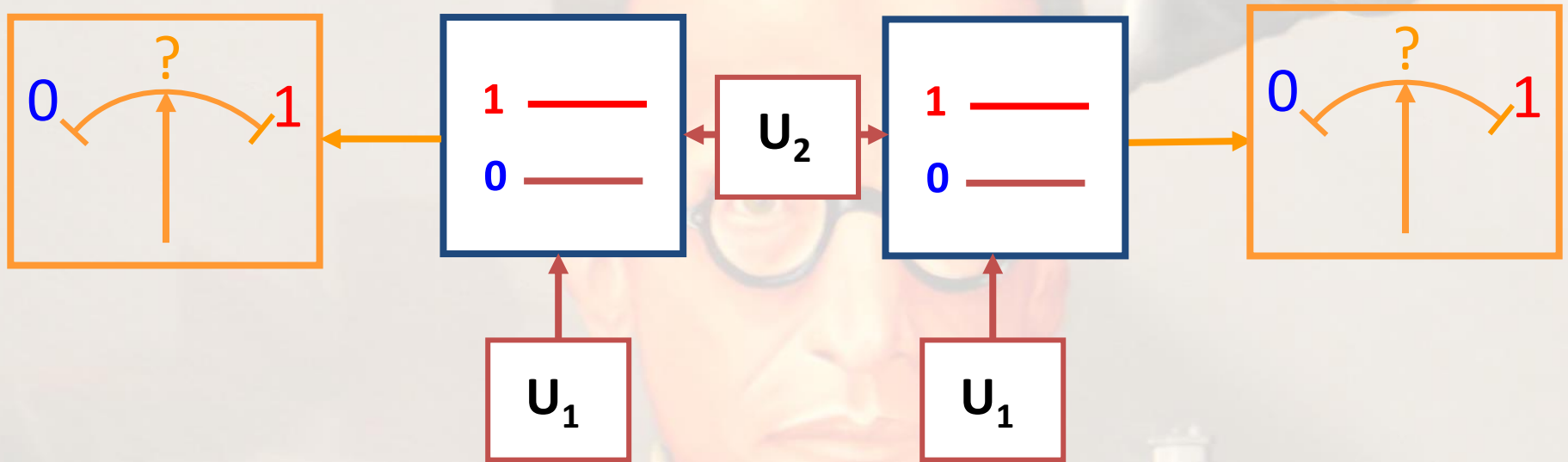


Routes towards quantum information processing with superconducting circuits



Daniel Estève
Quantronics
SPEC CEA Saclay

ED.C.04

Quantum Mechanics: resources for information processing

1930s: quantum weirdness



1960s: Bell inequalities

1980s: quantum violation demonstrated

A. Aspect et al.

●-----●
entangled states

$$|left+, right-\rangle + |left-, right+\rangle$$

breakthrough:
a resource for
computing

David
Deutsch



Richard
Jozsa

EPR



Albert Einstein



Boris Podolski



Nathan Rosen



John Bell

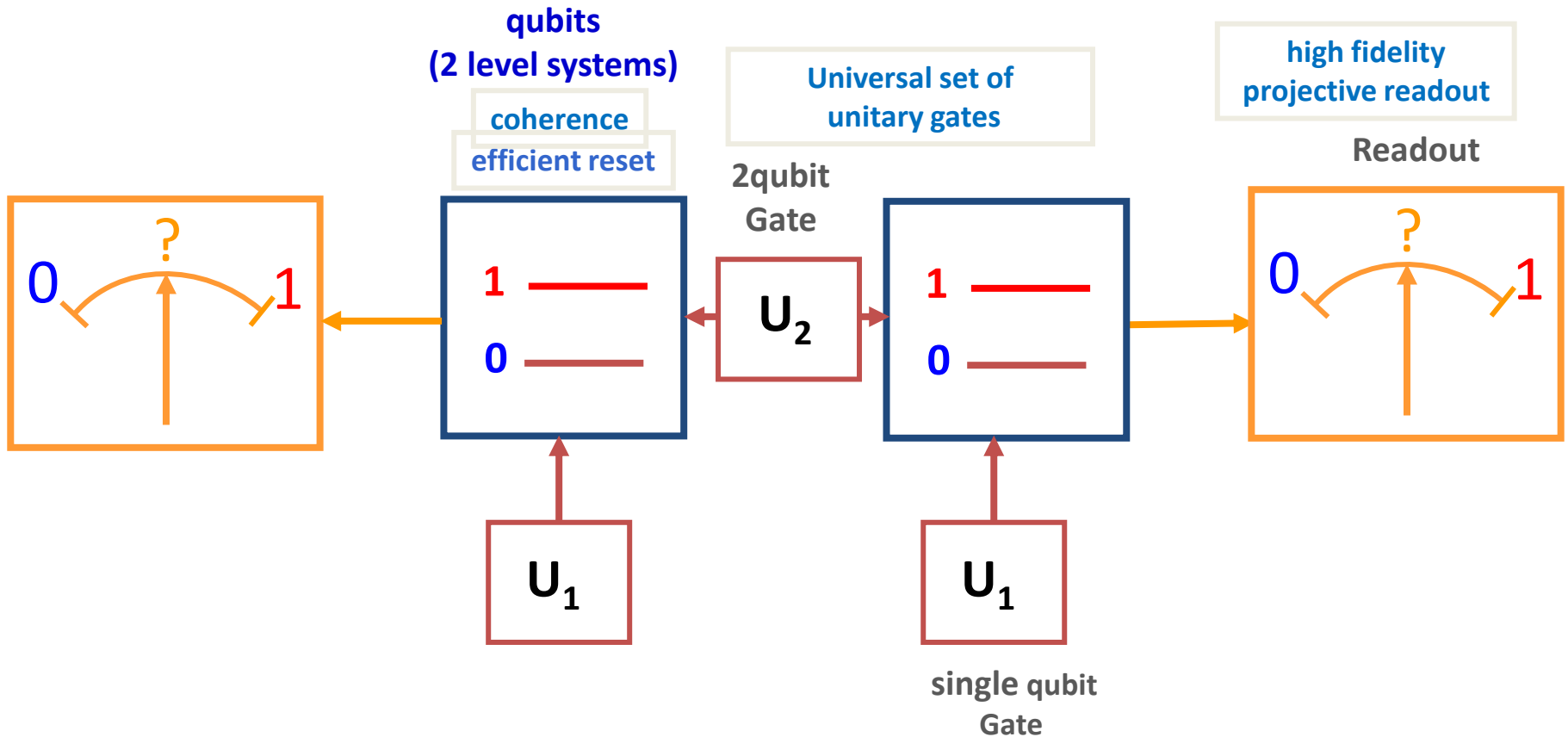


Alain Aspect

A second
quantum revolution ?

Blueprint of a quantum processor based on quantum gates

Specifications: "DiVincenzo criteria"



Electrical implementations ?

Can (macroscopic) electrical circuits be quantum (usually not !)

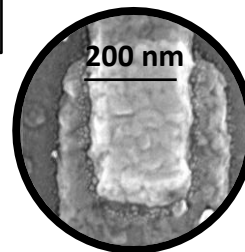
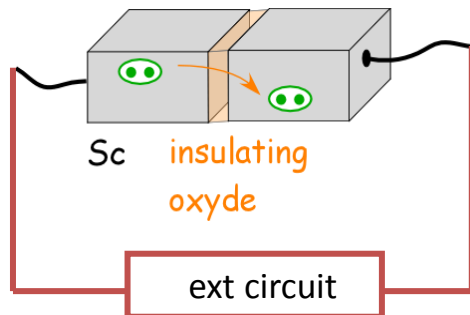
Jack S. Kilby handling the first integrated circuit



electrical variables
usually not quantum

ALL OF THEM ?

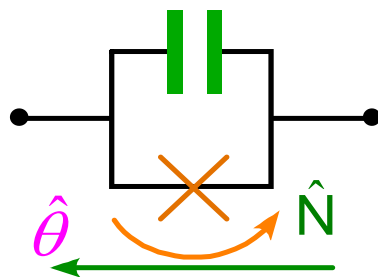
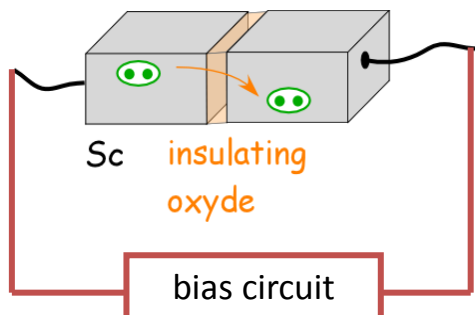
Superconductor/insulator/Superconductor
JOSEPHSON JUNCTION



Al/AIO_x/Al
junction



A quantum electrical component : the Josephson junction



1 single degree of freedom:

