

Device-independent protocols from computational assumptions

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Joint work with



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(UC Berkeley)



Yfke Dulek
(CWI & QuSoft)



Thomas Vidick
(Caltech)

Self-testing of a single quantum device under computational assumptions, arXiv:2001.09161.

Device-independent quantum key distribution from computational assumptions, arXiv:2010.04175.

Outline


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1. Setting for “standard” DIQKD



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1. Setting for "standard" DIQKD  *security based on Bell inequality violation*



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2. Setting for "computational" DIQKD




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3. Main technical tool: computational self-testing

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1. Setting for "standard" DIQKD  *security based on Bell inequality violation*
2. Setting for "computational" DIQKD  *can't base security on Bell inequality violation*
3. Main technical tool: computational self-testing  *replaces Bell inequality violation*

Device-independent QKD

Ekert, Quantum cryptography based on Bell's theorem, PRL 67, 661 (1991).
Mayers & Yao, Quantum cryptography with imperfect apparatus, FOCS 1998.

Device-independent QKD

Eve

Alice

Bob

Device-independent QKD

Eve

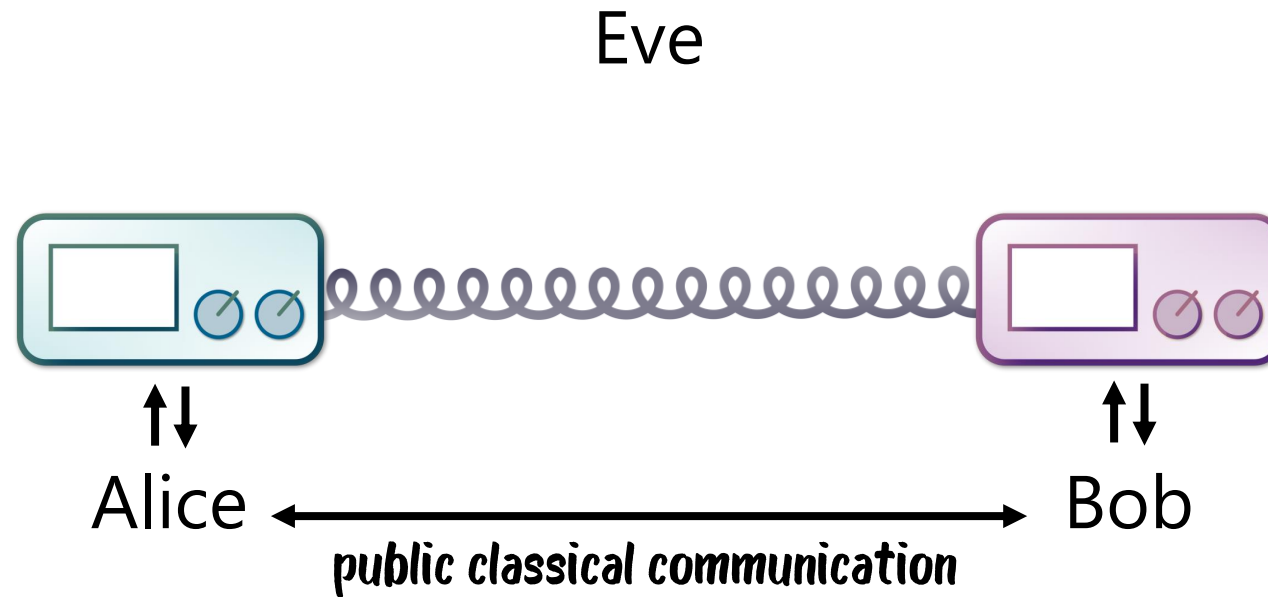


Device-independent QKD

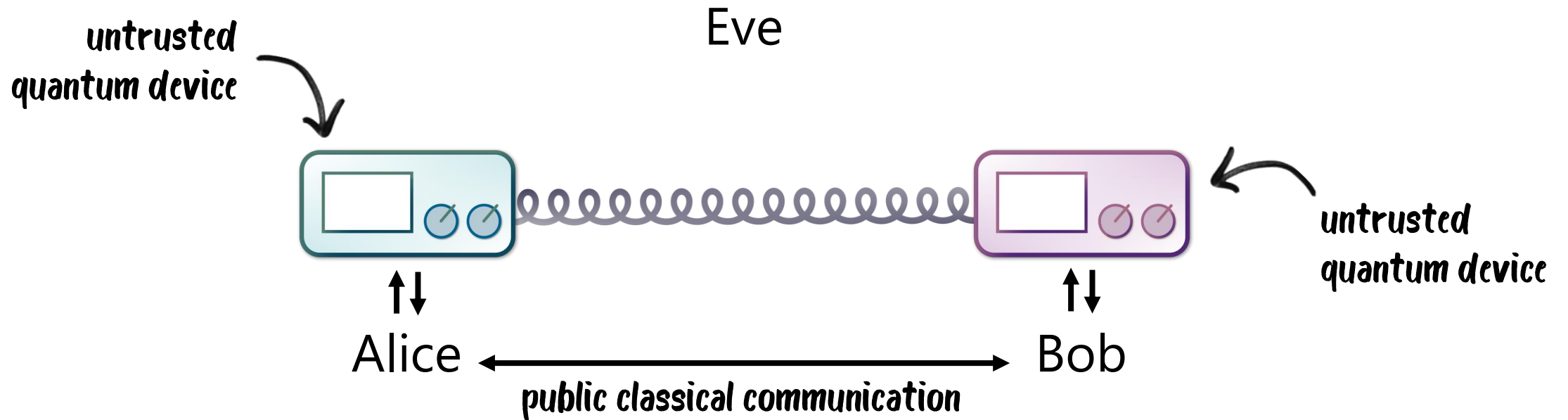
Eve



Device-independent QKD



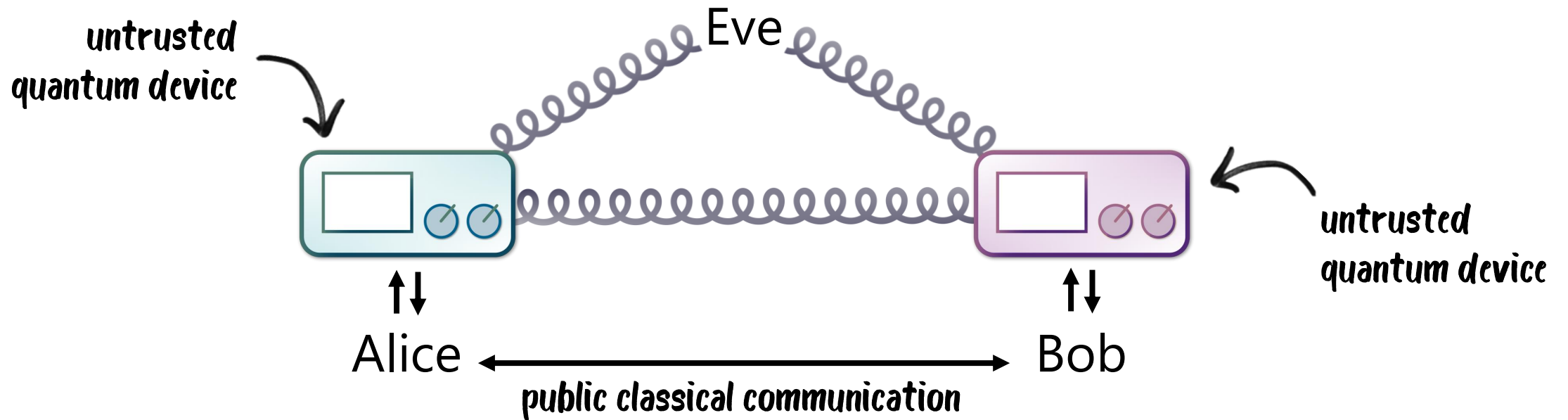
Device-independent QKD



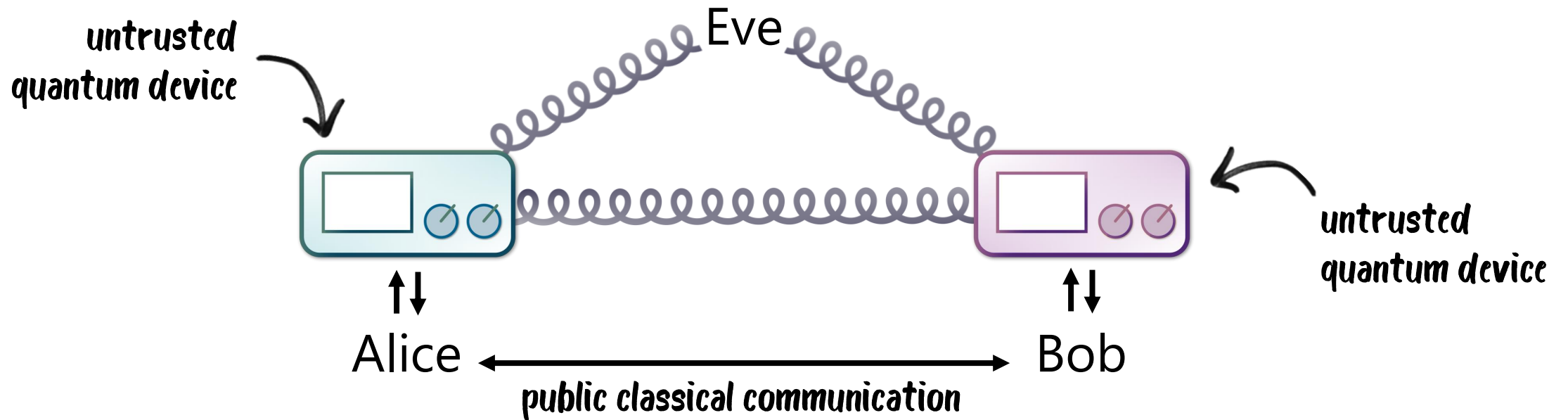
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Device-independent QKD

