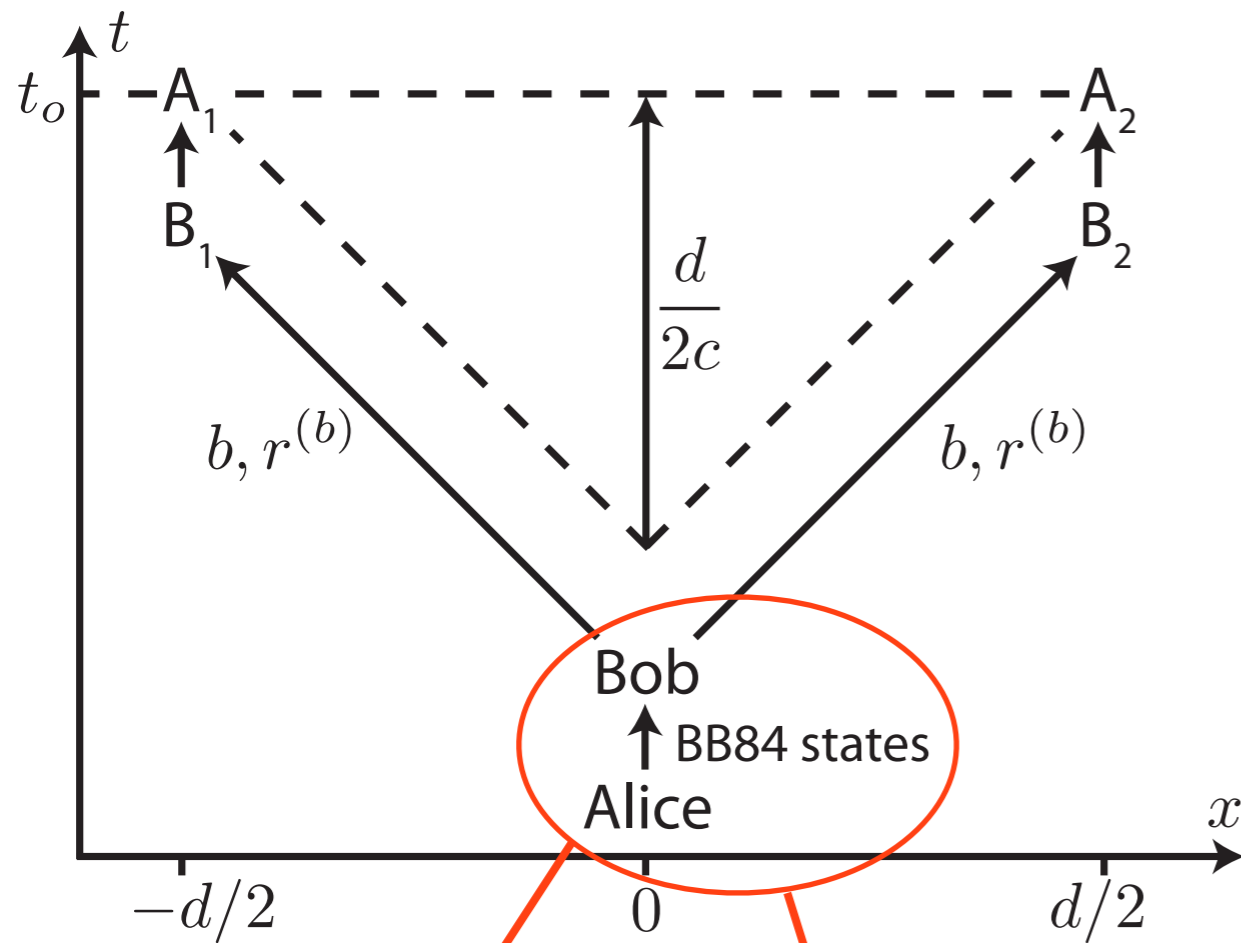
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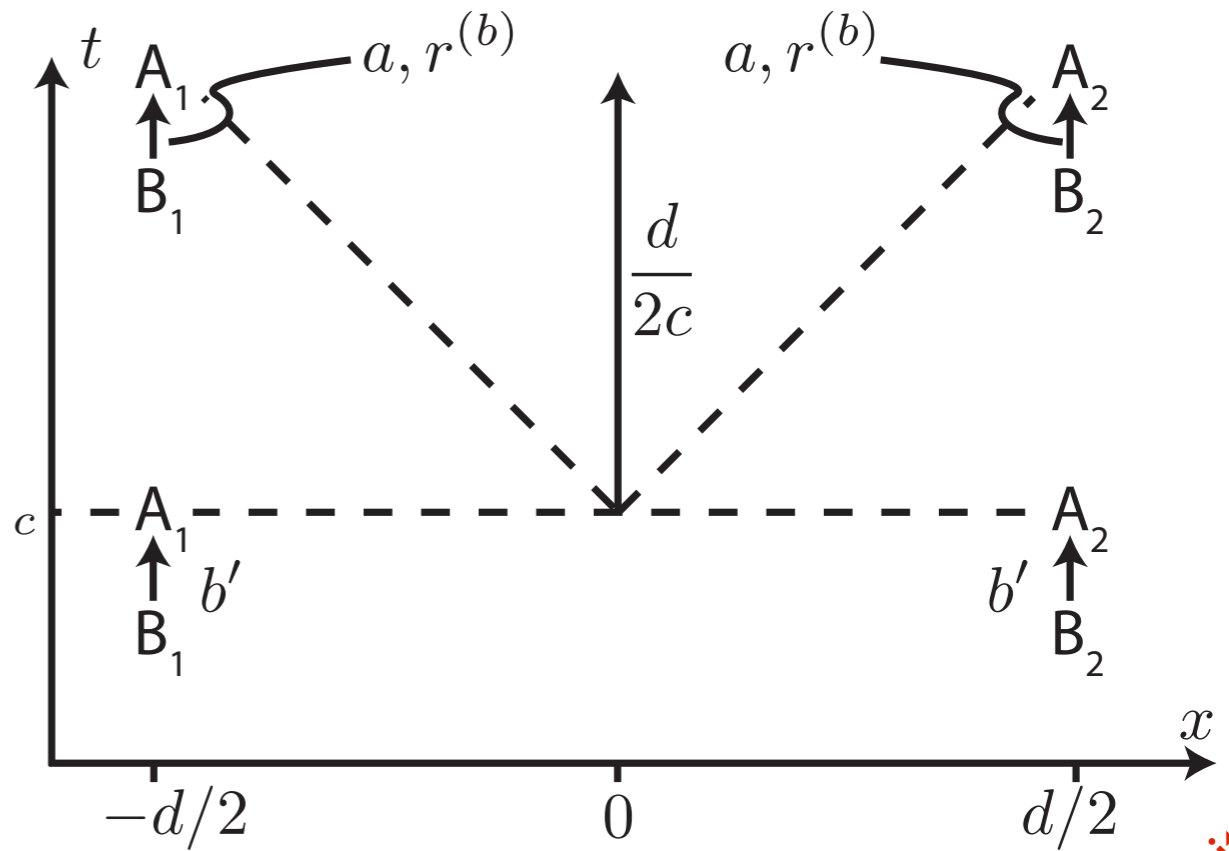


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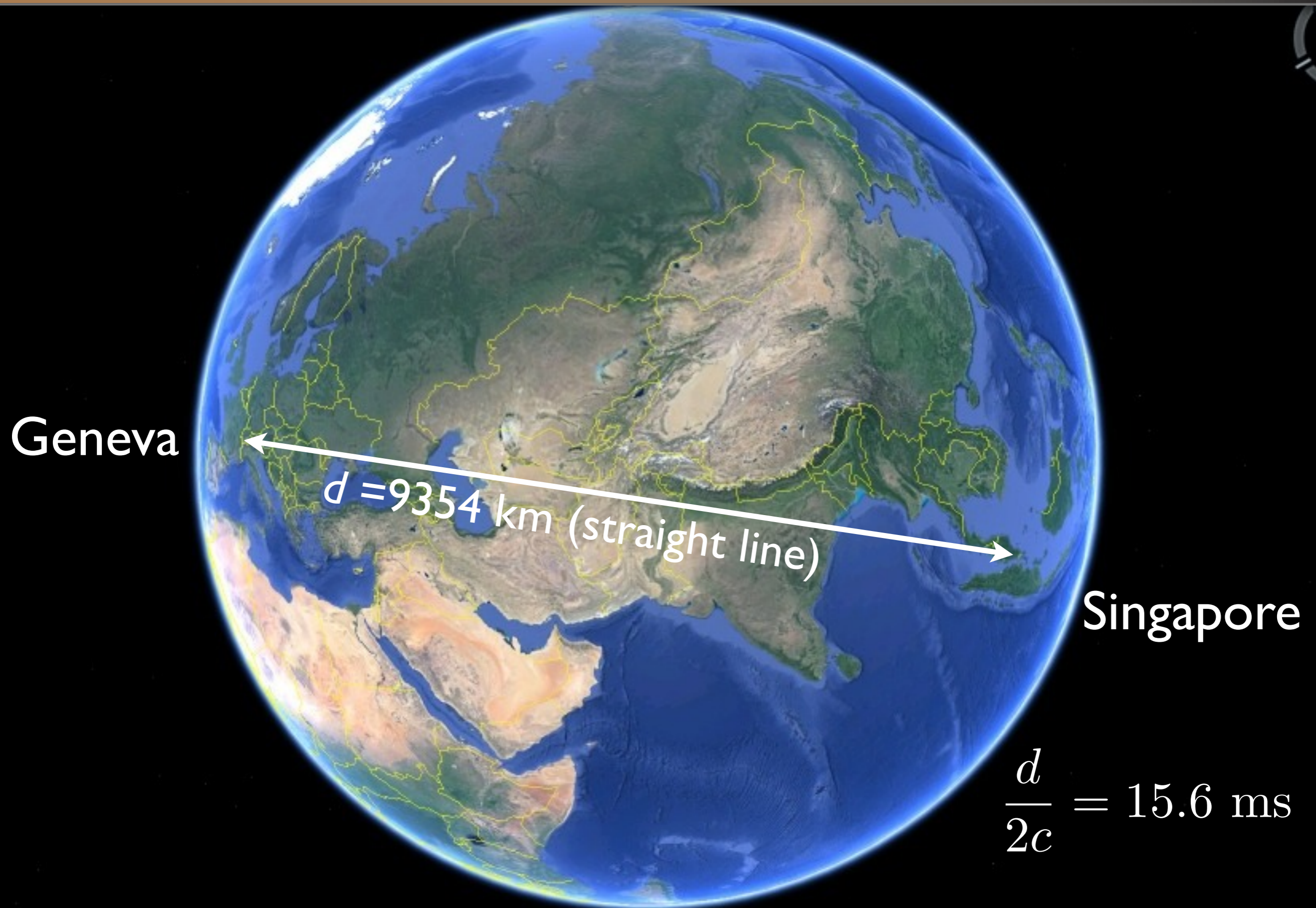
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$B_1$  and  $B_2$  simultaneously reveal  $a$  and  $r^{(b)}$