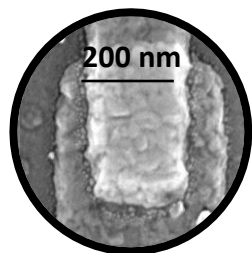
$$\Phi(t) = \int_{-\infty}^t V(t') dt' \quad Q(t) = \int_{-\infty}^t i(t') dt'$$

$$[\hat{\Phi}, \hat{Q}] = i\hbar \rightarrow [\hat{\theta}, \hat{N}] = i$$

θ and N conjugated variables

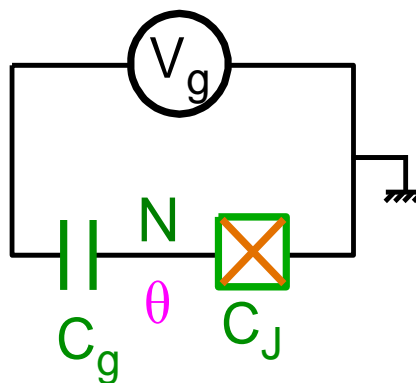
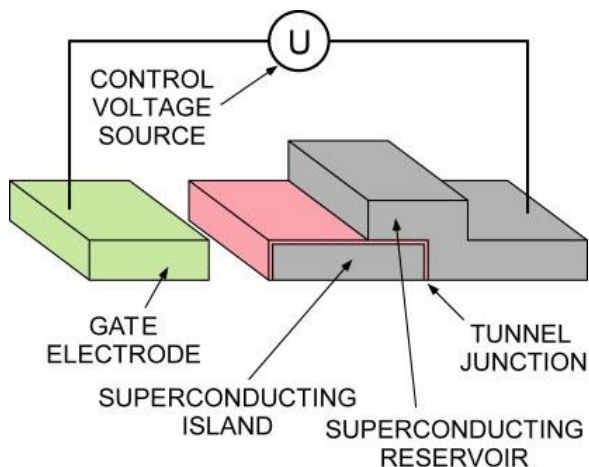
Hamiltonian:

$$H = -E_J \cos \hat{\theta} + H_{ELM}$$



Al/AIOx/Al
tunnel junction

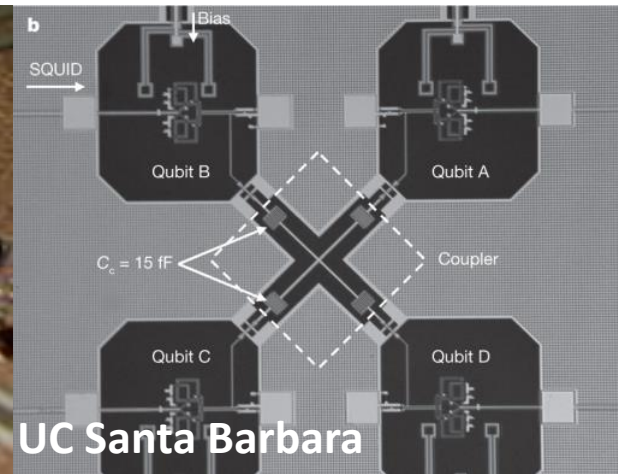
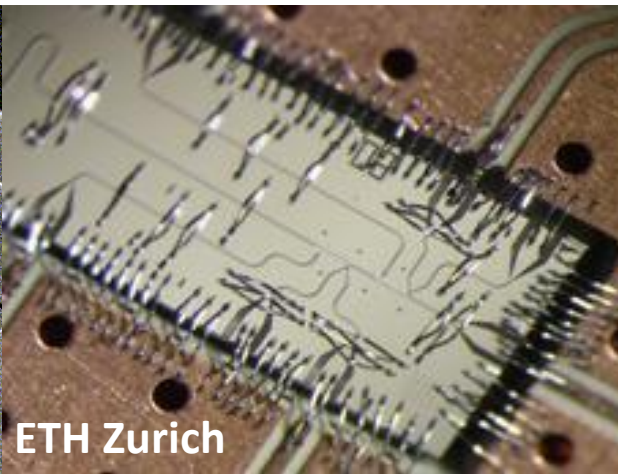
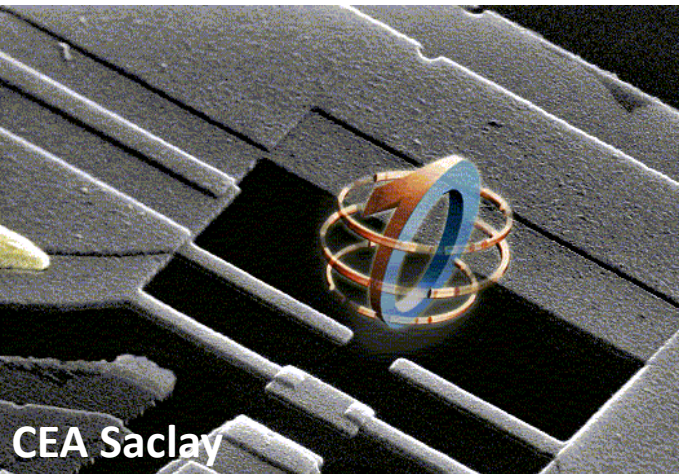
the single Cooper pair box



$$\hat{H} = E_C (\hat{N} - N_g)^2 - E_J \cos \hat{\theta}$$

reduced gate charge: $N_g = C_g V_g / 2e$

Superconducting Josephson quantum circuits



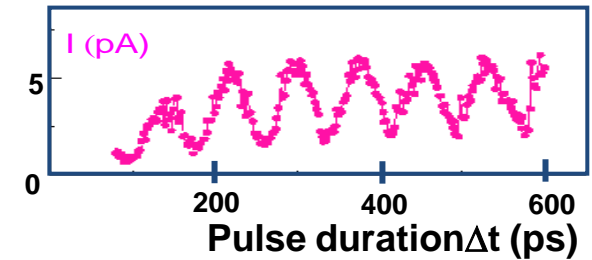
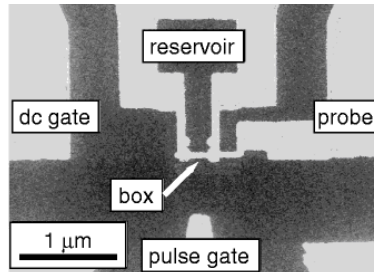
1. Quantum behavior demonstrated in 1980s
2. Since 1999 qubits with increasingly long coherence times.
3. **Potentially scalable**

Other electrical implementations :
quantum dots in 2DEGs

The Cooper Pair Box: from charge to phase

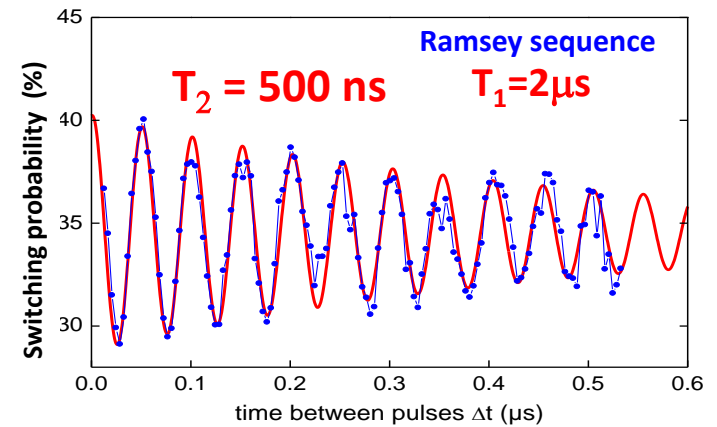
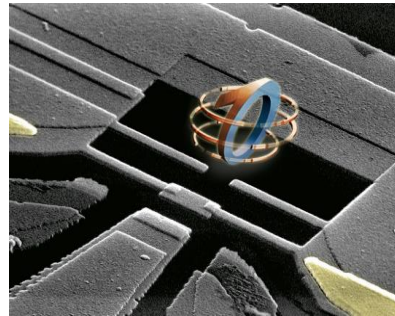
first electrical qubit : Cooper pair box

Nakamura, Pashkin & Tsai (NEC, 1999)



First operational qubit : quantronium, single-shot readout, protected against dephasing

Vion et al., (Quantronics, 2002)



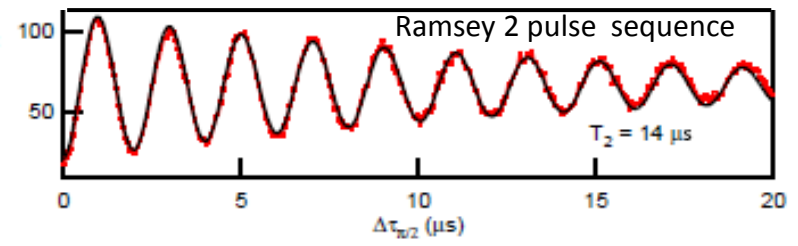
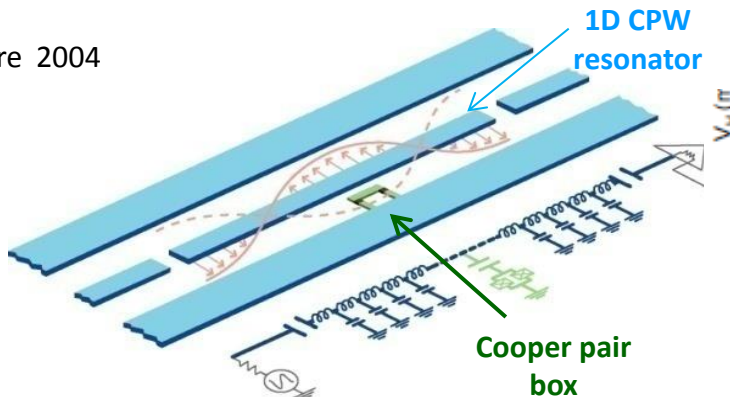
Circuit QED: Cooper pair box in a microwave cavity (2D, 3D)