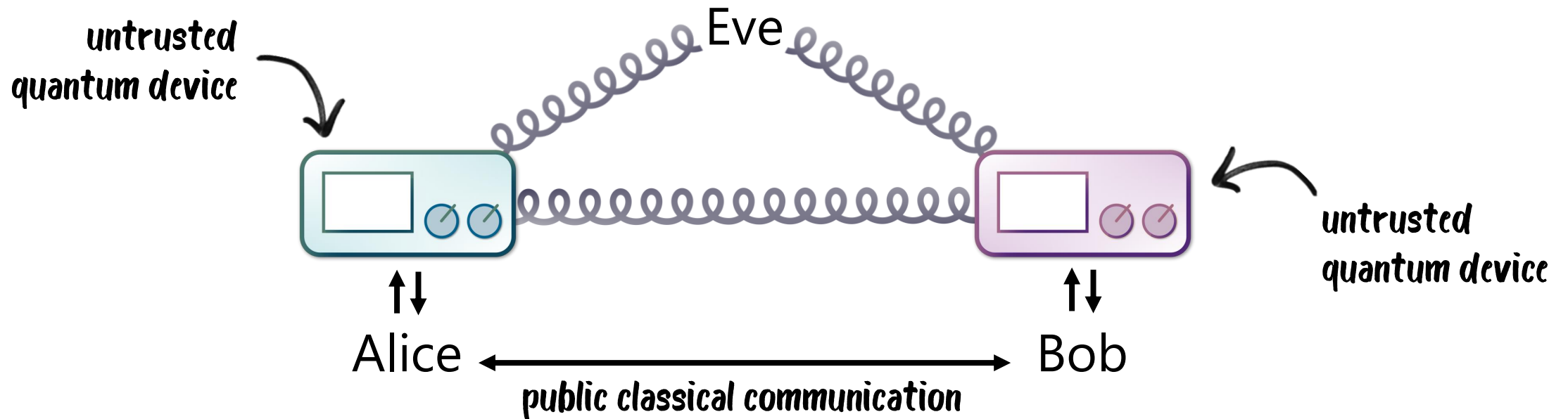


Device-independent QKD



Bell inequality
violation

Device-independent QKD

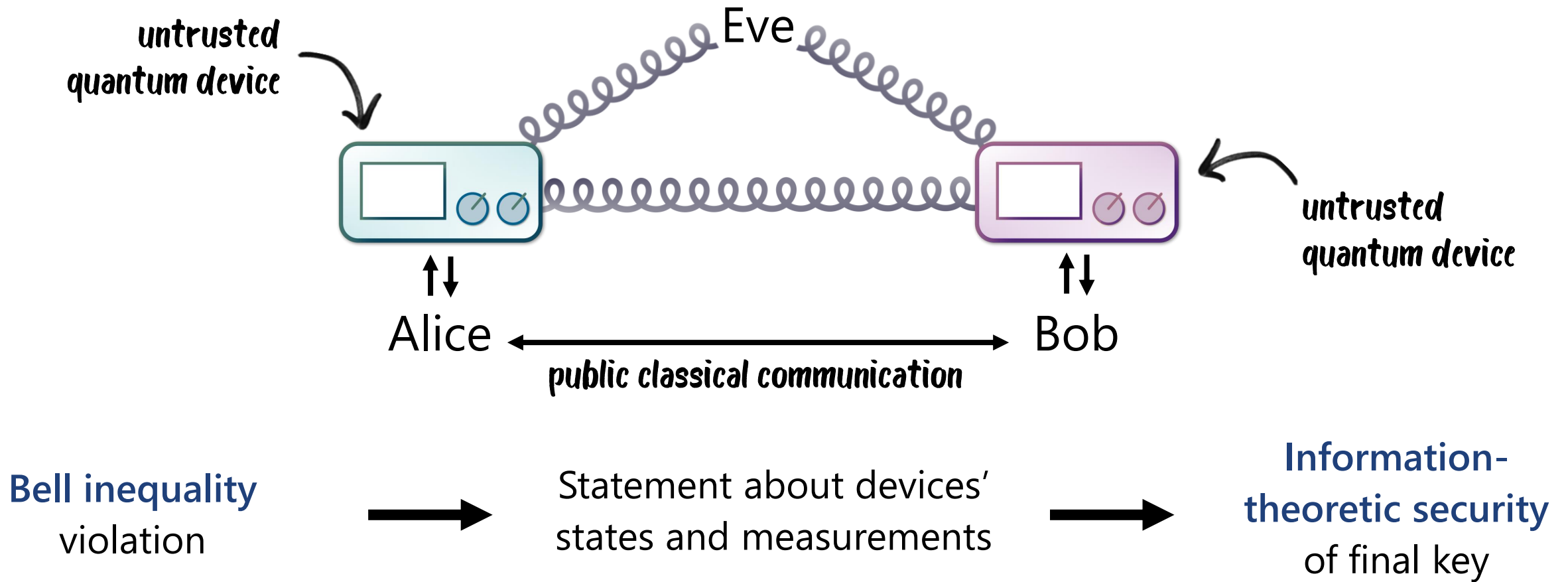


Bell inequality violation

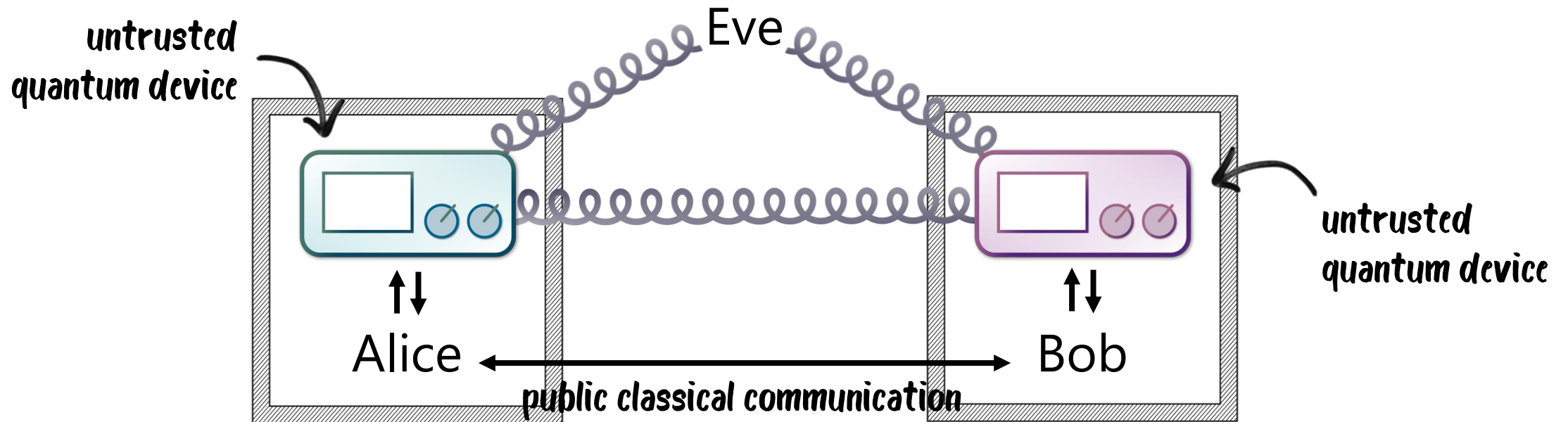