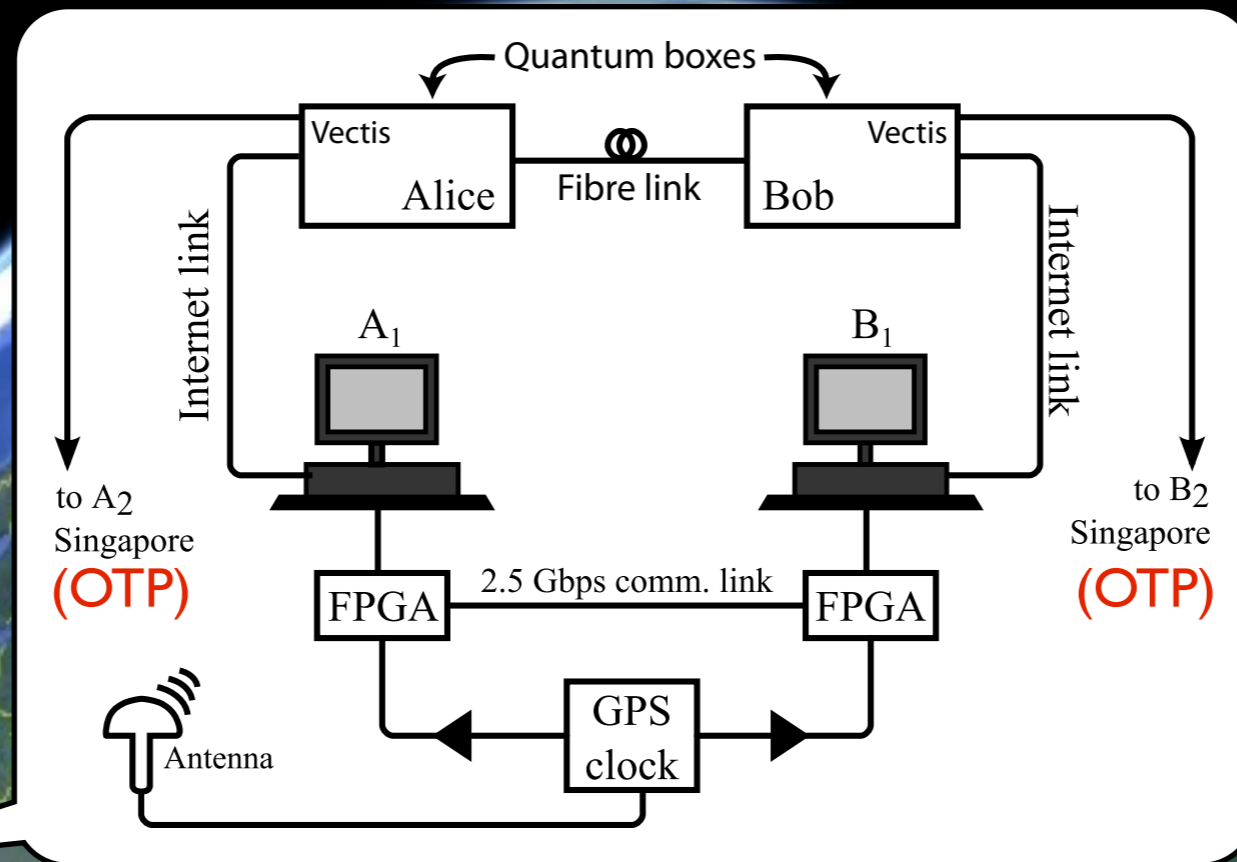
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# Experimental setup - The global picture





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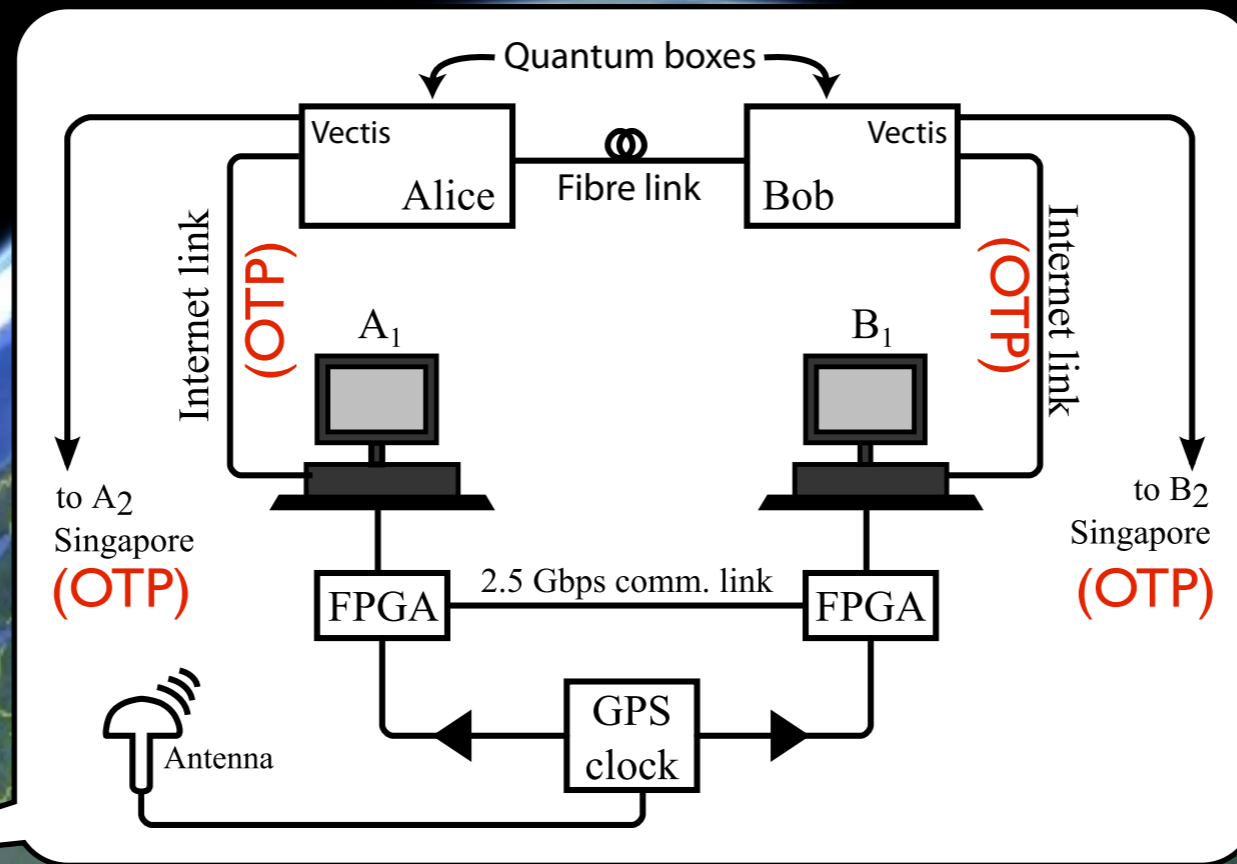
Geneva

$d = 9354$  km (straight line)