Schoelkopf lab., Yale

-Wallraff et al., Nature 2004

-Koch et al., 2007

-Paik et al., PRL **107**, 240501 (2011)

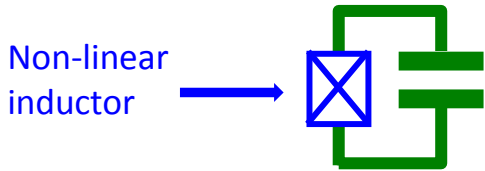


Longer coherence times, up to $\sim 25 \mu\text{s}$ (2D), $100 \mu\text{s}$ (3D)

The transmon Cooper pair box: circuit QED

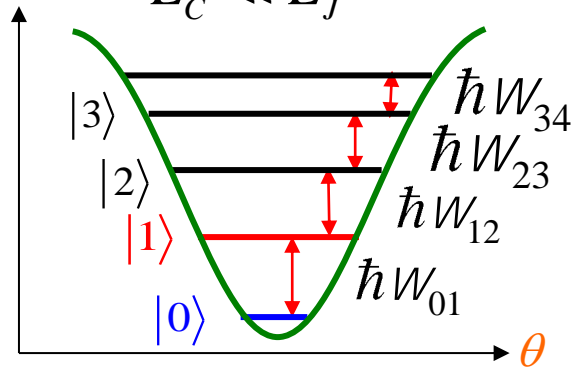
(inspired from cavity QED)

Cooper pair box
in the phase regime



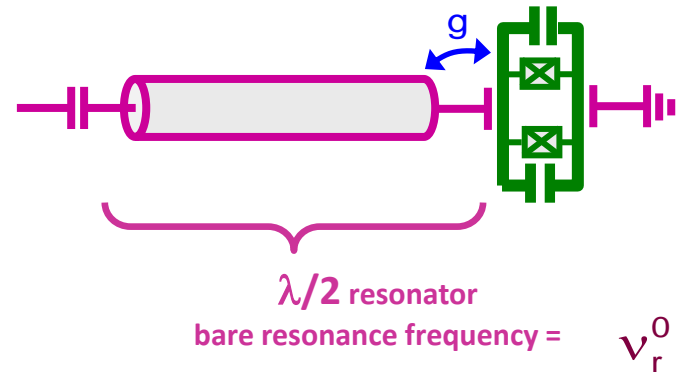
$$H_{\text{transmon}} = E_C \hat{N}^2 - E_J \cos \hat{q}$$

$$E_C \ll E_J$$

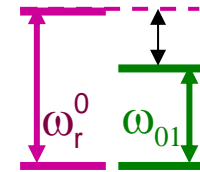


a non linear resonator
at the **single** photon level

Circuit QED:
dispersive regime



$$|\Delta| = |\omega_{01} - \omega_r^0| \gg g$$



$$\hat{H}_{\text{eff}} = -\frac{\hbar}{2} (\omega_{01} + \chi) \hat{\sigma}_z + \hbar (\omega_r^0 - \chi \hat{\sigma}_z) \hat{a}^+ \hat{a}$$

qubit Stark shift

qubit controlled Cavity pull

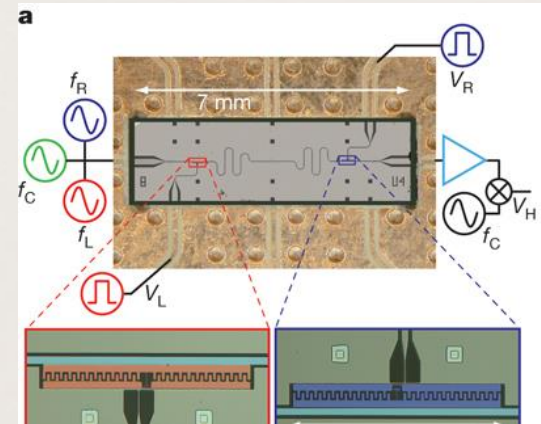
Status of SC quantum processors

Schoelkopf Lab, Yale University

DiCarlo et.al., Nature 2009

Two-Qubit Grover Search

**No individual readout:
not operational**



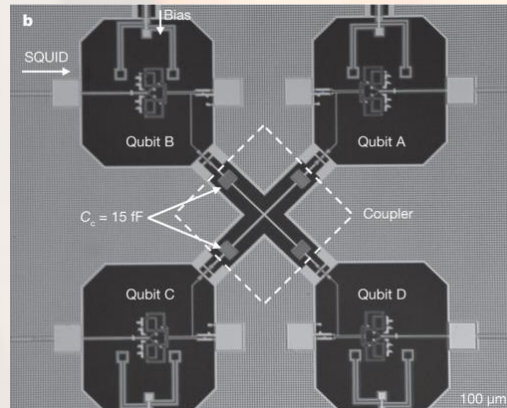
Martinis Lab, UC Santa Barbara

Yamamoto et.al., PRB 82 2010, Nat Phys 2012

Two-Qubit Deutsch-Josza Algorithm

Factorization of 15

individual destructive readout

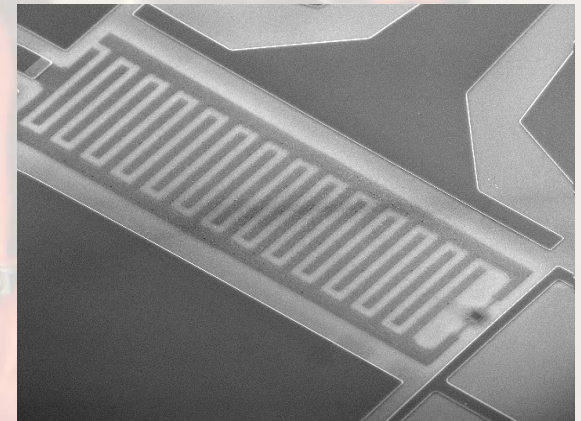


Quantronics, CEA

Dewes et. al., PRL & PRB 2012

Grover Search Algorithm on 4 items

Individual non-destructive readout



**Quantum speedup demonstrated
on elementary cases**

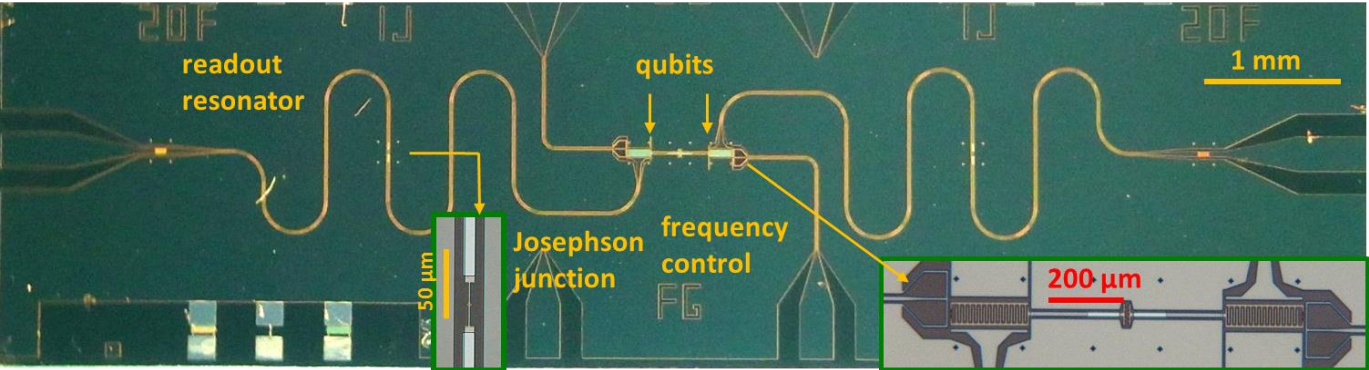
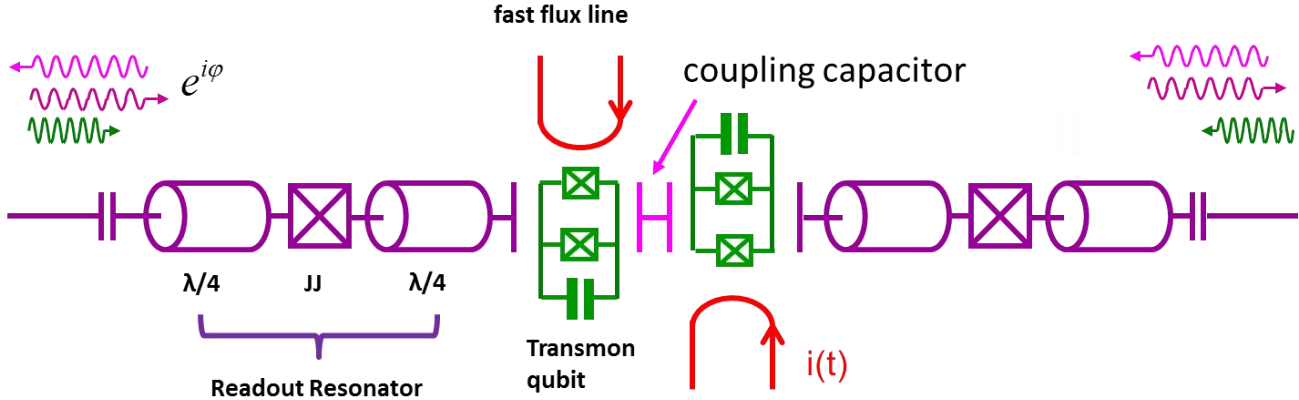
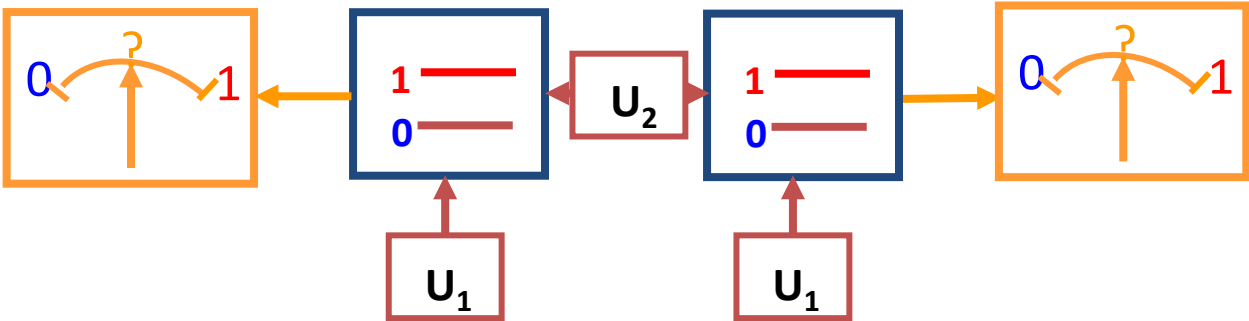
Why slow progress ?