Statement about devices' states and measurements

Device-independent QKD



Device-independent QKD



Bell inequality violation

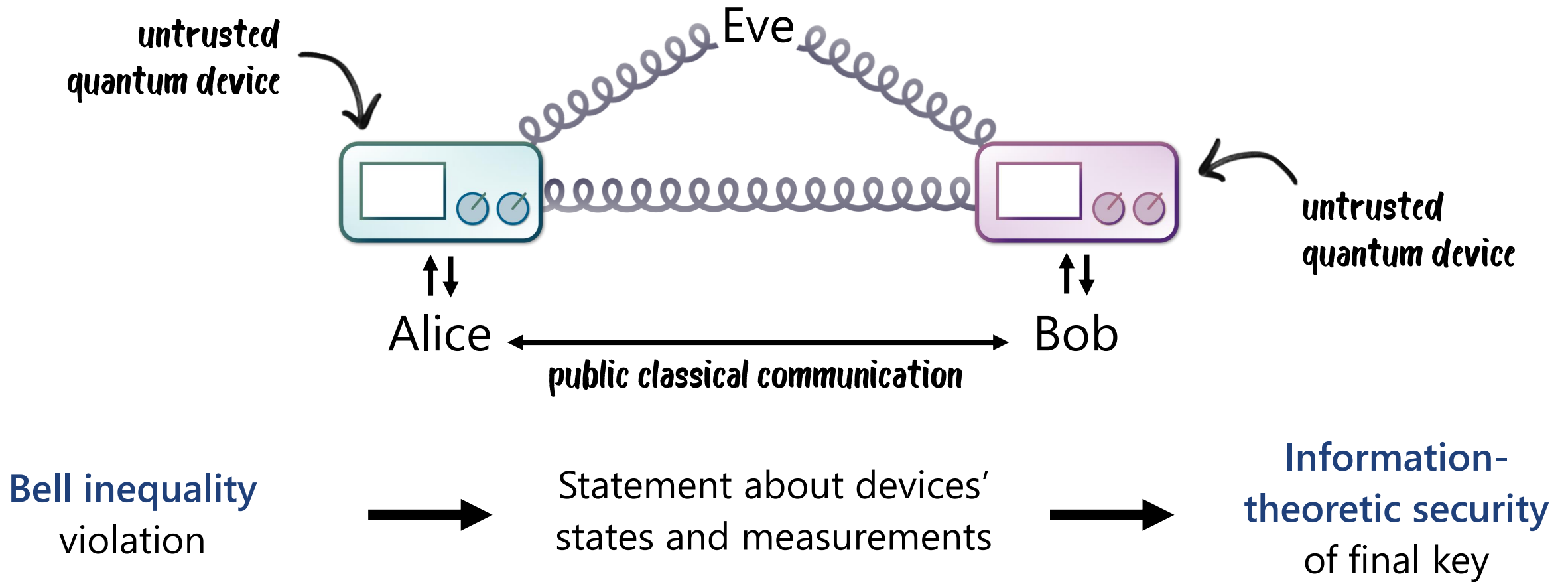


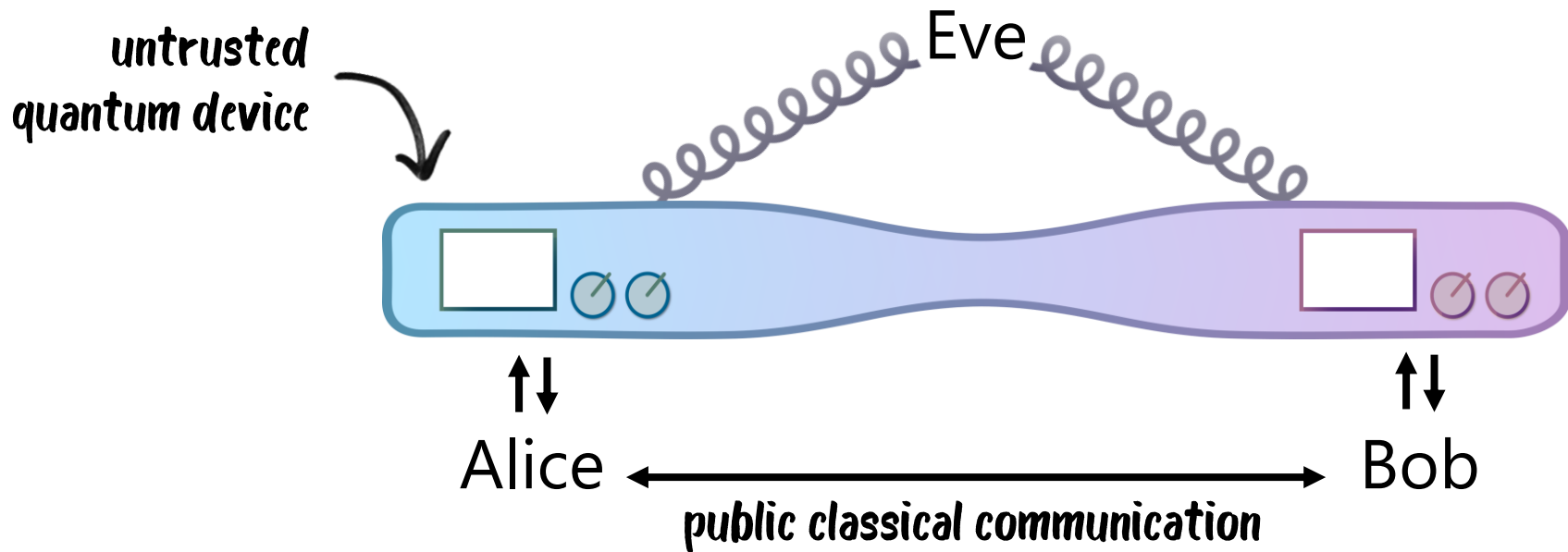
Statement about devices' states and measurements