Singapore

$$\frac{d}{2c} = 15.6 \text{ ms}$$

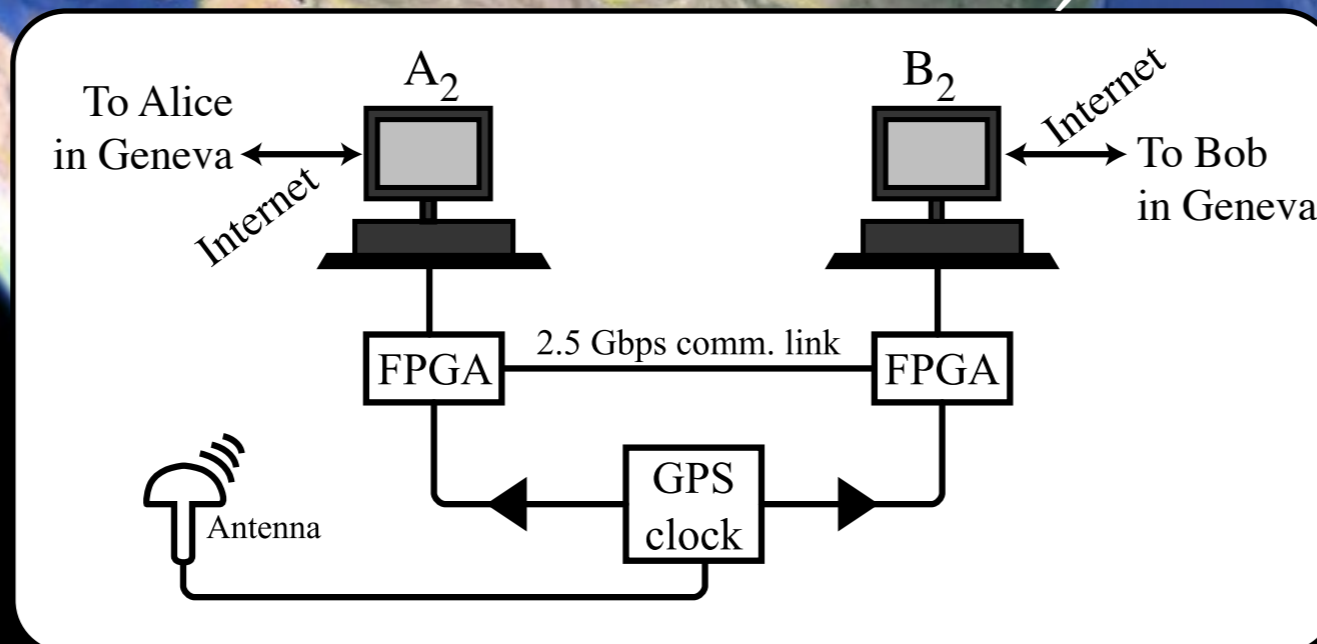
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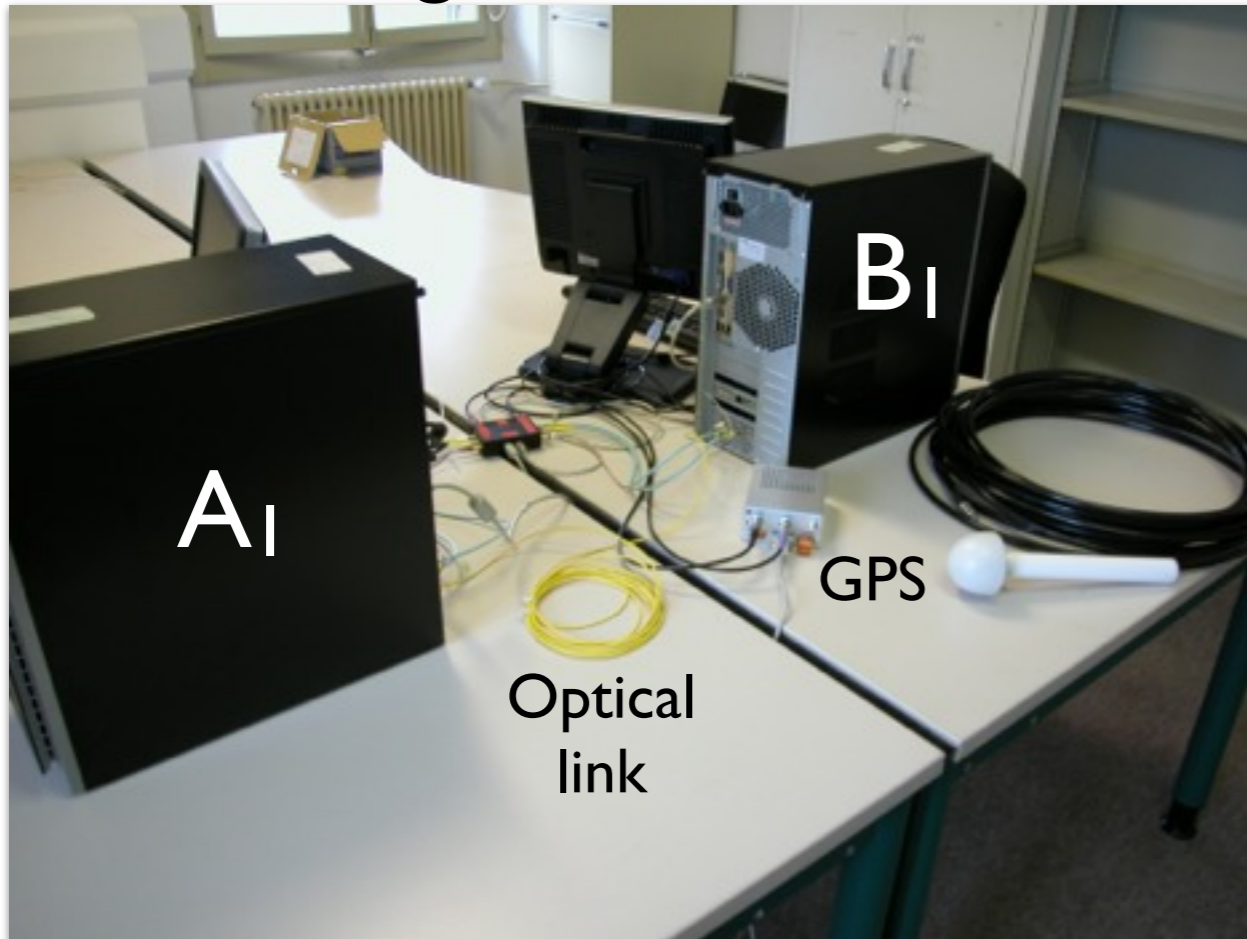


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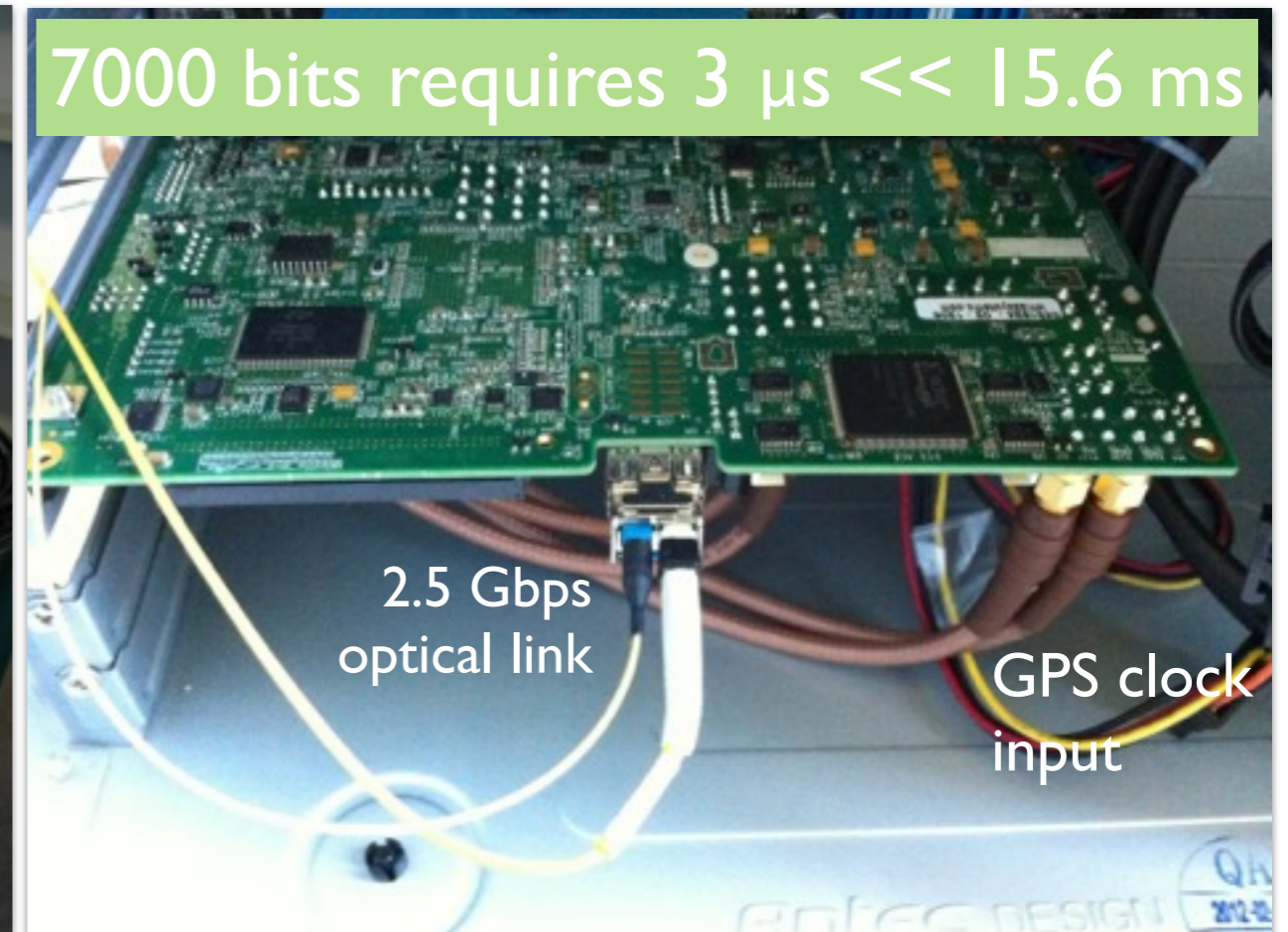