**Difficult
scalability issues**

Quantum coherence in complex architecture
Hifi readout of qubit register
Quantum error Correction

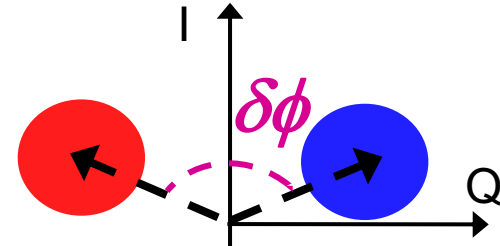
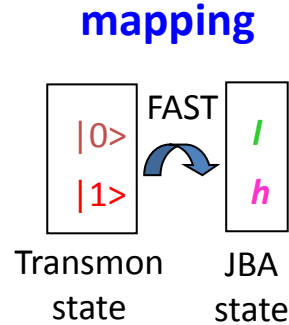
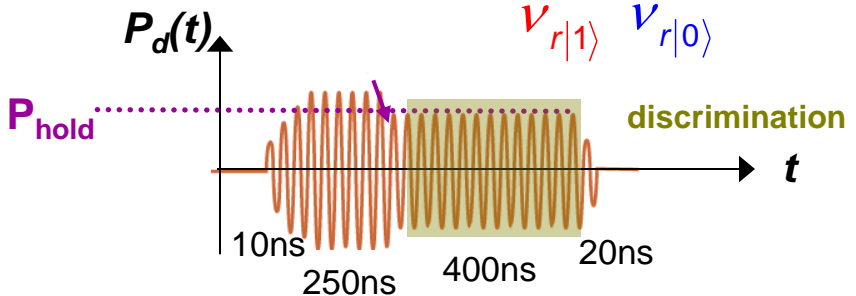
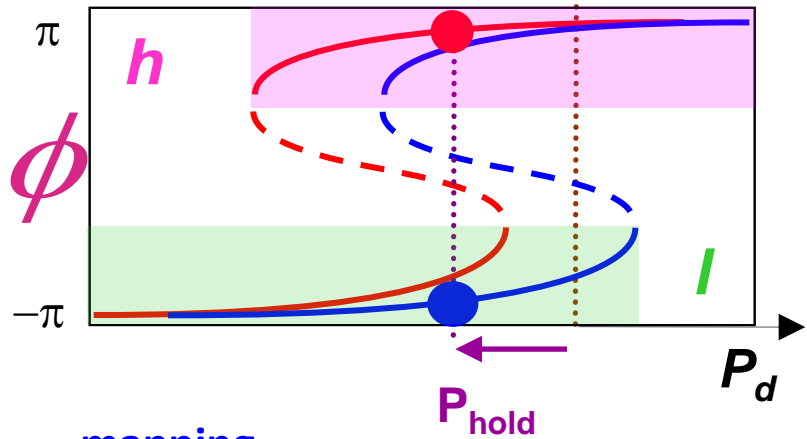
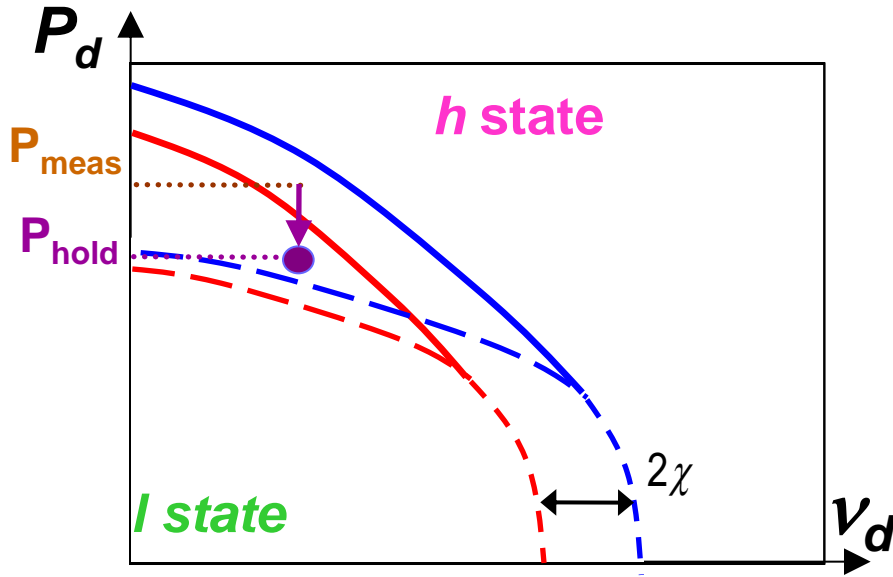
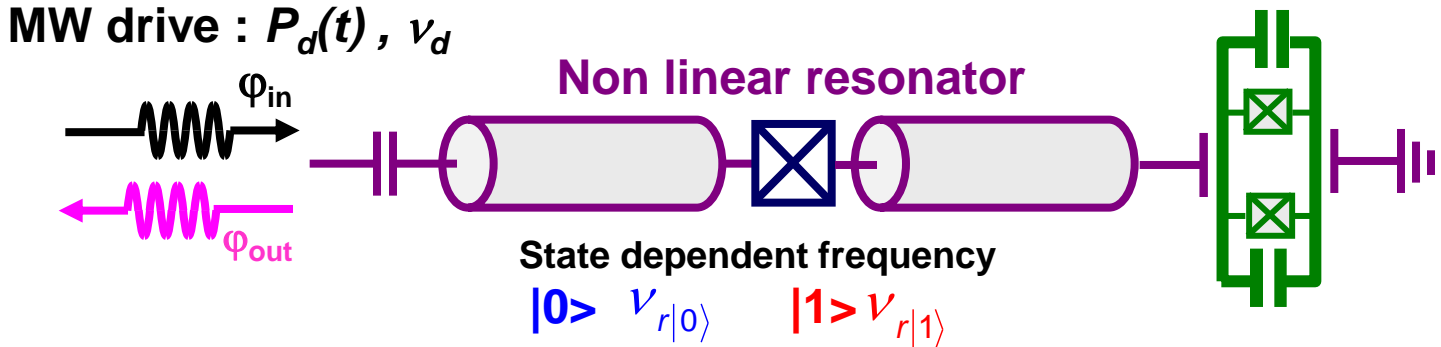
An operational two-qubit (4 states) processor

Dewes et al., Phys. Rev. Lett. 108, 057002 (2012)

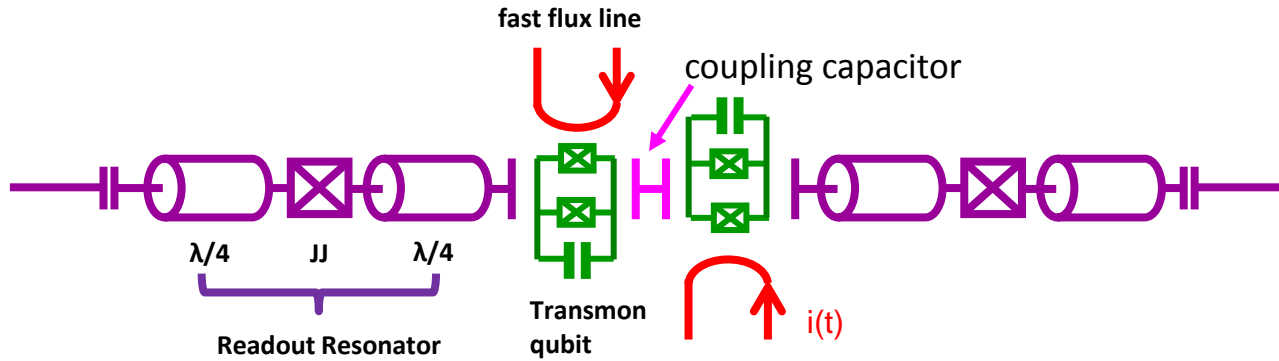


Transmon readout with a non-linear resonator

Josephson Bifurcation Amplifier: Siddiqi et al., Phys.Rev.Lett 93 (2004)
 Transmon Readout: Mallet et al. Nature Physics 5, 791 - 795 (2009)