Information-theoretic security of final key

Device-independent QKD





Bell inequality violation

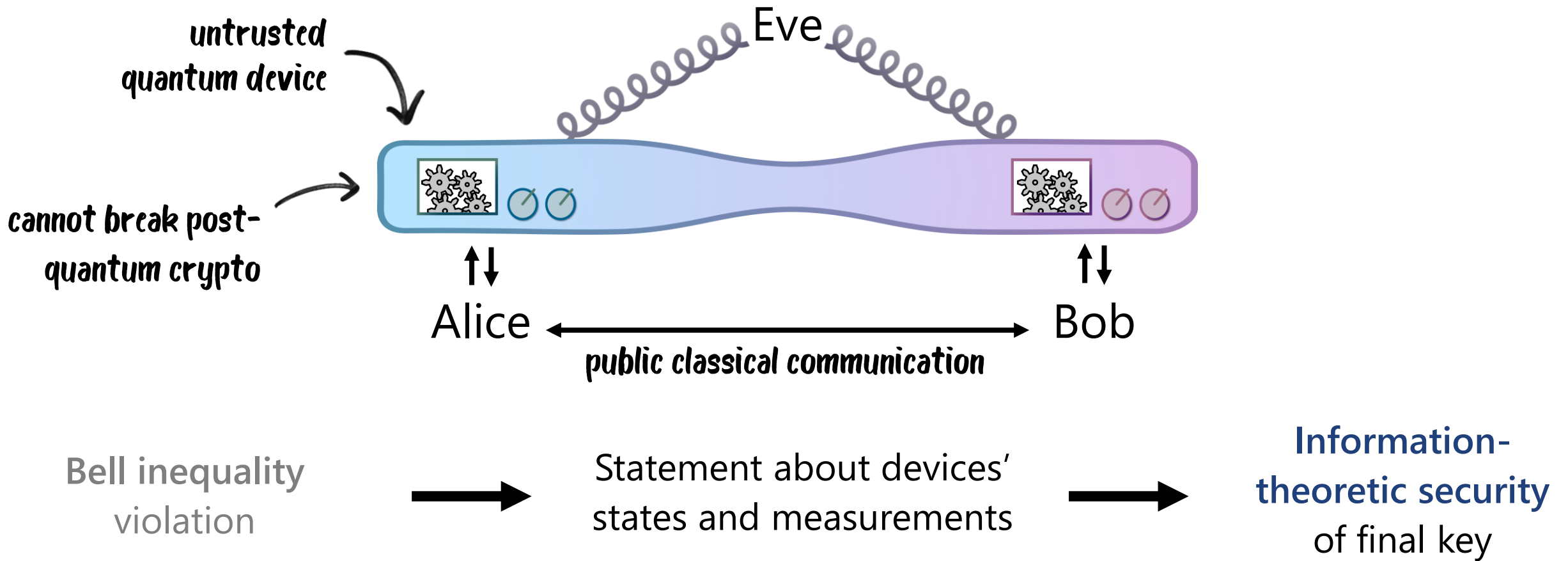


Statement about devices' states and measurements



Information-theoretic security of final key

Computational DIQKD setting

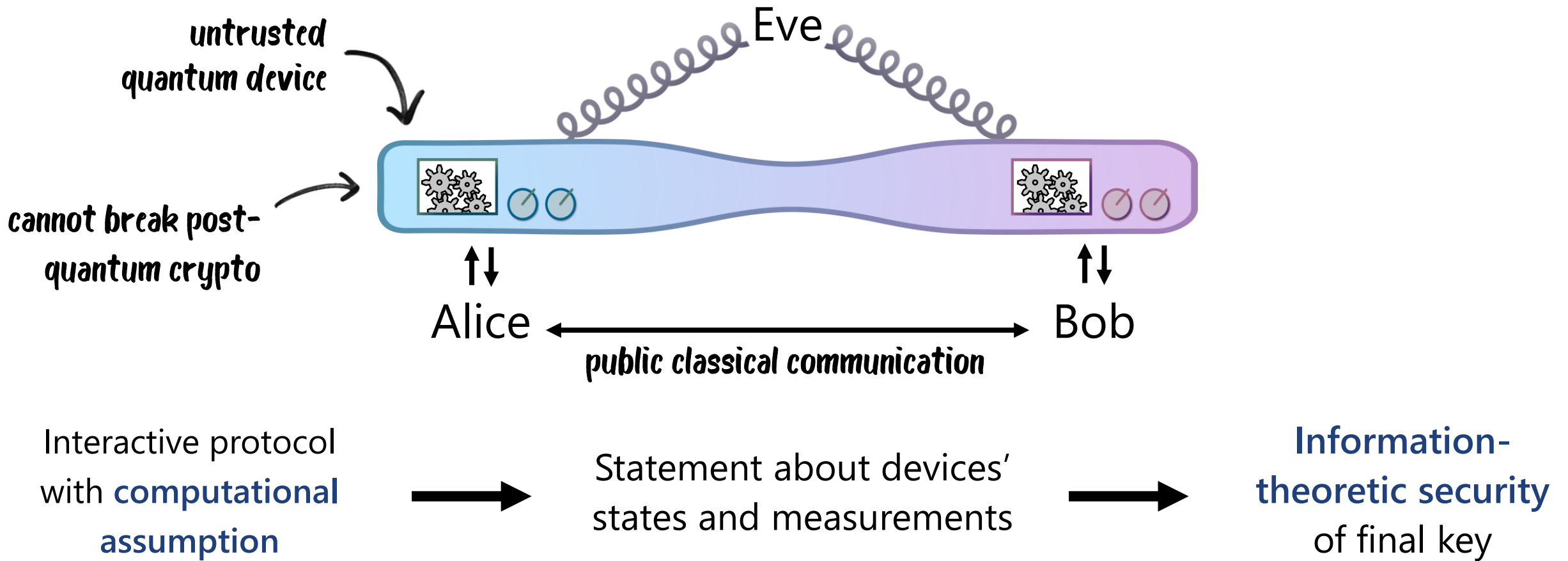


Brakerski et al., A cryptographic test of quantumness and certifiable randomness from a single quantum device, FOCS 2018.