# The classical agents : timing performances

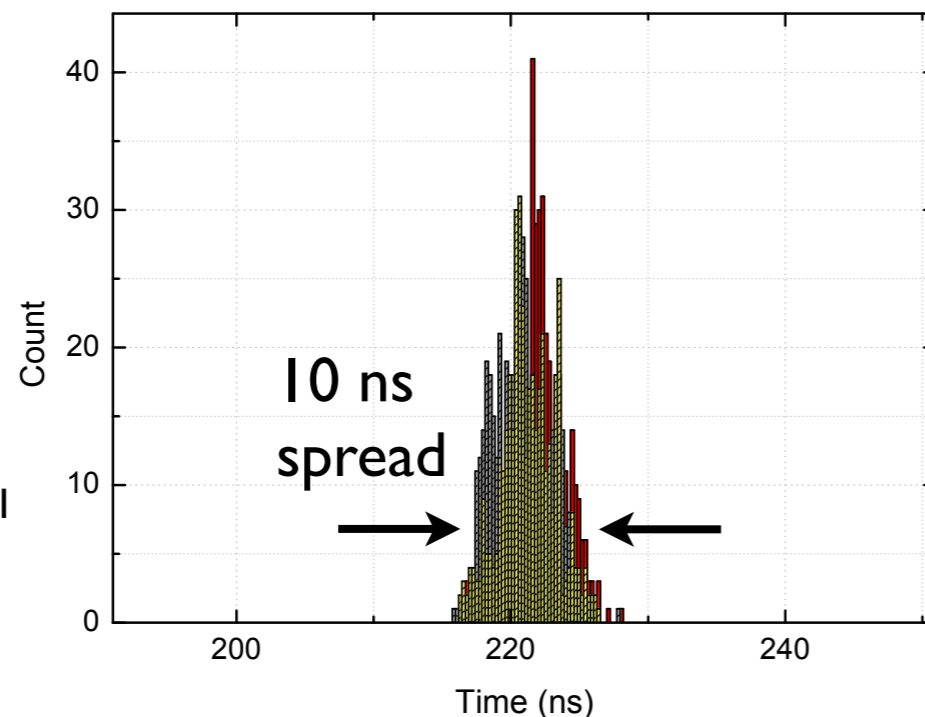
## Classical agents in Geneva



## FPGA boards



Timing accuracy of the FPGAs with a GPS for  $A_1$  and another for  $B_1$

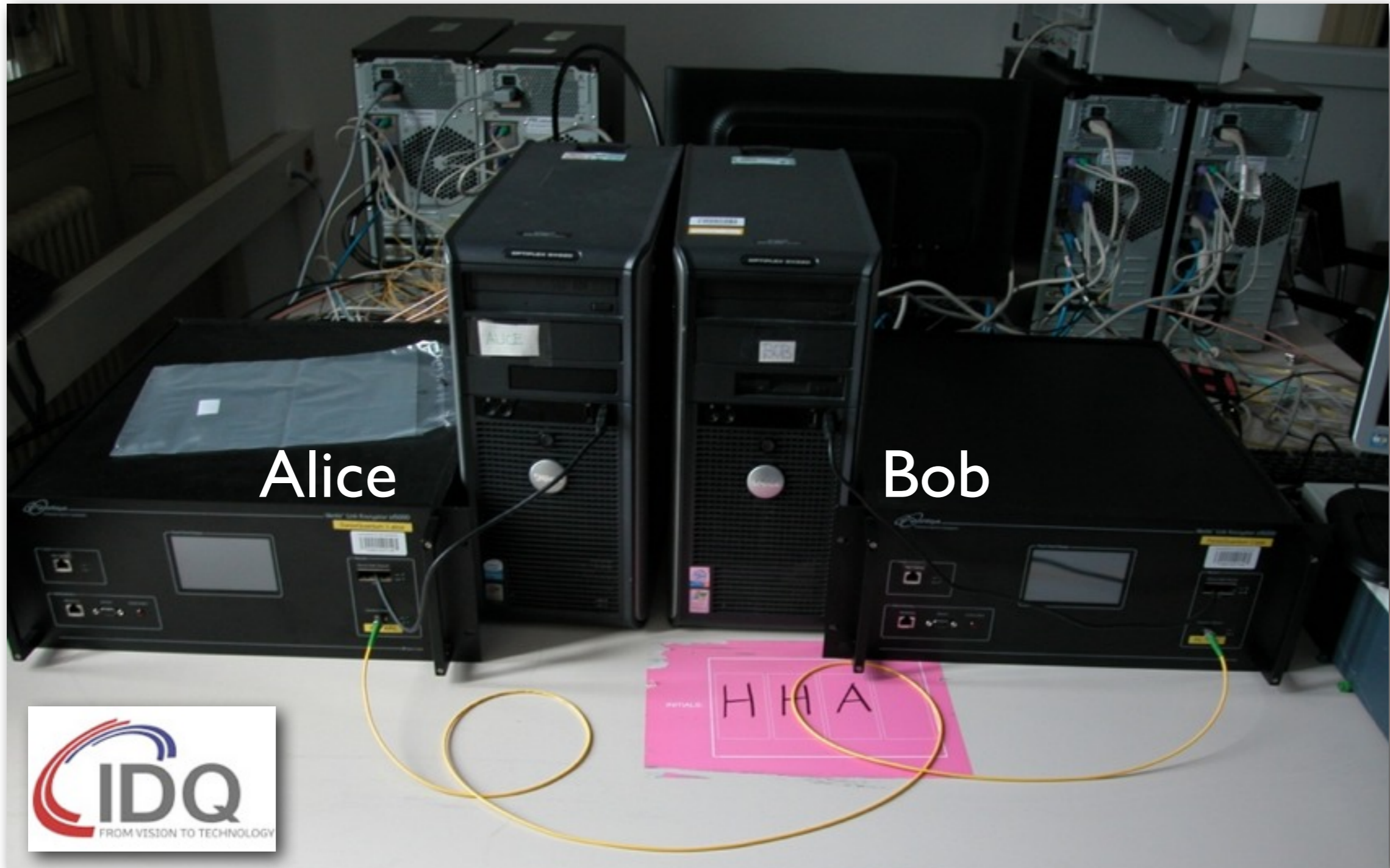


Other tests showed that

- $B_1$  and  $B_2$  are in sync to within 100 ns
- Synchronization is maintained over the 15 ms of the protocol

# The quantum boxes (Geneva)

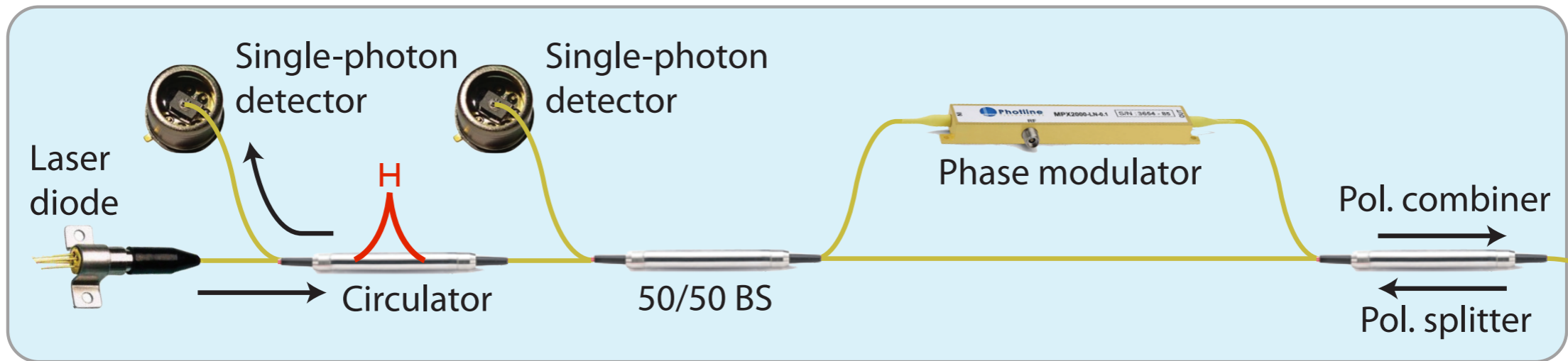
Commercial QKD system by IDQ “Vectis 5100”



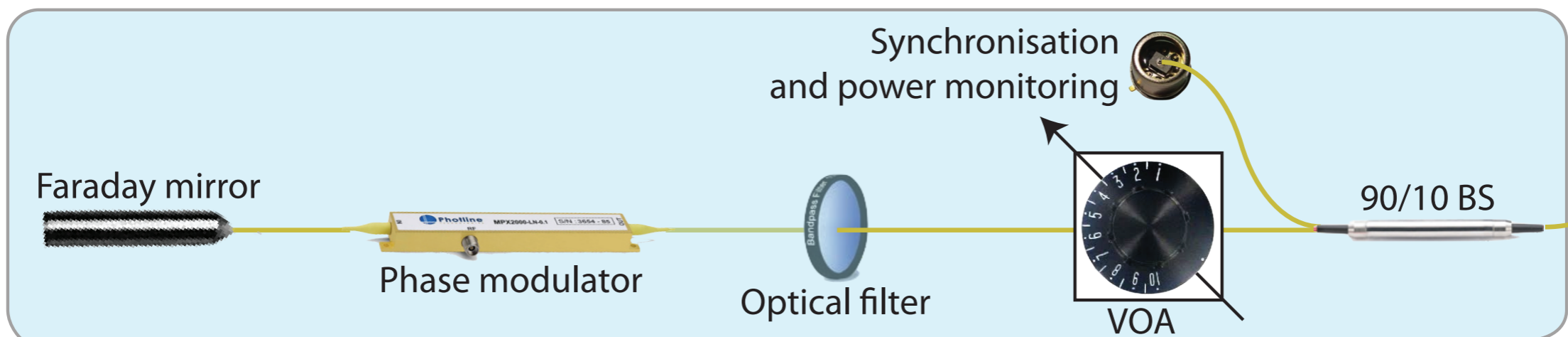


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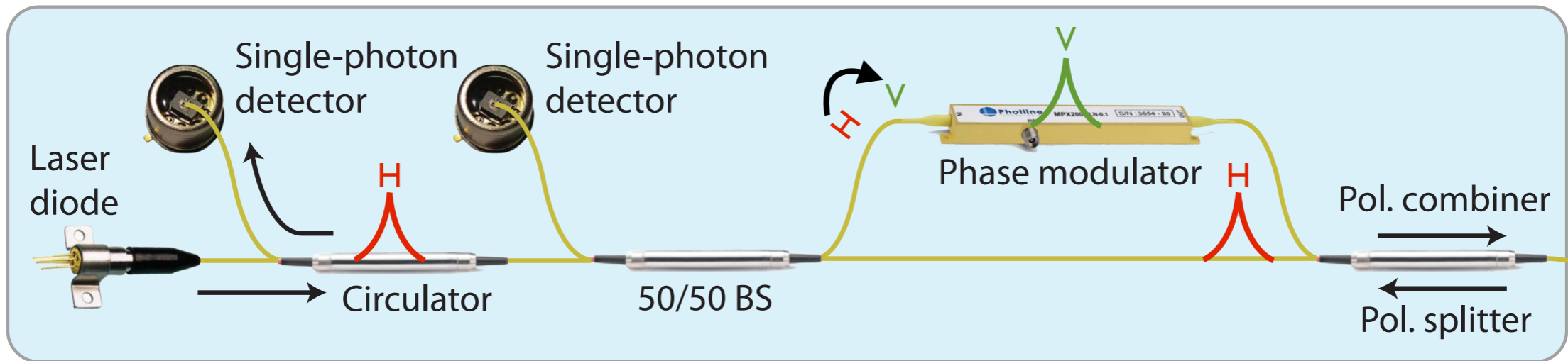


**Alice**

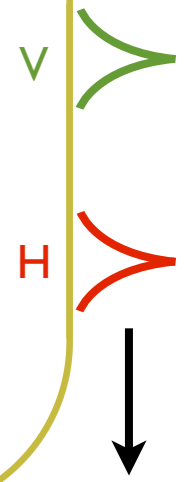
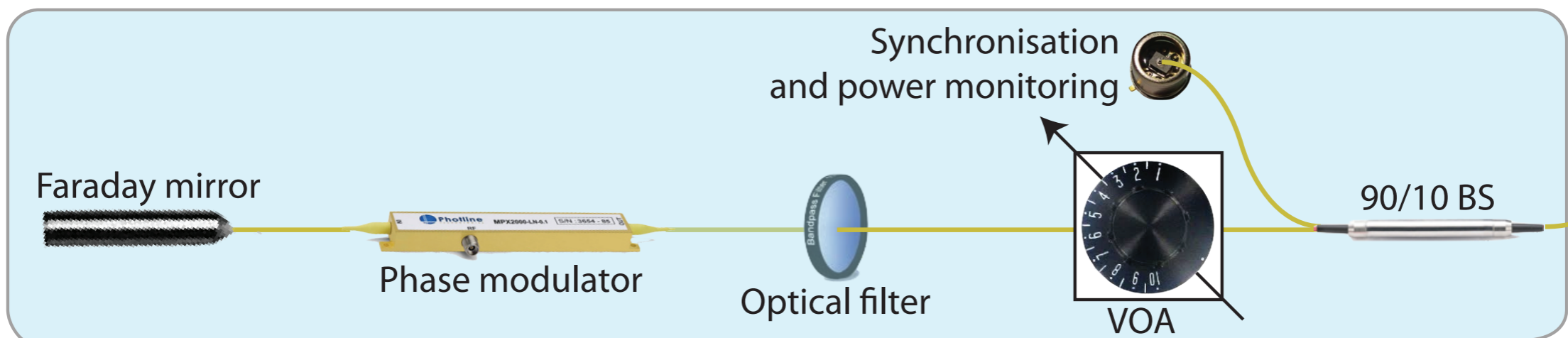