Switchable SWAP interaction



$$H / \hbar = -\frac{\omega_{01}^I}{2} \sigma_z^I - \frac{\omega_{01}^{II}}{2} \sigma_z^{II} + \overbrace{g (\sigma_+^I \sigma_-^{II} + \sigma_-^I \sigma_+^{II})}^{H_{\text{int}}}$$

Off resonance: $|\omega_{01}^I - \omega_{01}^{II}| \gg g$ no effect of coupling

On resonance: $\omega_{01}^I = \omega_{01}^{II}$

$$U_{\text{int}}(t) = \begin{array}{c} \text{00} \quad \text{10} \quad \text{01} \quad \text{11} \\ \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(gt) & -i \sin(gt) & 0 \\ 0 & -i \sin(gt) & \cos(gt) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{array} U_{\text{int}}\left(\frac{\pi}{2g}\right) = \begin{array}{c} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1/\sqrt{2} & -i/\sqrt{2} & 0 \\ 0 & -i/\sqrt{2} & 1/\sqrt{2} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \sqrt{i\text{SWAP}} \end{array}$$

➔ universal gate : $\sqrt{i\text{SWAP}}$

A quantum algorithm for the search problem

The 4 state case: $x, y \in \{00,01,10,11\}$

Game: find **y** by calling the discriminating function **f** once only

$$f_y(x) = \begin{cases} 1, & x = y \\ 0, & x \neq y \end{cases}$$



$$f_{01}(00) = 0$$



$$f_{01}(01) = 1$$



$$f_{01}(10) = 0$$



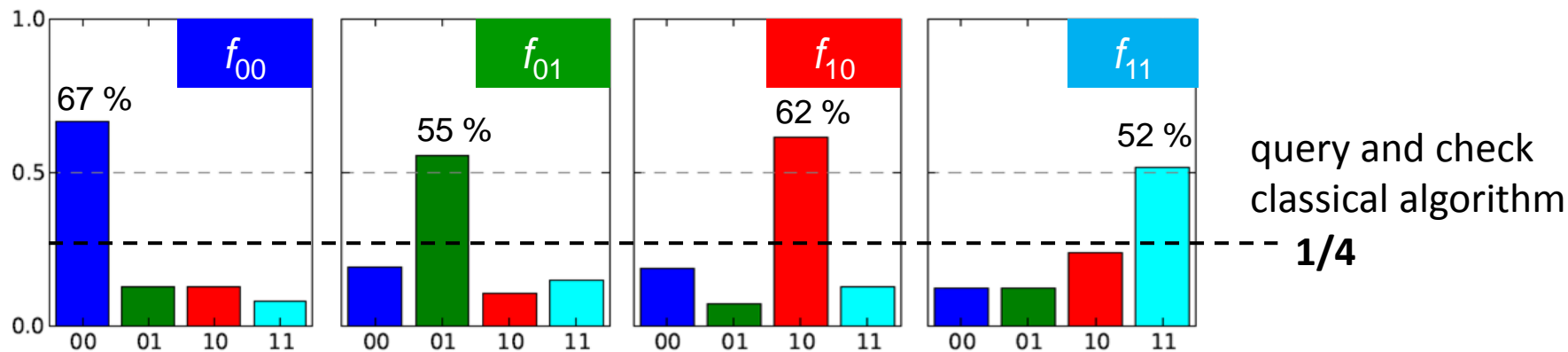
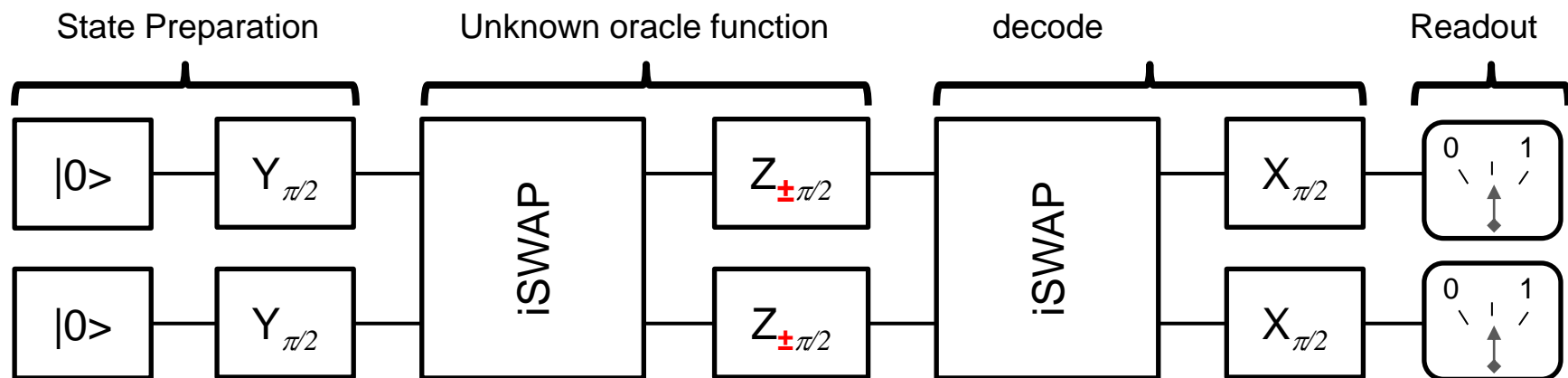
$$f_{01}(11) = 0$$

Classical "Guess and check strategy " success probability : 1/4

Quantum Grover search quantum algorithm finds in 1 call !

For searching 1 object out of N: \sqrt{N} steps
 \sqrt{N} gain/ classical search algorithm

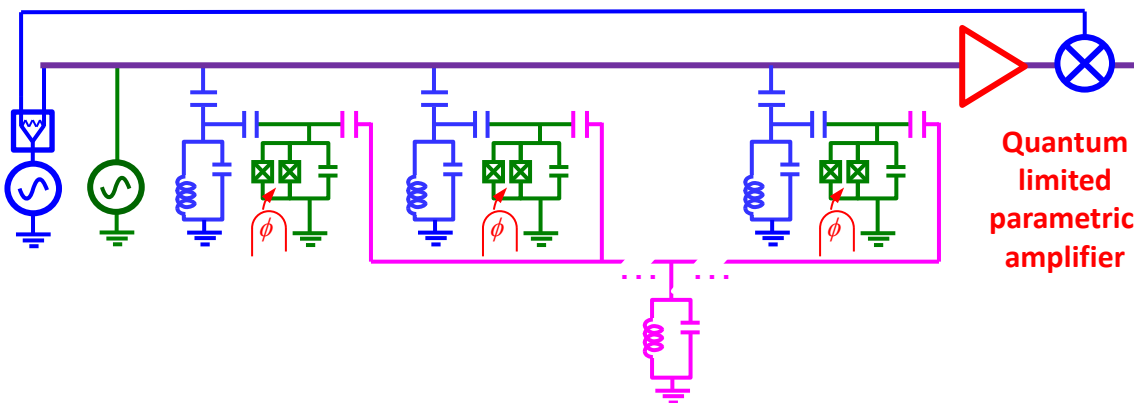
The Grover search algorithm



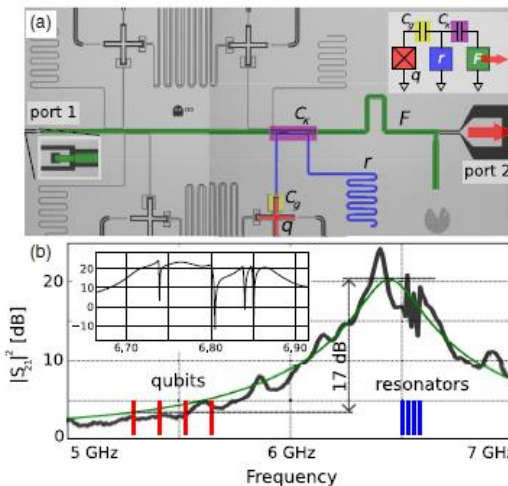
Single run success rate $> 1/4$ demonstrates Quantum Speedup