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Computational DIQKD setting

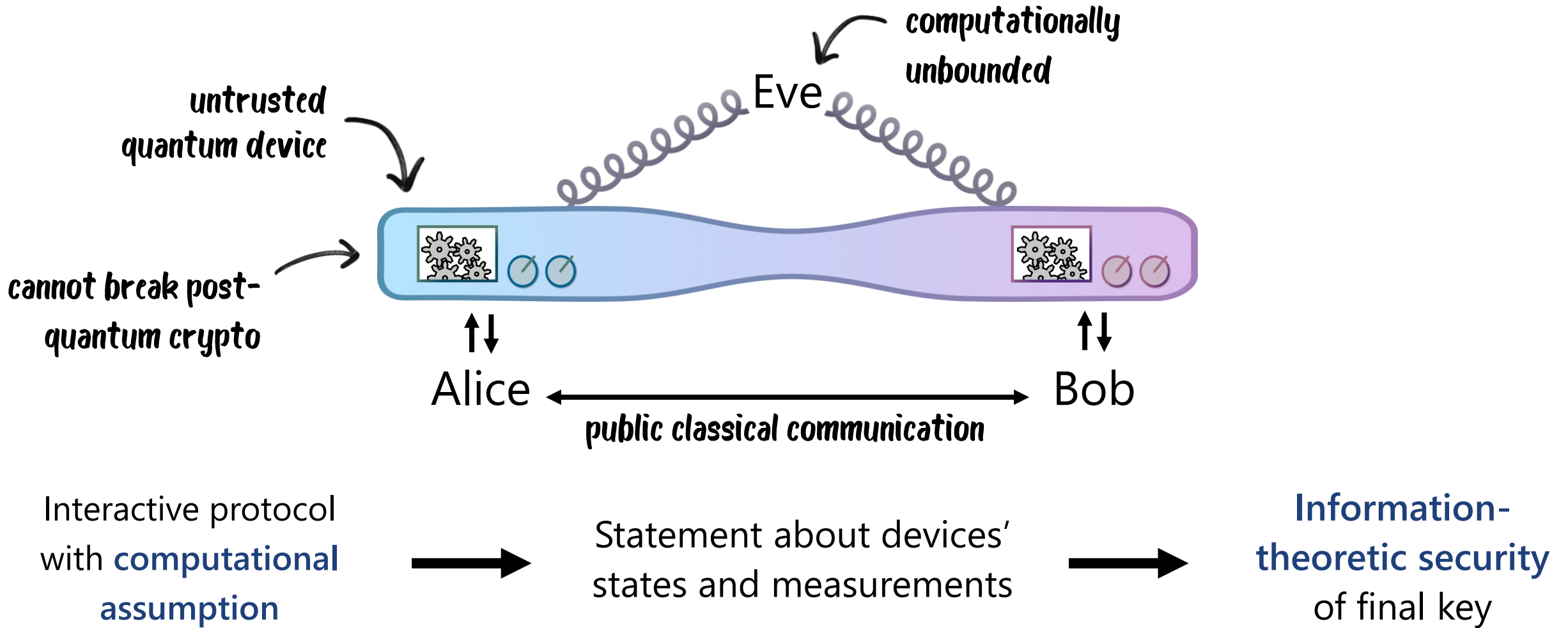


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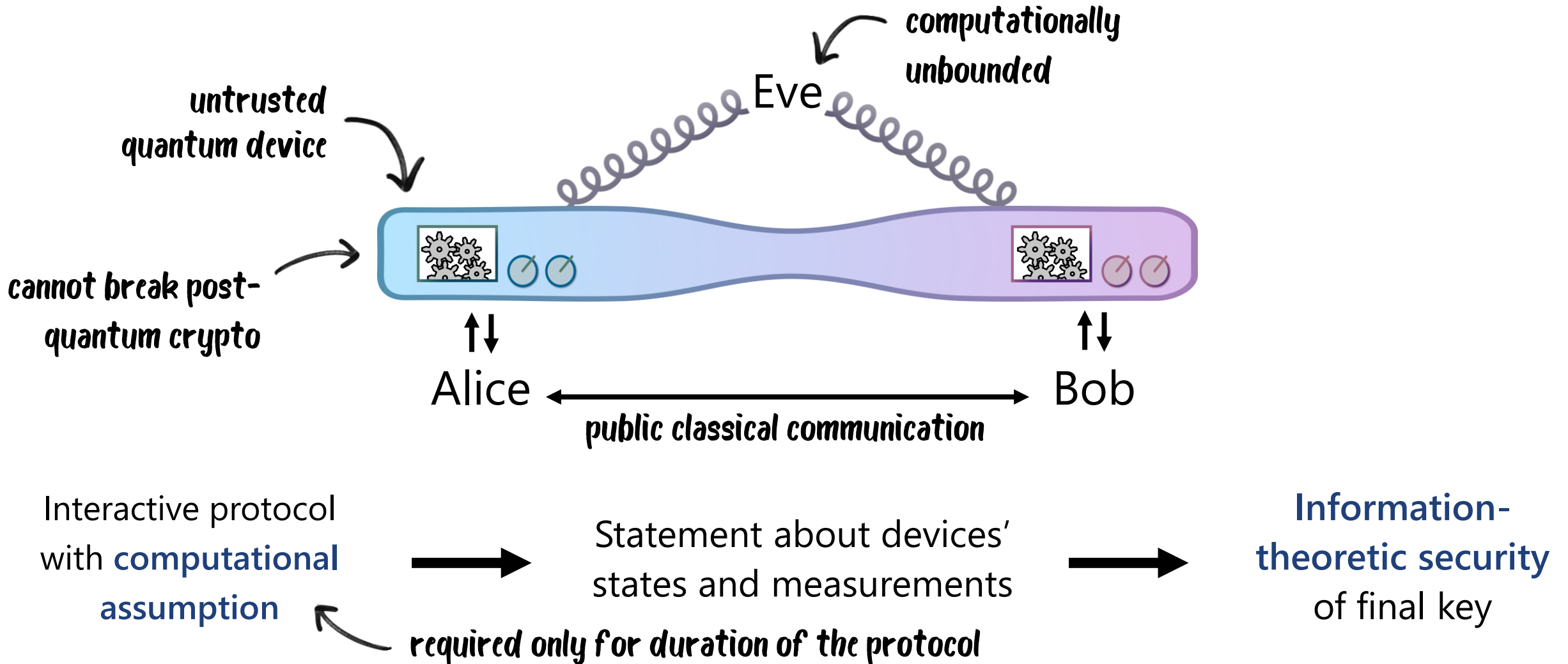


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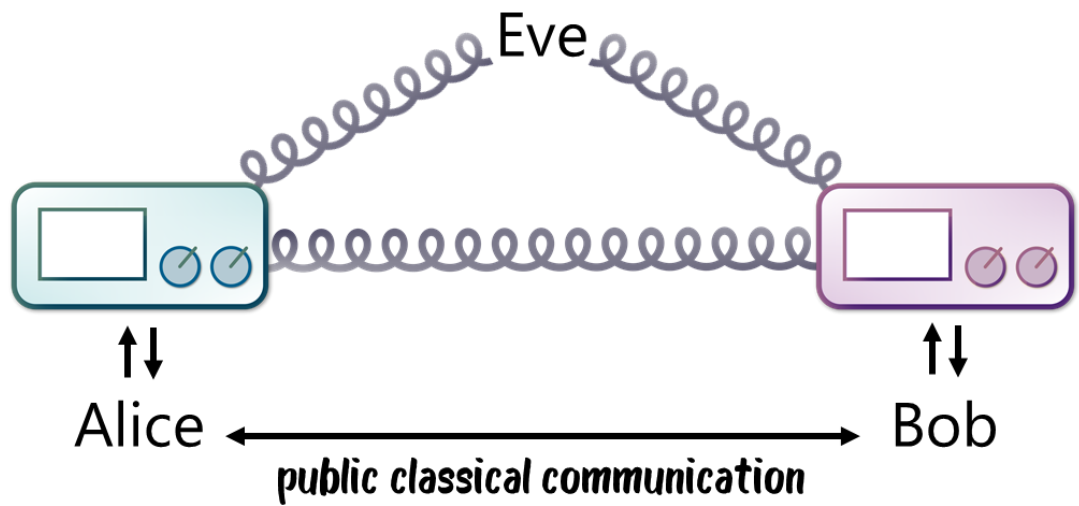
Computational DIQKD setting