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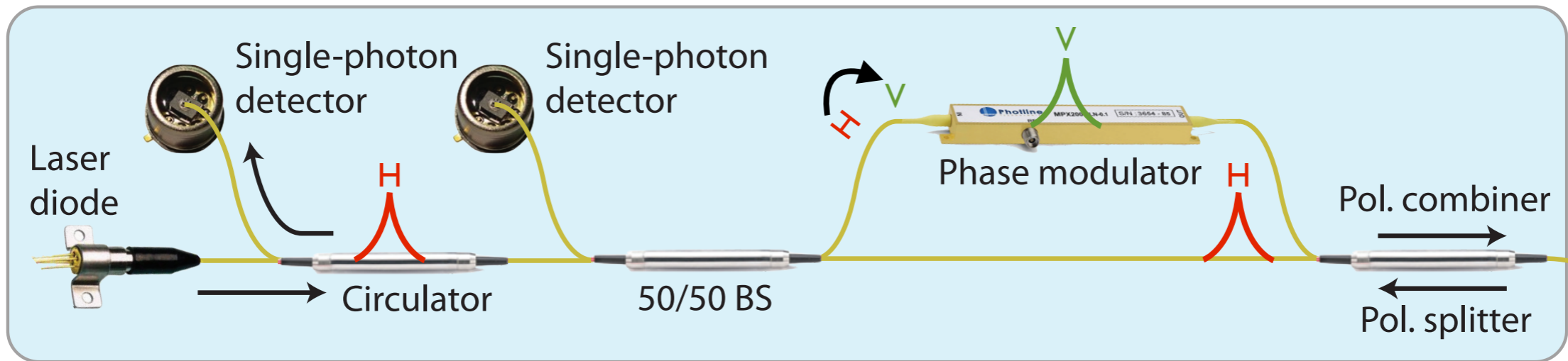
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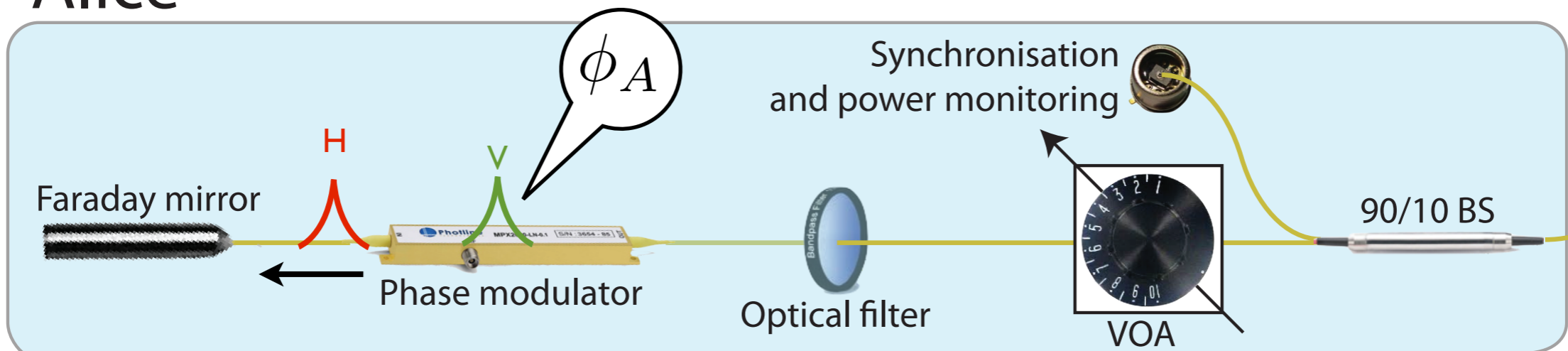


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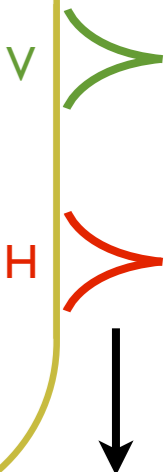
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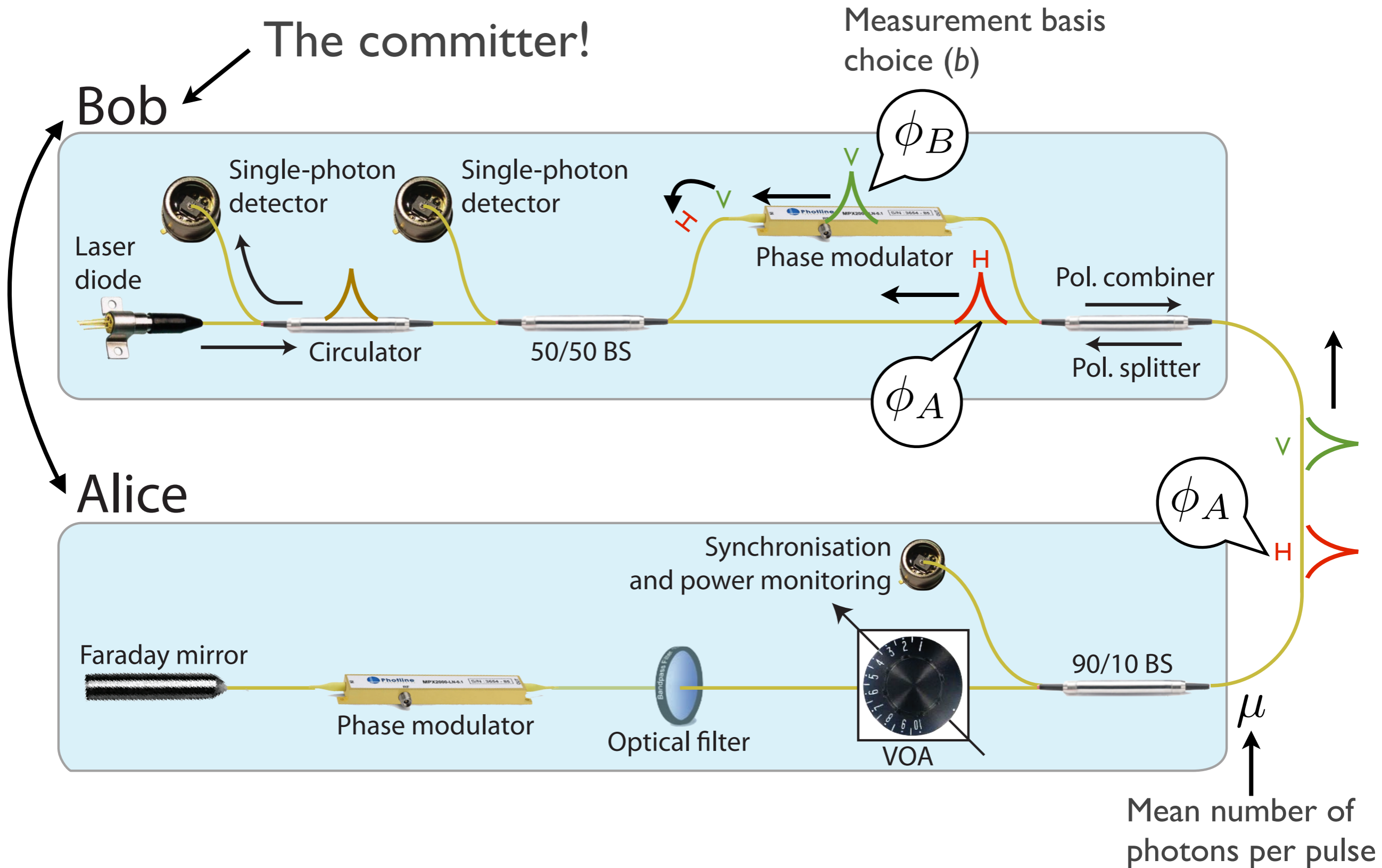
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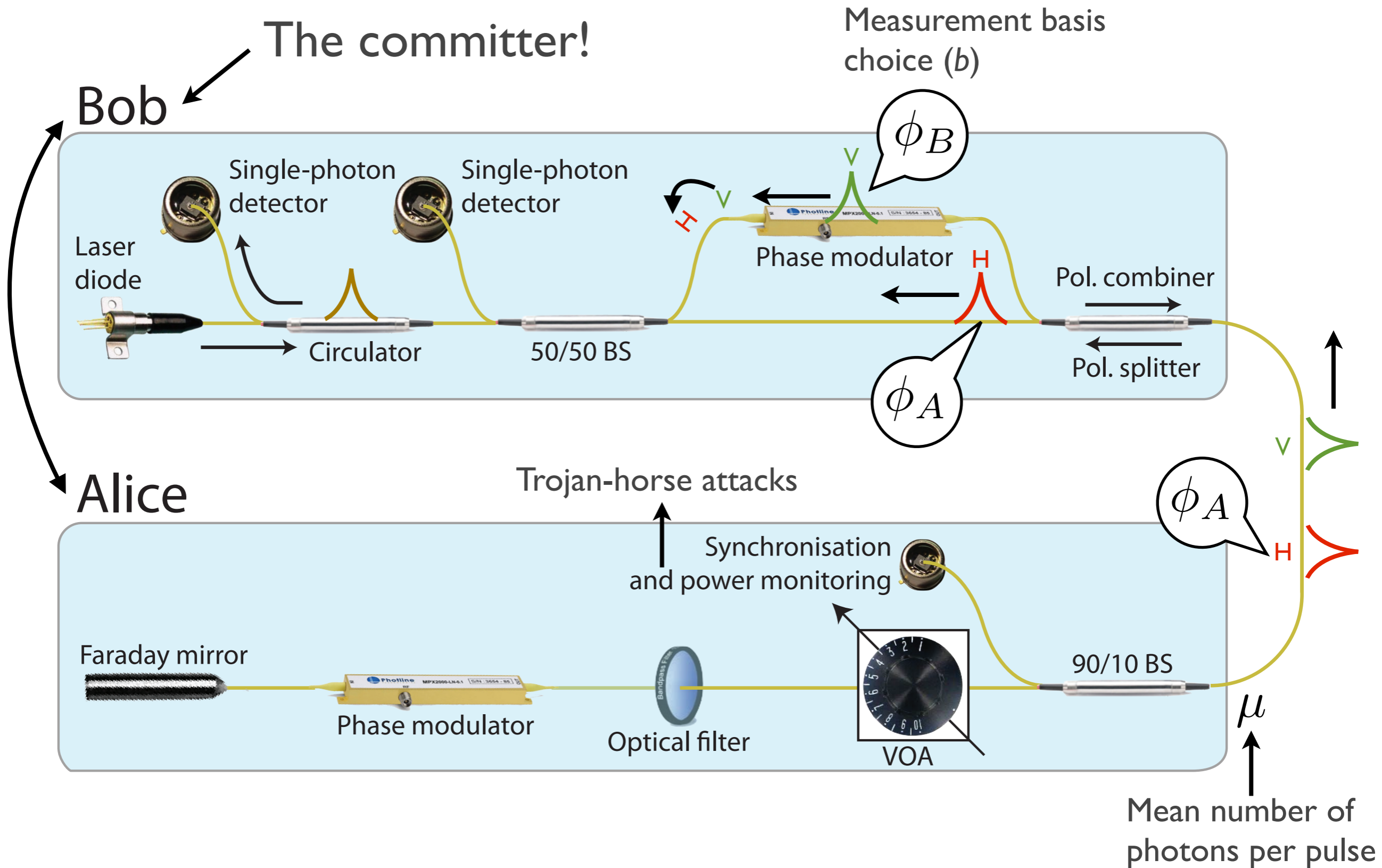
Qubit preparation  
(phase encoding)