The readout scalability issue in circuit QED

Linear dispersive readout

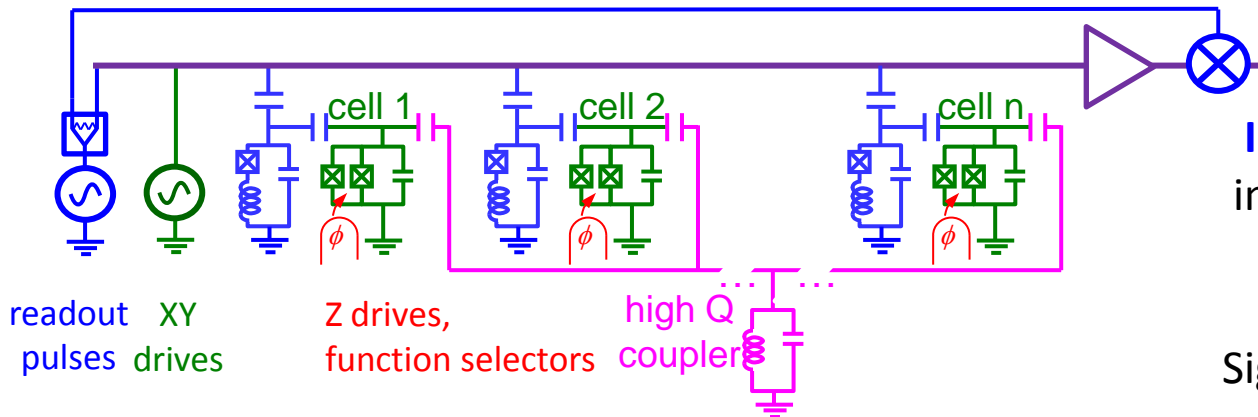


Issues: limited bandwidth, low saturation power
many groups at work



E. Jeffrey et al.
PRL **112**, 190504 (2014)

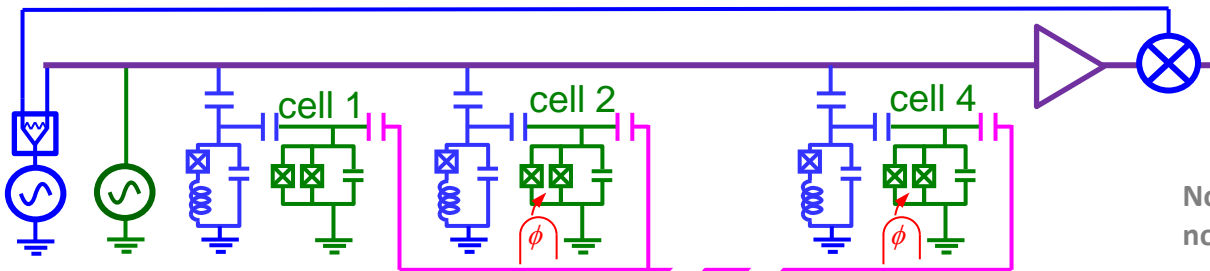
A N+1 architecture based on multiplexed JBA-readout



Issues:
interactions btw non-linear readout resonators

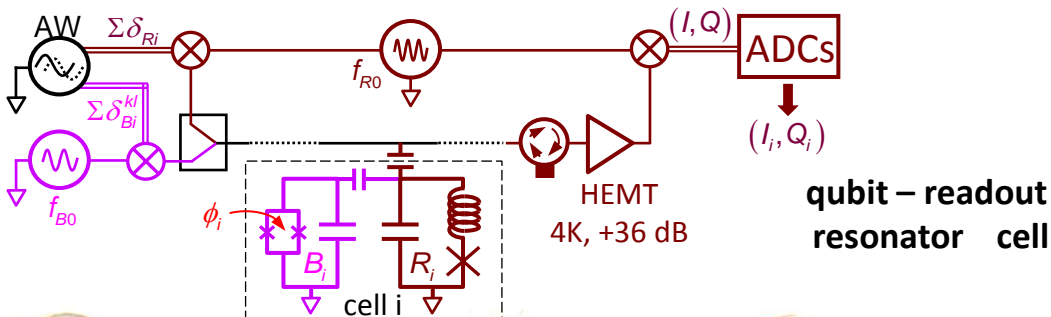
Signal processing

Demonstrating multiplexed JBA-readout

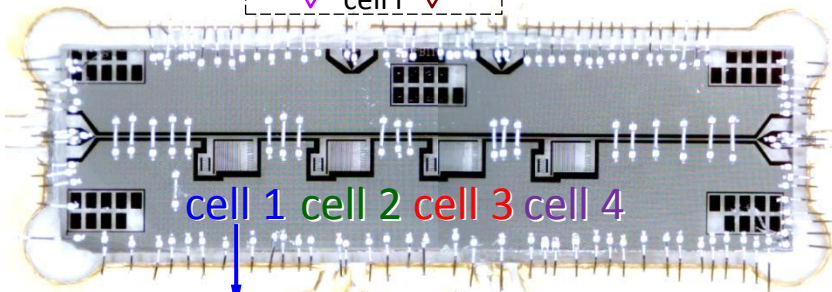


Note:
not a full processor !

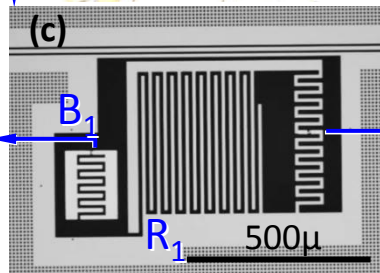
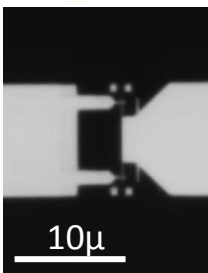
readout XY
pulses drives