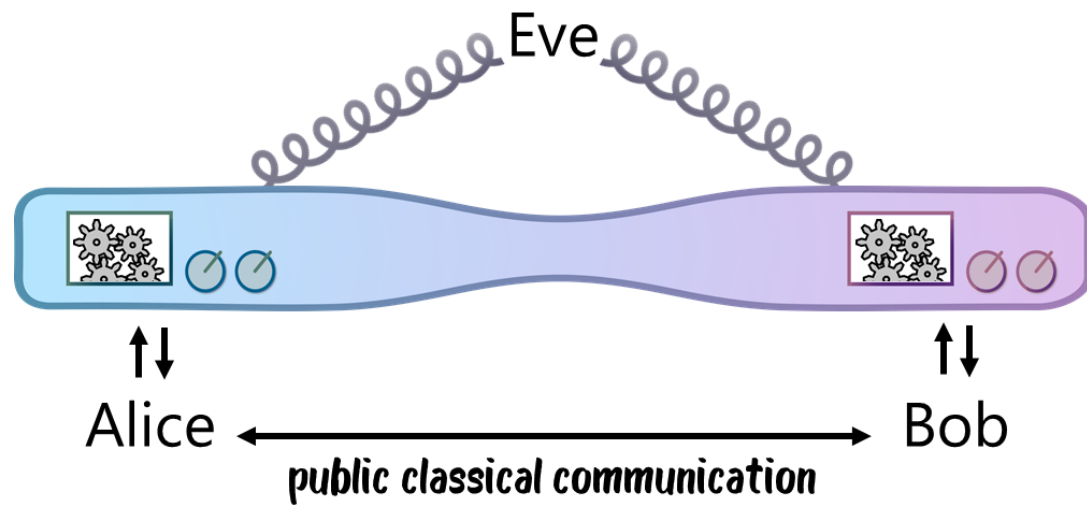
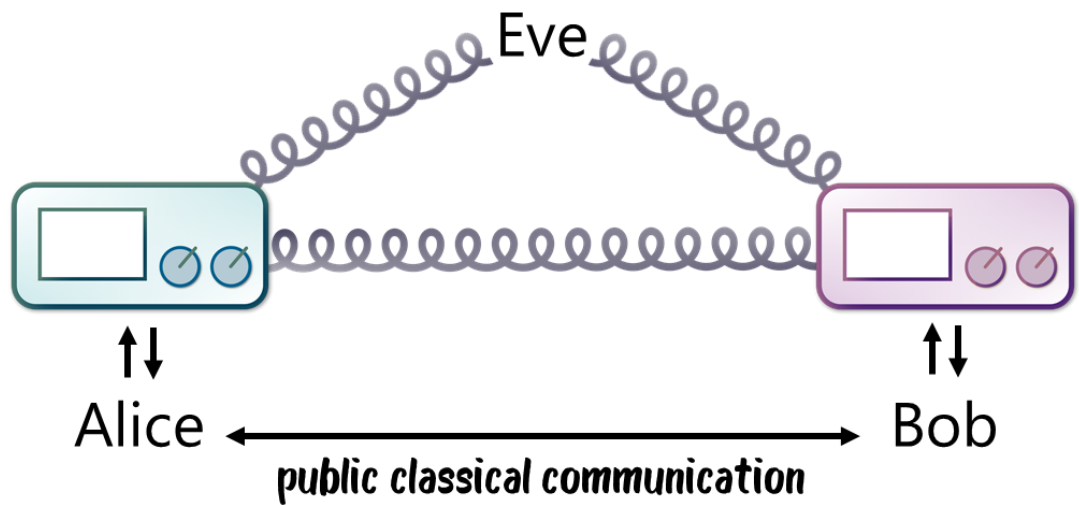


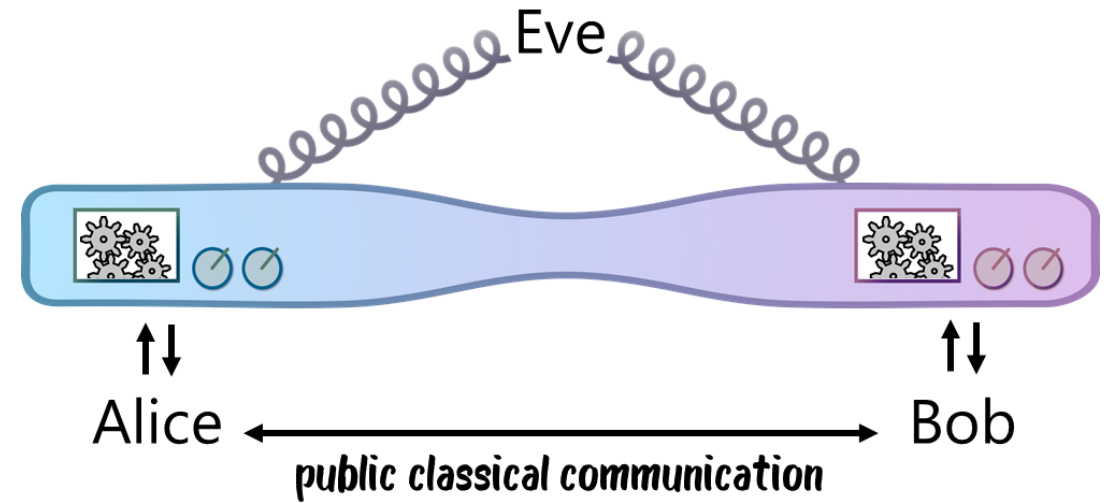
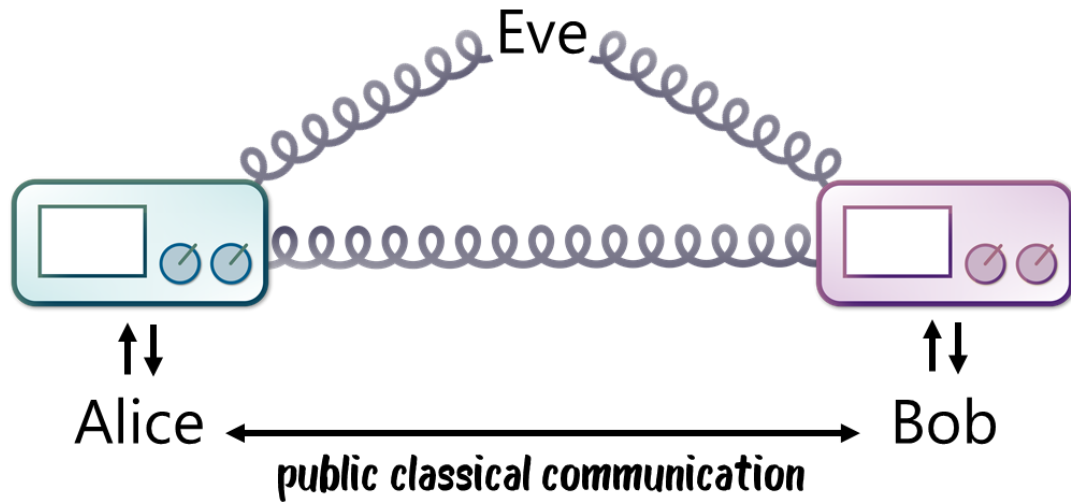
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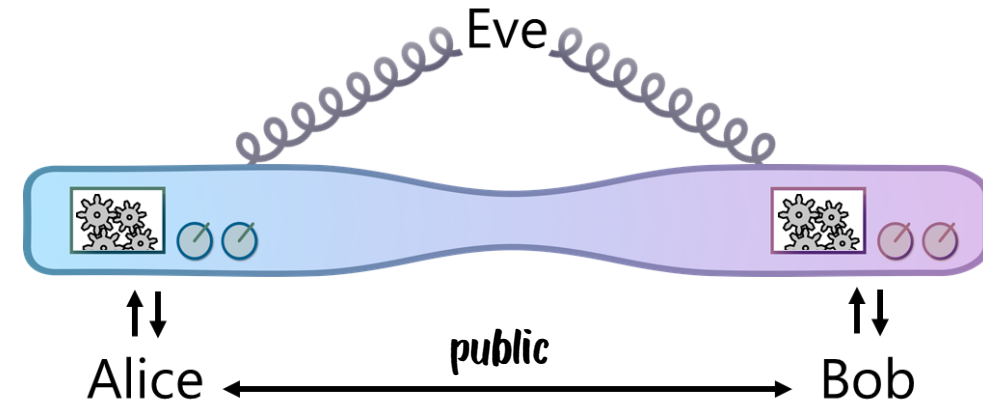
Extra requirement: **honest** devices should be able to succeed in the protocol with pre-shared EPR pairs and local operations