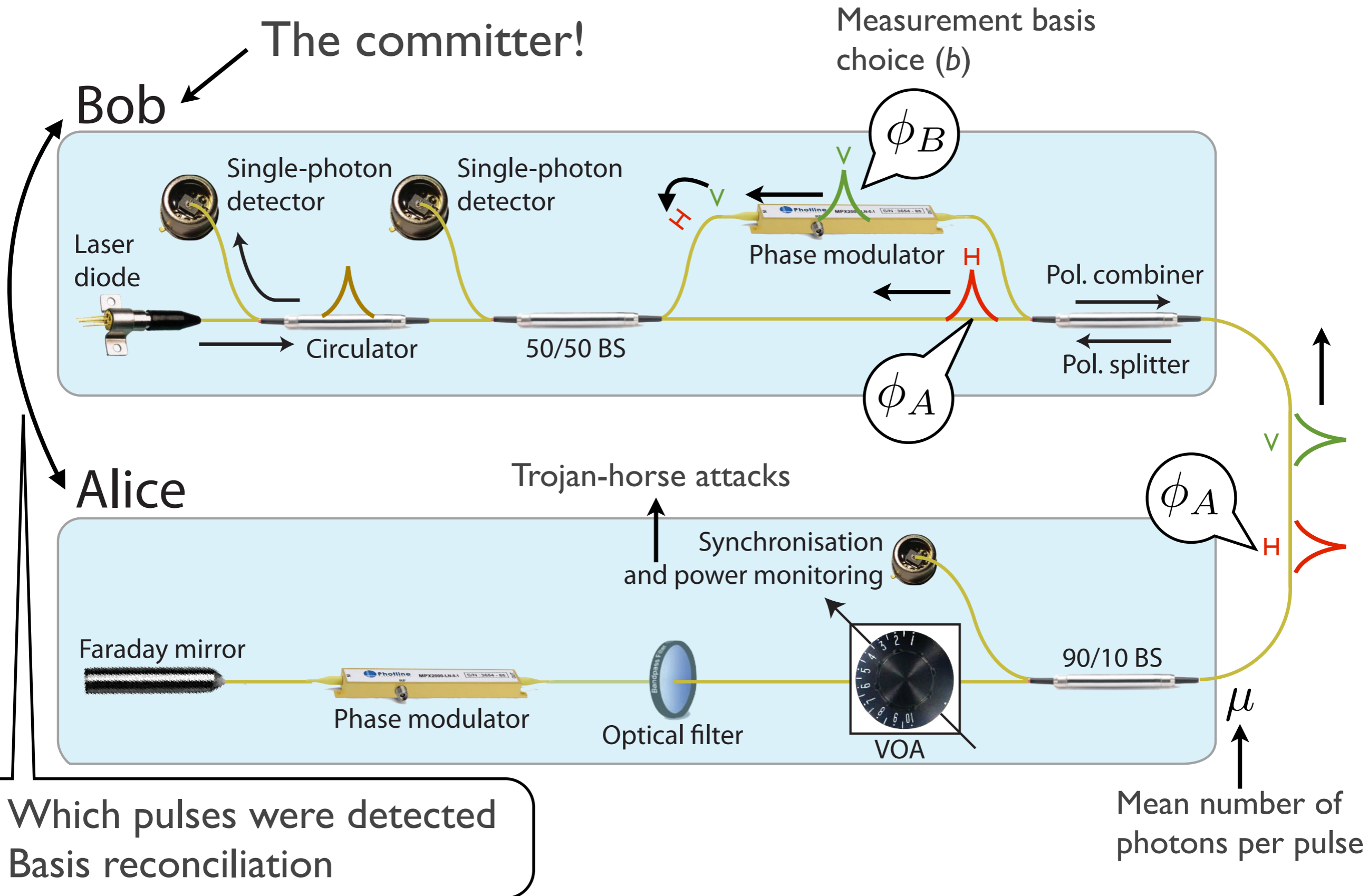
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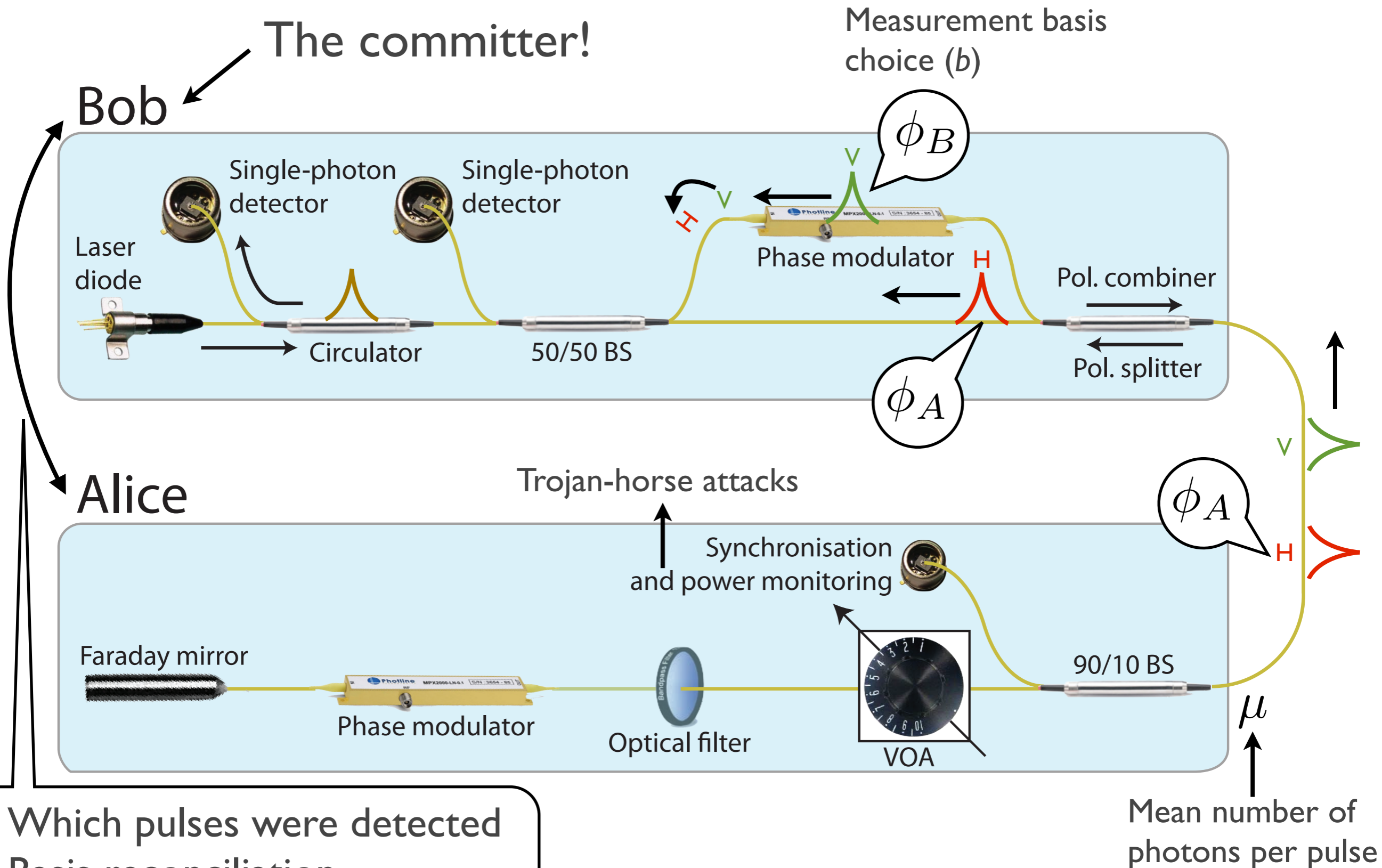
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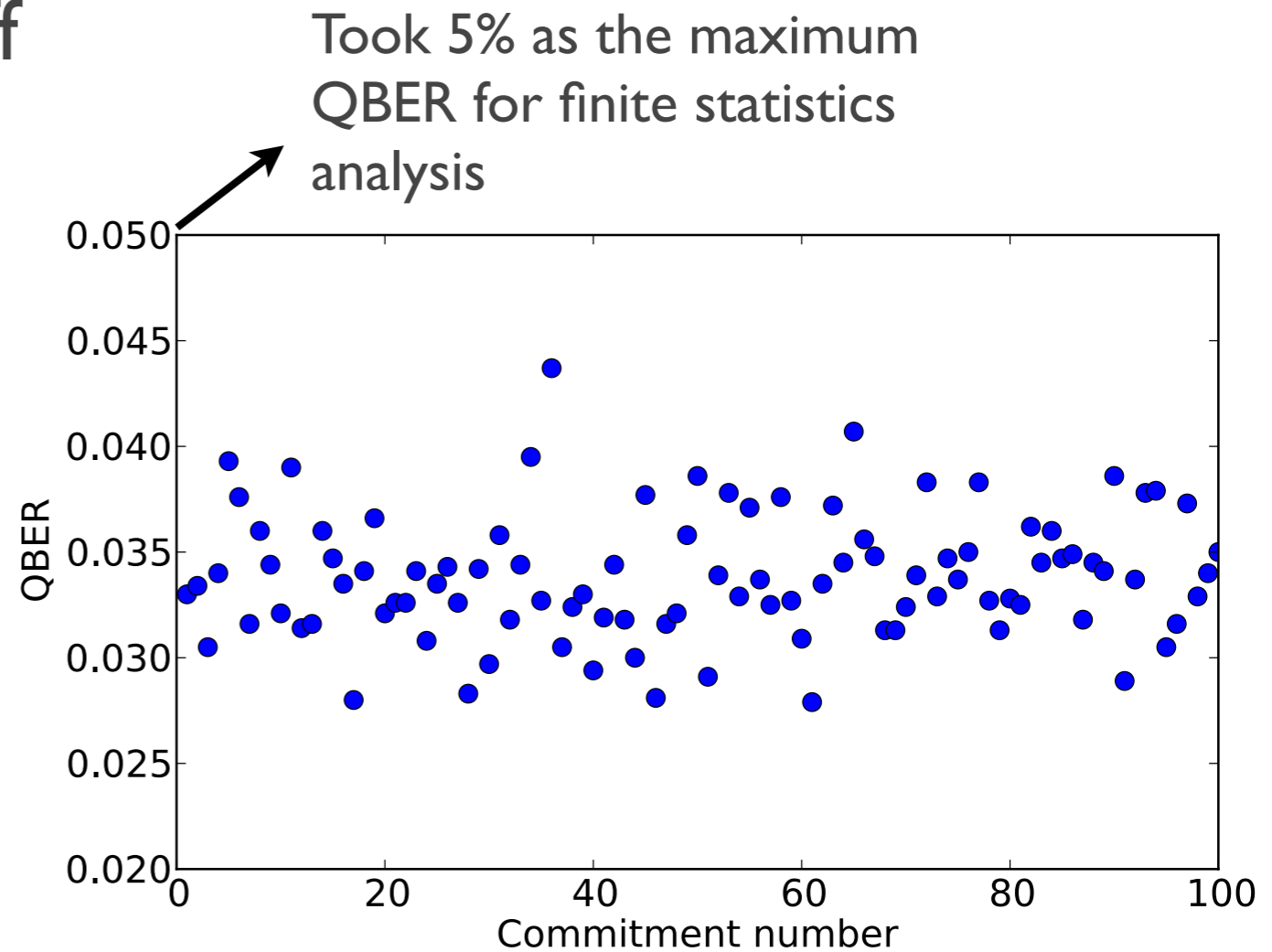
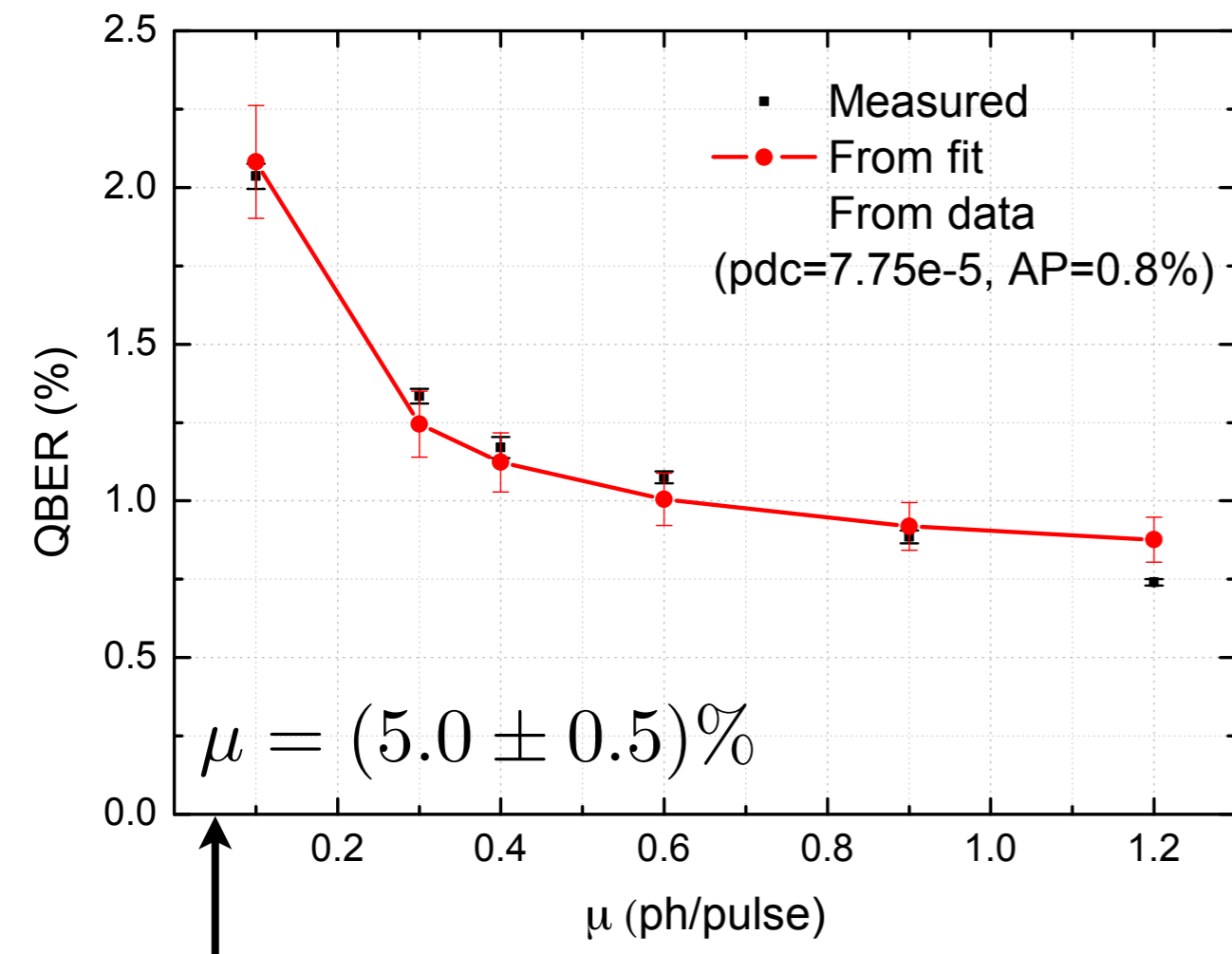
# The quantum boxes (Geneva)