qubit – readout
resonator cell



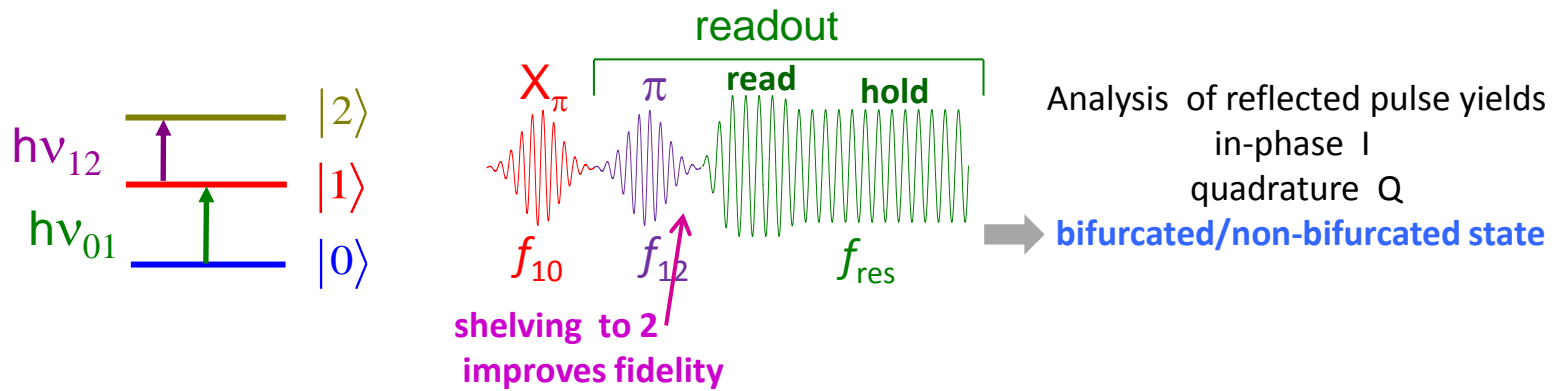
Flux tunable
junction



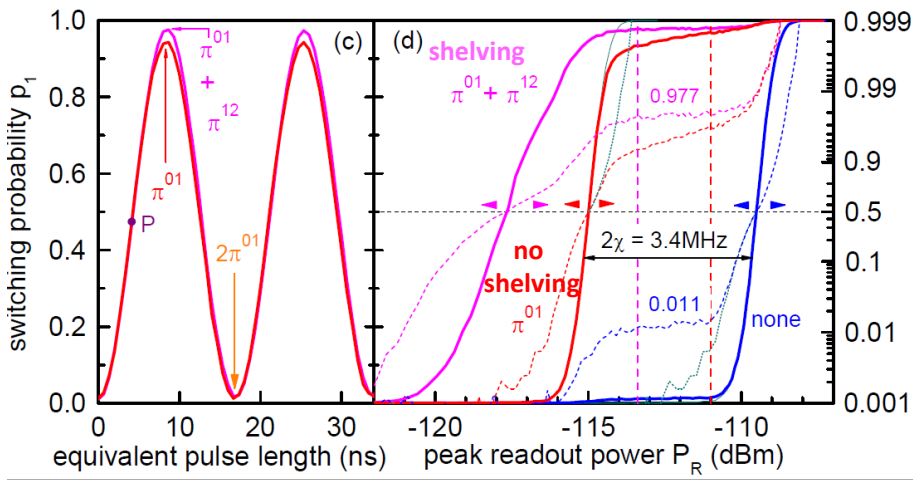
readout
resonator
junction



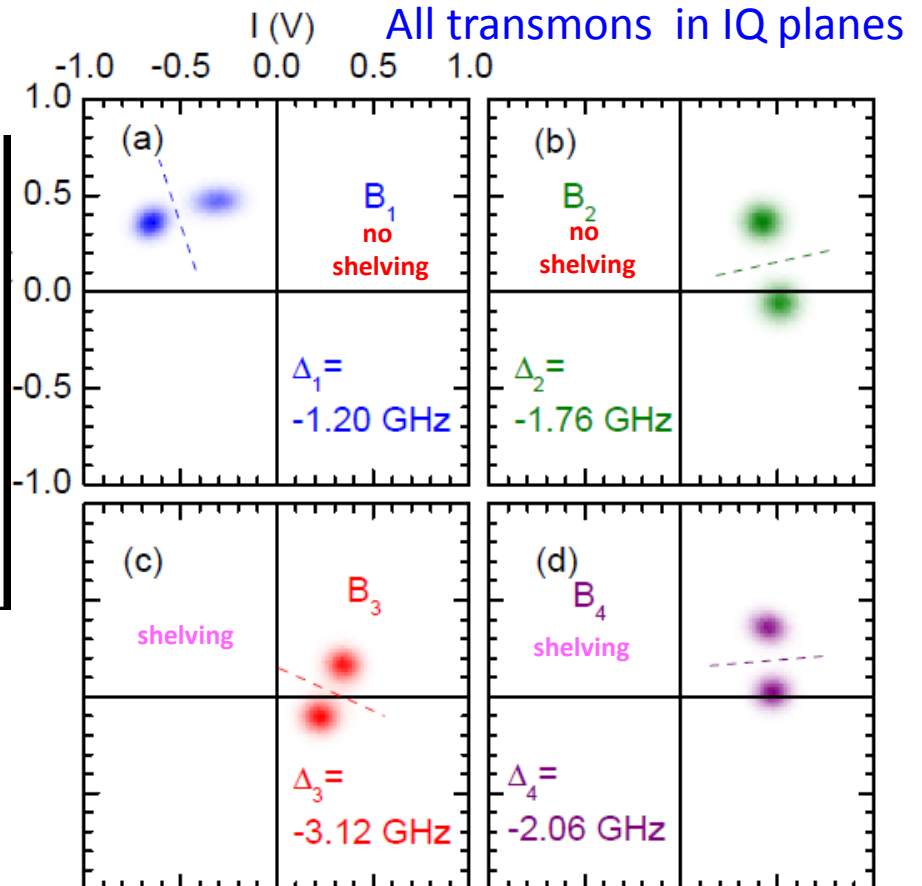
Individual qubit readout



single transmon readout performance

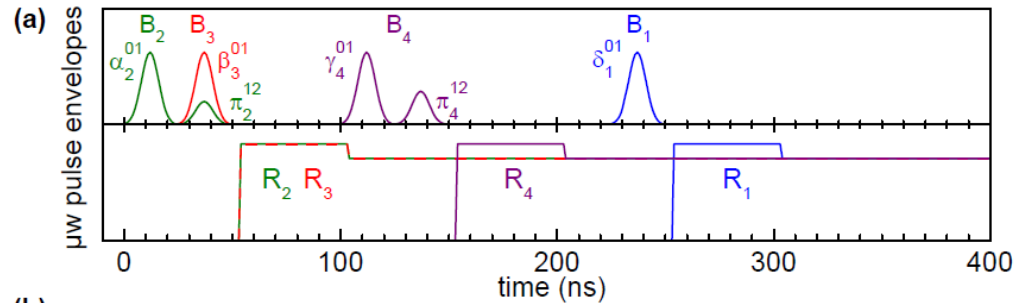


All transmons in IQ planes

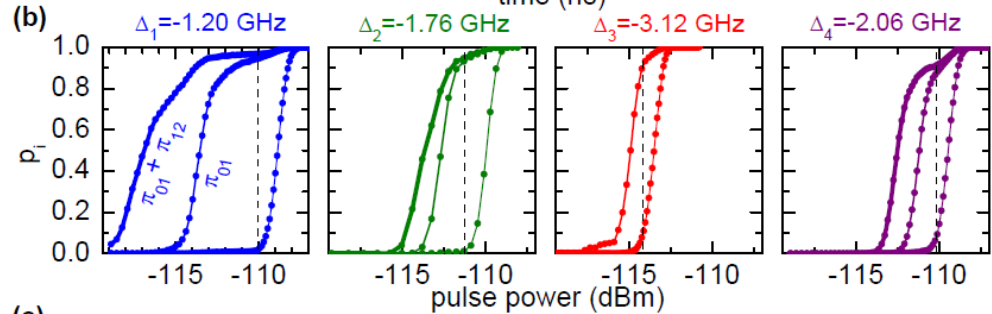


multiplexed qubit readout

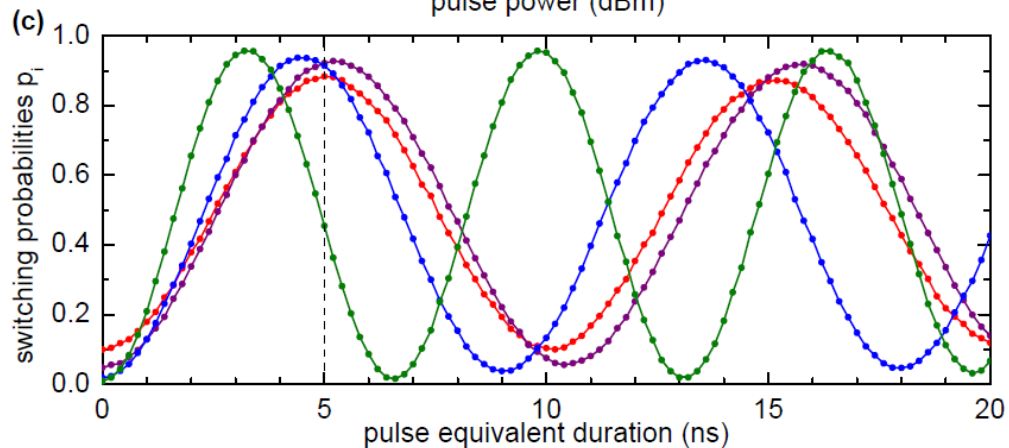
drive & readout timing



switching curves



simultaneous Rabi oscillations



Note: lack of local flux tuning lines prevents getting best readout performance simultaneously.

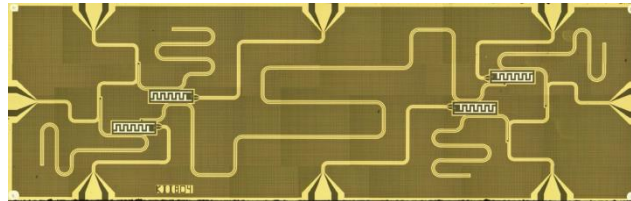
Scalability issues: quantum error correction

QC: > 100s of robust logical qubits needed

(1) Quantum error correction codes: demanding threshold for gate errors $< 10^{-4}$
huge resource overhead $\times 50$?

Measure syndroms for assigning errors without qubit projection

Di Carlo, TUD
parity measurements
for bit-flip detection
+ FPGA feedback



bit-flip correction
of a single qubit
within reach

(2) Surface codes: less demanding threshold for gate errors $< 10^{-2}$
extreme resource overhead $\times 10^3$ $\times 10^4$

(3) Other paradigms:

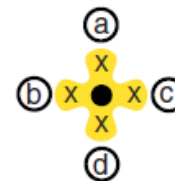
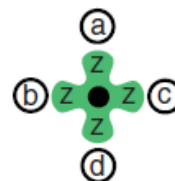
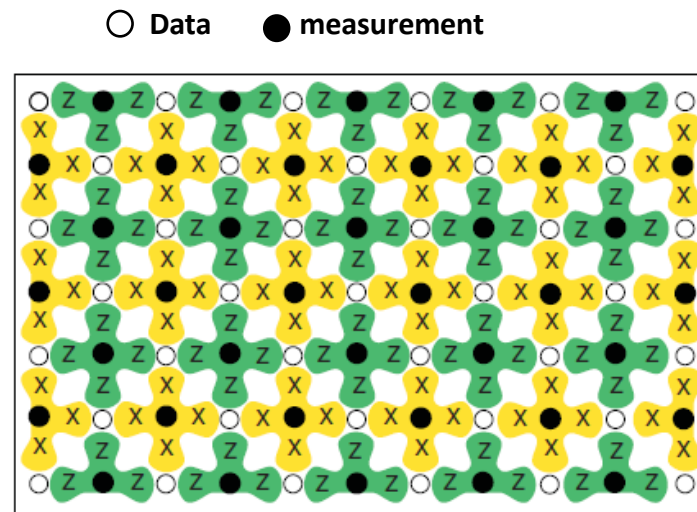
spins, Schrödinger cat states in high Q resonators, Adiabatic Quantum Computing

(2) The surface code

Kitaev, 2002, Preskill 2003,
Gottesman stabilizers

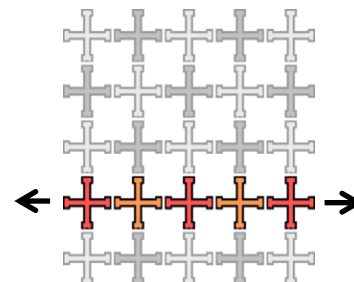
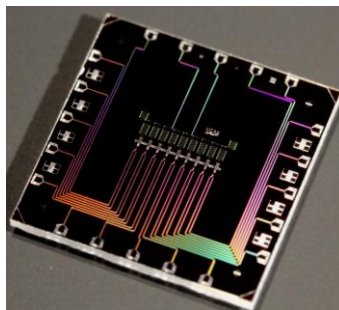
[Readable ref: Fowler et al., PRA 86, 032324 2012\)](#)