Computational self-testing protocol

Computational self-testing

Classical **interactive protocol** run by
Alice and Bob

Device can win or lose

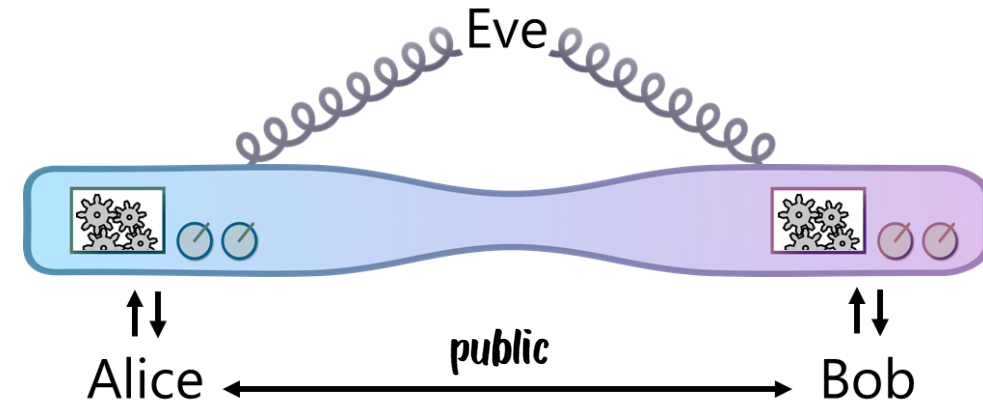


Computational self-testing

Classical **interactive protocol** run by Alice and Bob

Device can win or lose

If a **computationally bounded device** wins with probability (close to) 1:



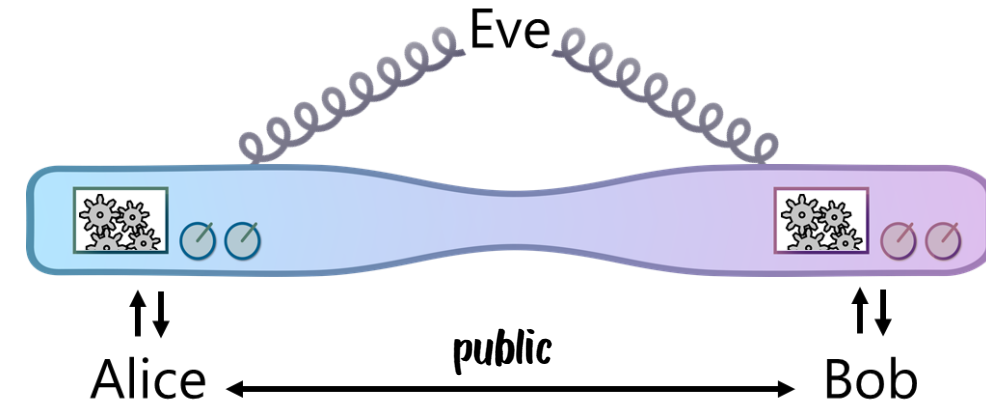
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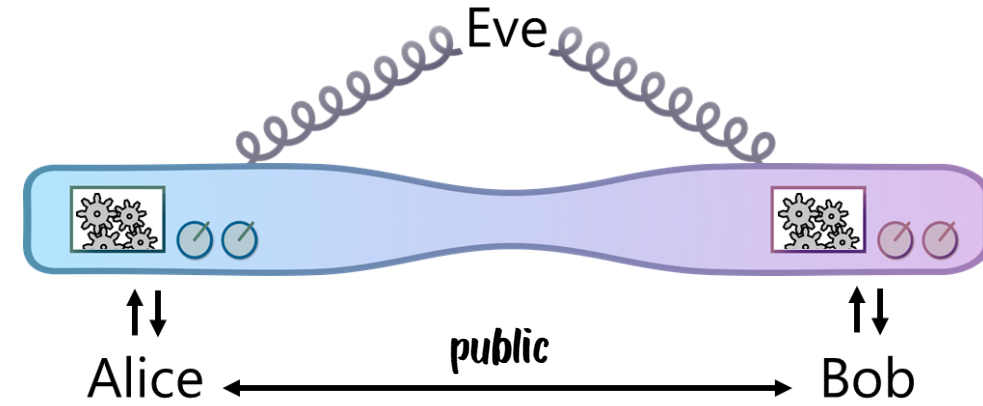
- the **state** prepared by the device must have been an EPR pair



Computational self-testing

Classical **interactive protocol** run by Alice and Bob

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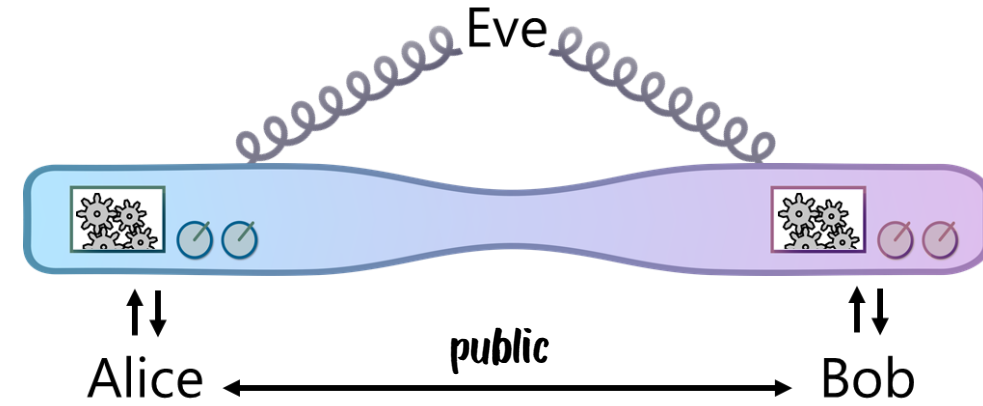
If a **computationally bounded device** wins with probability (close to) 1:

- the **state** prepared by the device must have been an EPR pair
- the device must have **measured** each qubit in the bases requested by Alice and Bob, respectively

Computational self-testing

Classical **interactive protocol** run by Alice and Bob

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If a **computationally bounded device** wins with probability (close to) 1:

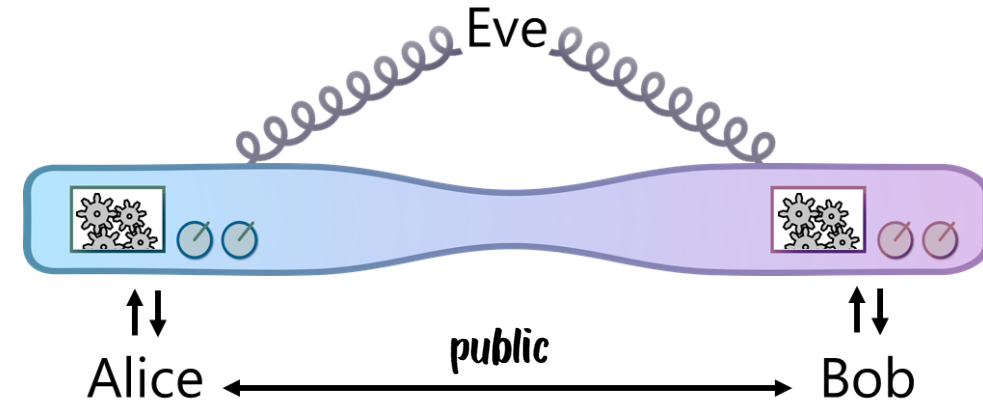
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up to **global** changes of basis.