- Which pulses were detected
- ~~Basis reconciliation~~

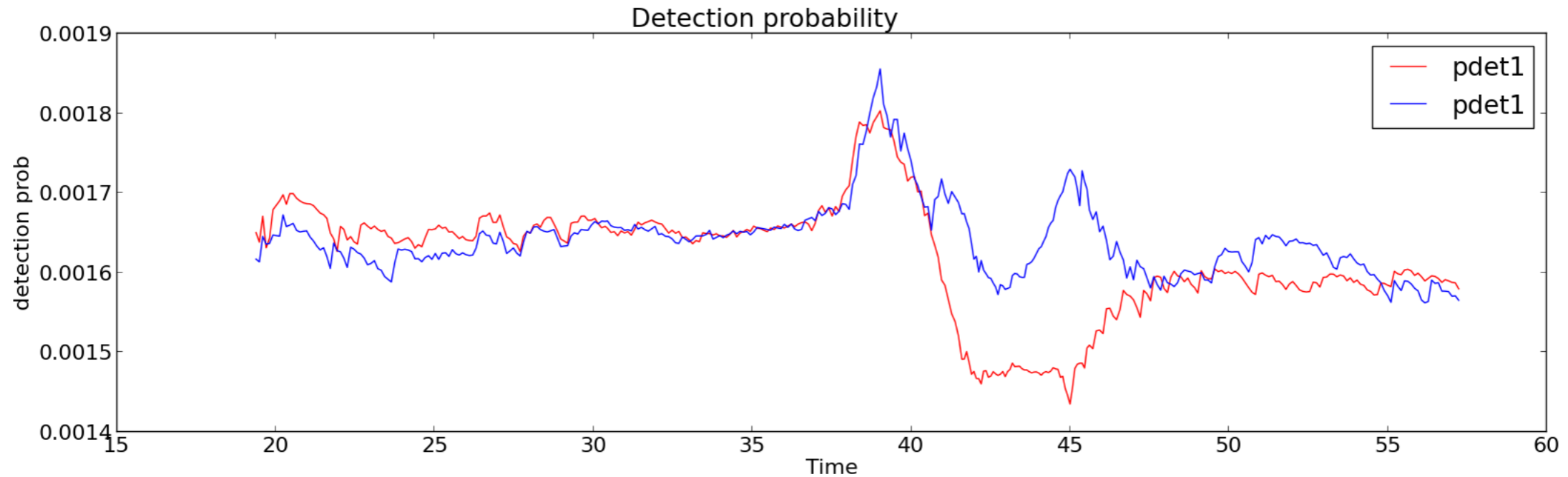
# The quantum boxes (Geneva) : performances