- 2D array of qubits (measure (x and Y types), data) with CNOT gates , Z measurements.
- nearest-neighbor coupling
- **Forgiving threshold** (~0.99)
- Error detection is enough, correction handled by classical post-processing
- **Extreme** resource overhead (*irrealistic ?*)



Preliminary 9 qubit test circuit

J. Martinis team
UCSB- Google



(3) Engineered dissipation for robust logical qubits with simple errors that can be detected and corrected

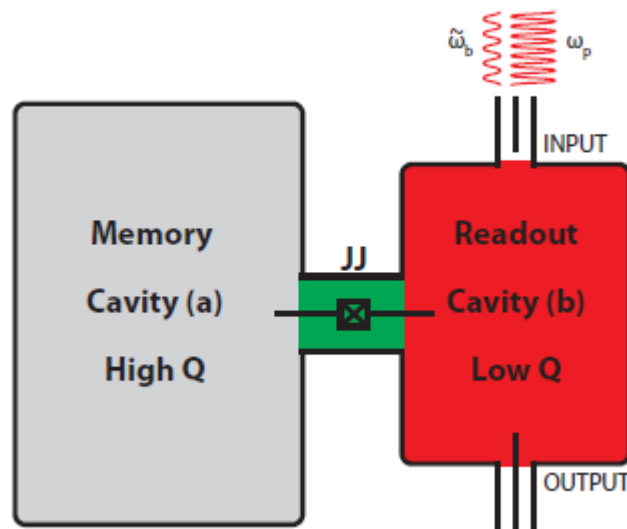
See:

Dynamically protected cat-qubits:
a new paradigm for universal quantum computation

Mirrahimi, Leghtas, Albert, Touzard, Schoelkopf, Liang, Devoret

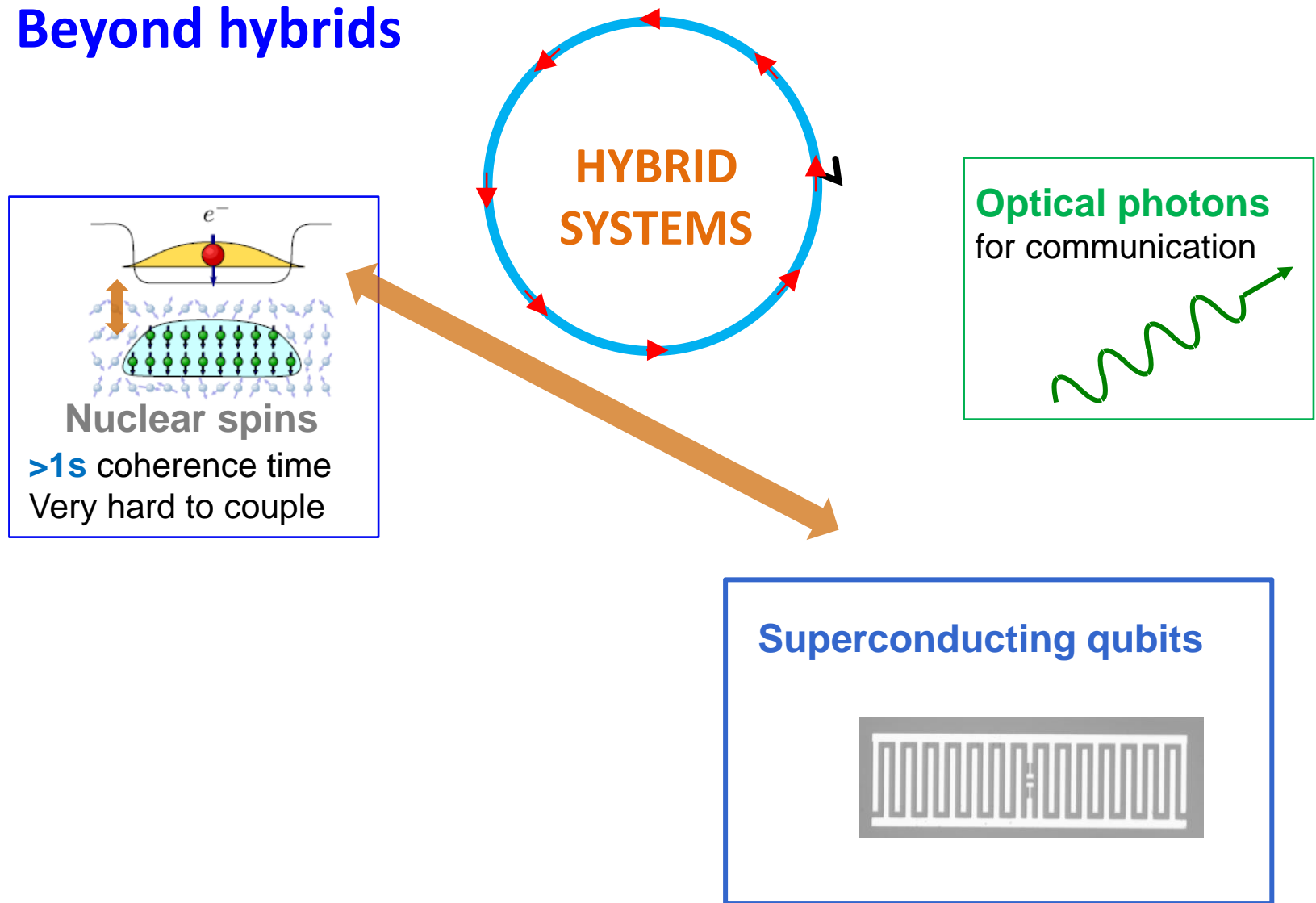
NEW JOURNAL OF PHYSICS 16 045014 (2014) arXiv:1312.201

Pumping + non-linear element yield 2photon dissipation for memory



Cat states built with coherent states are robust
Parity measurements detect errors.
Gates based on Zeno effect

(3) Beyond hybrids



See:

- Kubo et al., PRL 107, 220501, 2011
- Grèzes et al., PRX 2, 021049, 2014
- Julsgaard et al., PRL 110, 250503 2012

The Dwave strategy & machine (10 M\$)

The New York Times

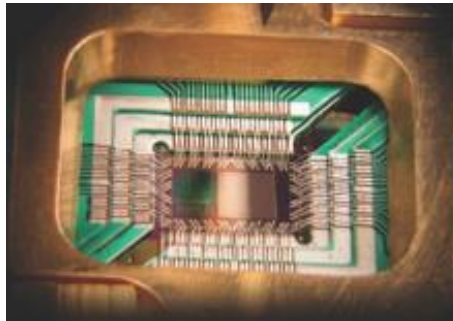
March 22 2013

A Strange Computer Promises Great Speed



Kim Stallknecht for The New York Times

512 qubits



??

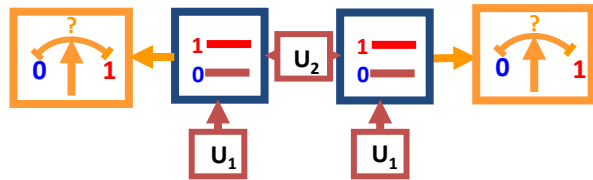
Adiabatic Quantum computing (?)

An annealing machine assisted by quantum effects ??

QC with gates versus Adiabatic Quantum Computation

The QC way:

unitary evolution of a qubit register
(according to algorithm) & readouts



Difficulties:

- unitary evolution
- quantum error correction
- readout
- scalability

overcoming standard computers:

N=50-100 robust qubits
(i.e. corrected from errors)

State of the art:

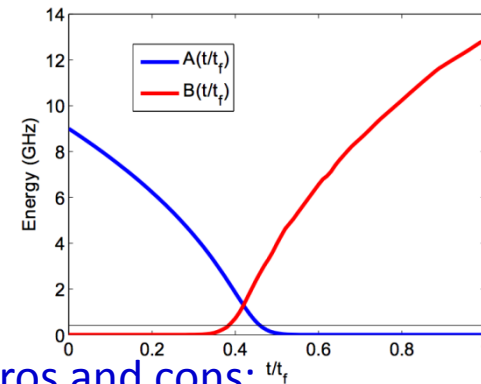
N=2-4, errors, no QEC
N=10 in view, without QEC

Proof of principle for quantum speedup on elementary problem

(3) The AQC way:

finding the ground state of a Ising spin Hamiltonian $H^z(t)$
(that encodes the problem) starting from a trivial one
following an adiabatic evolution

$$H(t) = B(t)H^z(t) - A(t)\sum\sigma_i^x$$



Pros and cons:

- Evolution is simple
- Problem encoding not easy, good for optimization
- role of decoherence and temperature not understood

overcoming standard computers:

N=4000-8000 qubits

State of the art (Dwave machine):

N=500, operational, not perfect, N=2000 in view

Ising spin-glass problem solved on 100 spins but quantum speedup not demonstrated

Ronnow, ..., Troyer Science 334, 420 (2014)

**QIP :**

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