## Choosing $\mu$ : security trade-off



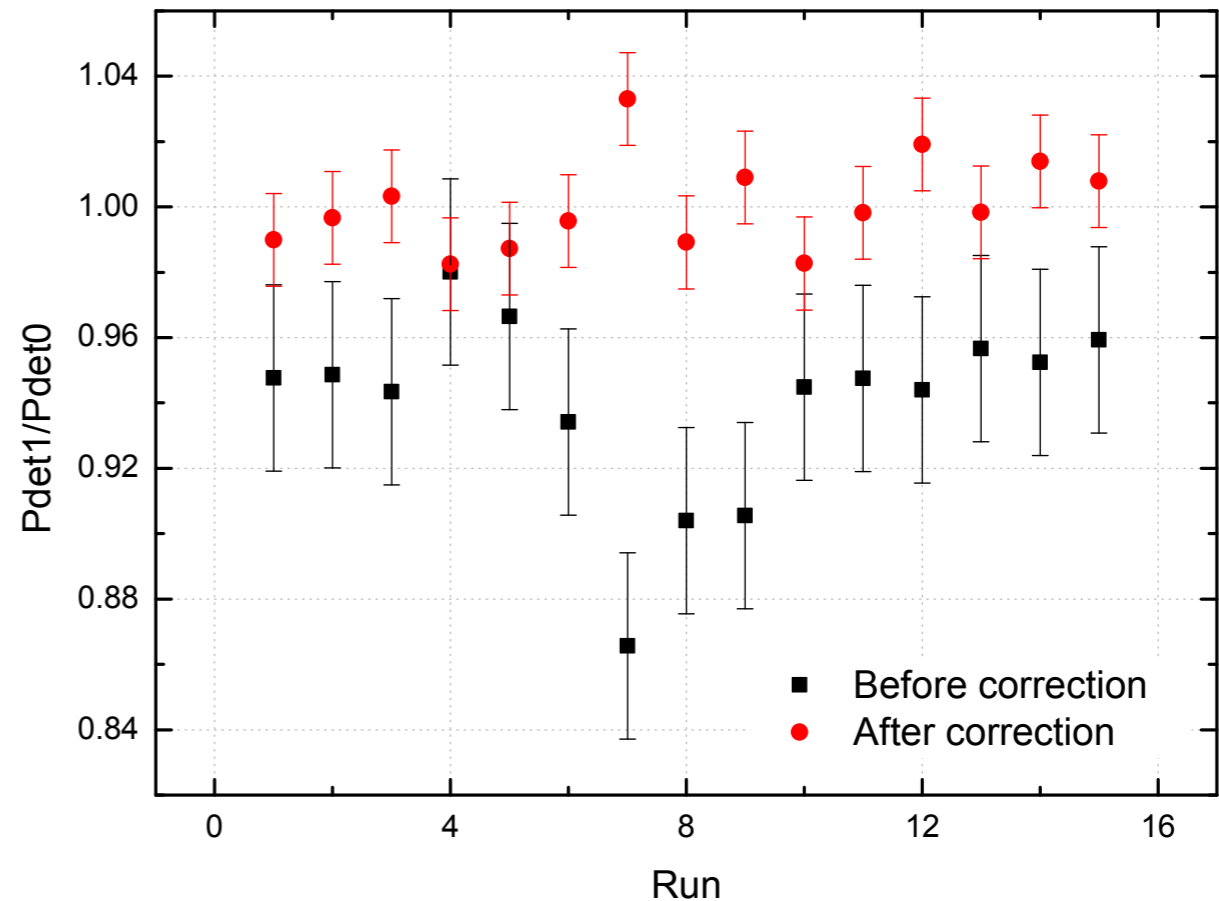
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## Stability of the detection probability : Bob must monitor!



Basis detection probability mismatch: side-channel!

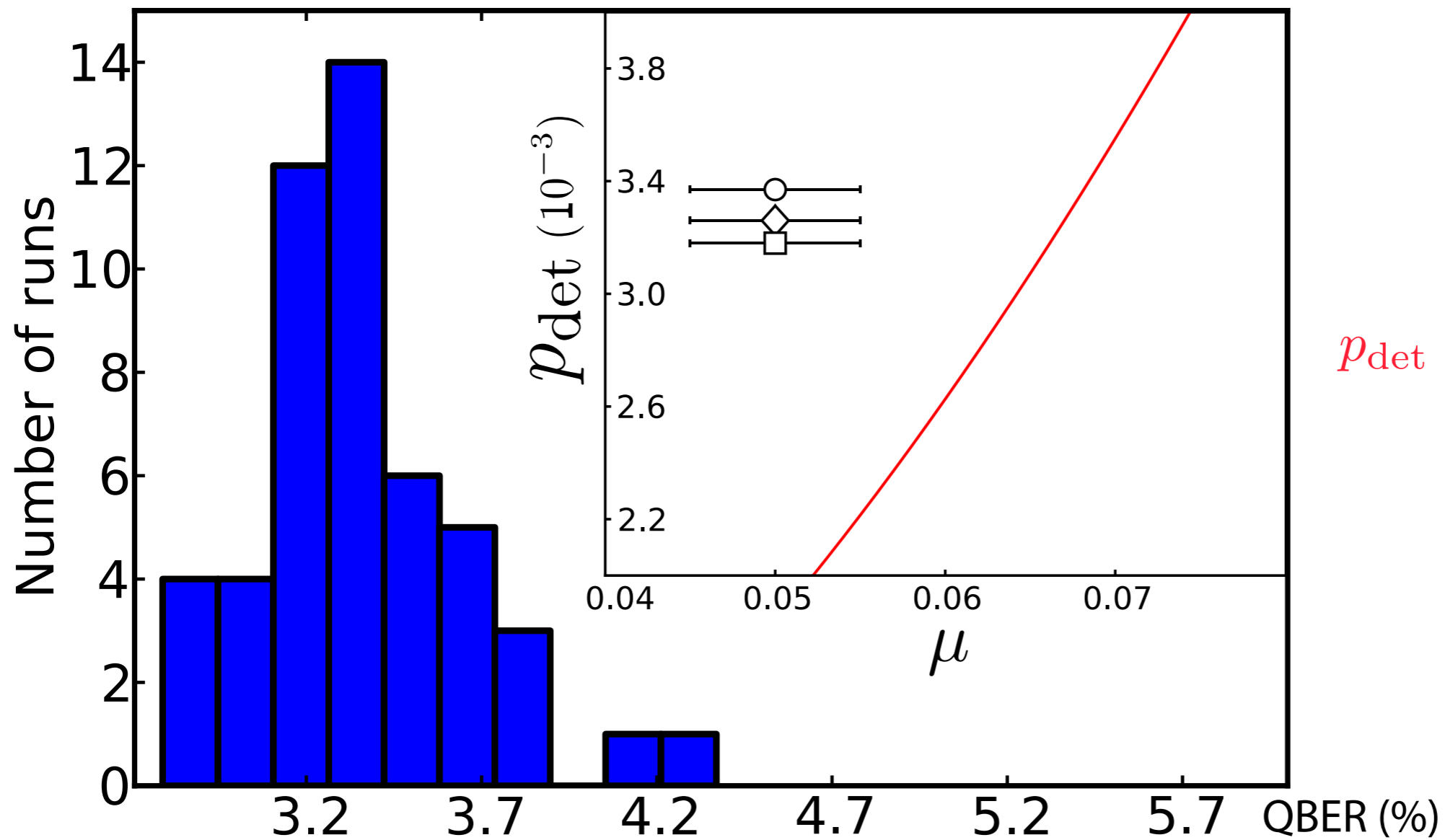
Software bias elimination.





# The quantum boxes (Geneva) : performances

Results: 50 commitments of bit 1 from  
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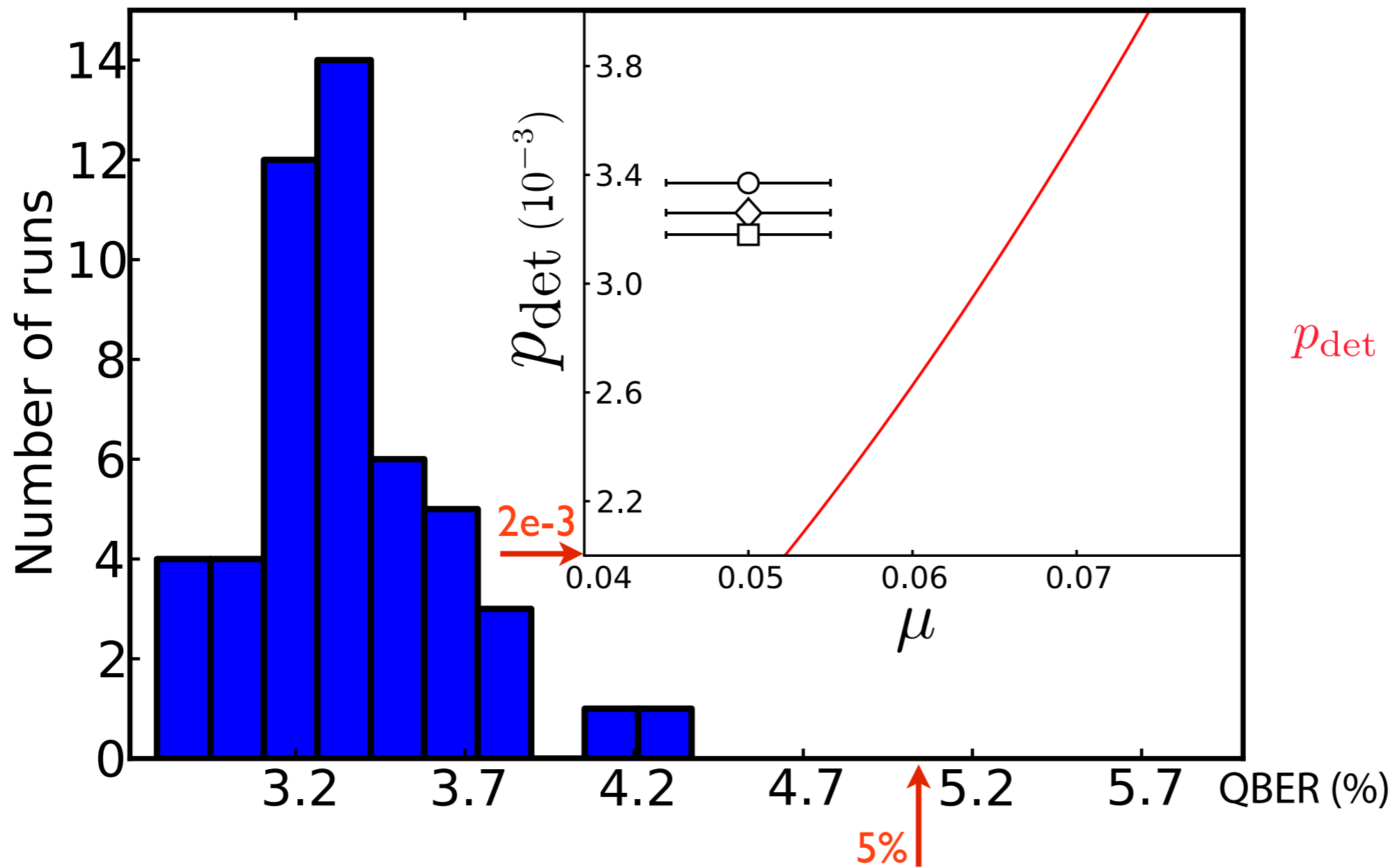


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Security  
parameter

$$\epsilon \leq 5.5 \times 10^{-8}$$

# Summary and outlook

- First implementation of bit commitment using quantum communication and special relativity
- Closing on the maximum commitment time allowed on the surface of the Earth
- Possible extensions for sustained commitments with constant communication at each round? (Kent'05)