Computational self-testing

Classical **interactive protocol** run by Alice and Bob

Device can win or lose

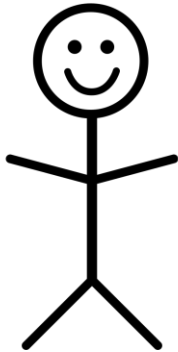
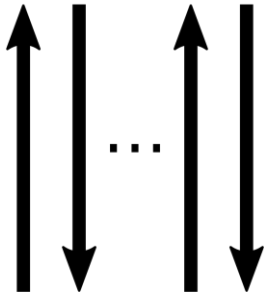
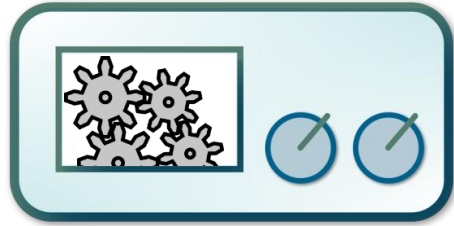


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Previous work



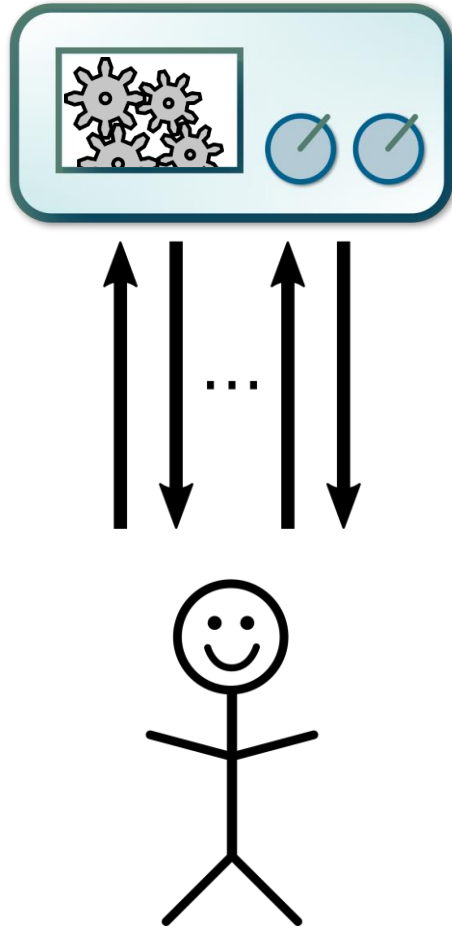
- Certifiable information-theoretic randomness expansion (Brakerski et al. 2018)

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Previous work



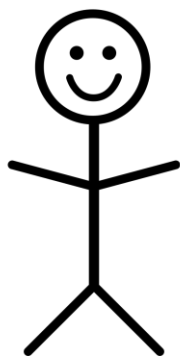
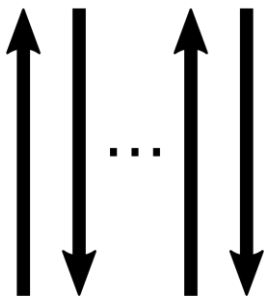
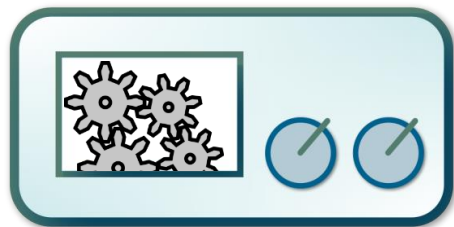
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- **Remote state preparation** (Gheorghiu, Vidick 2019)

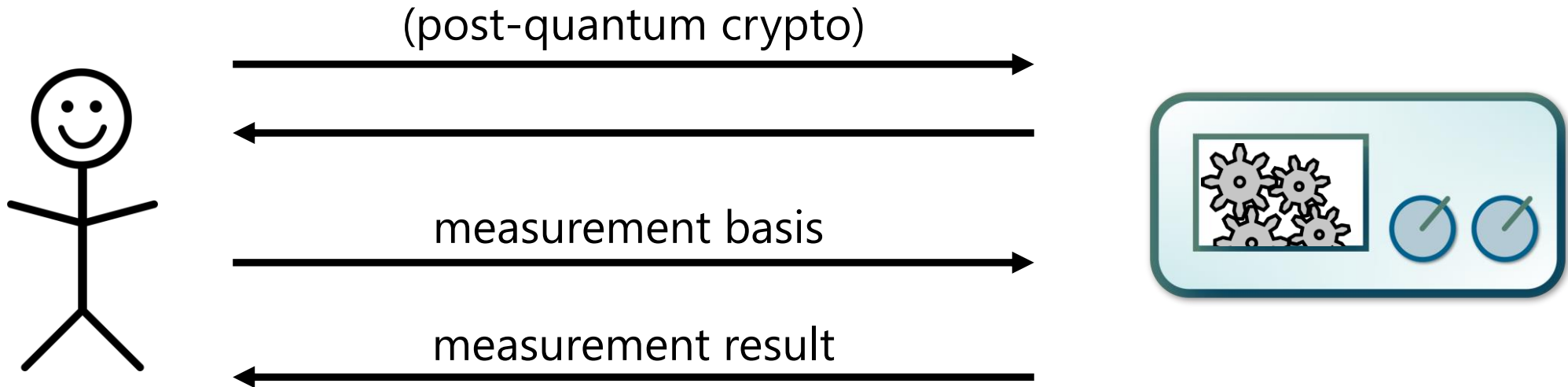
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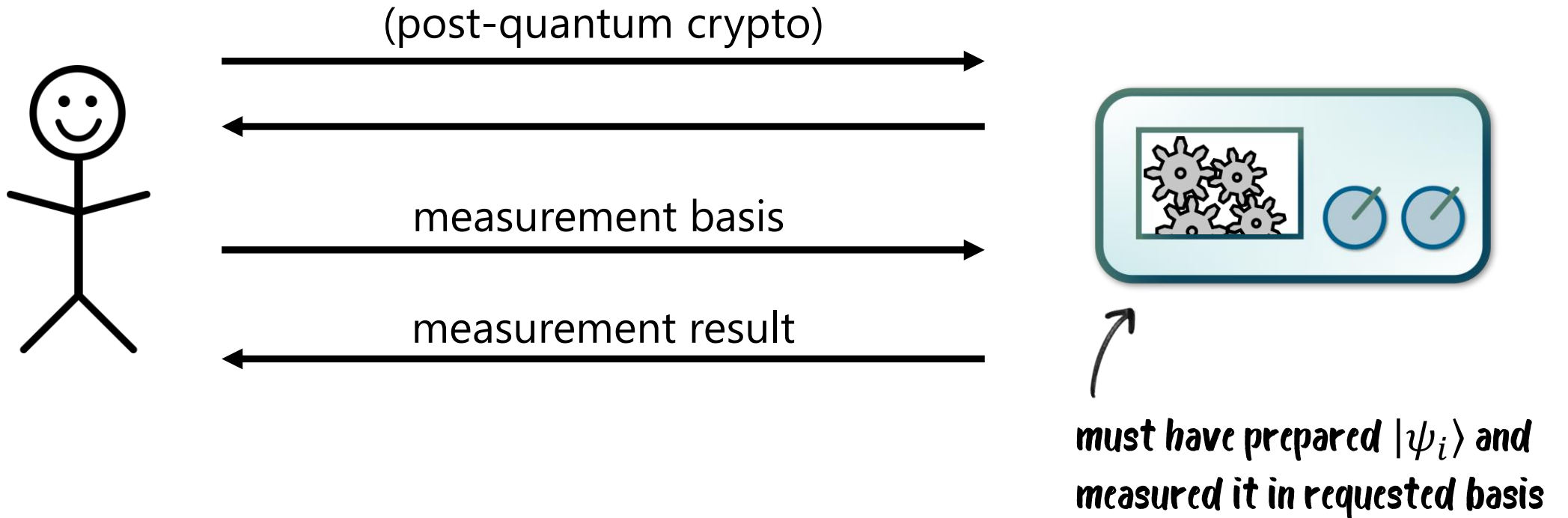
Remote state preparation [GV'19]

Given: set of **single-qubit** states $\{|\psi_i\rangle\} = \{|0\rangle, |1\rangle, |+\rangle, |-\rangle\}$



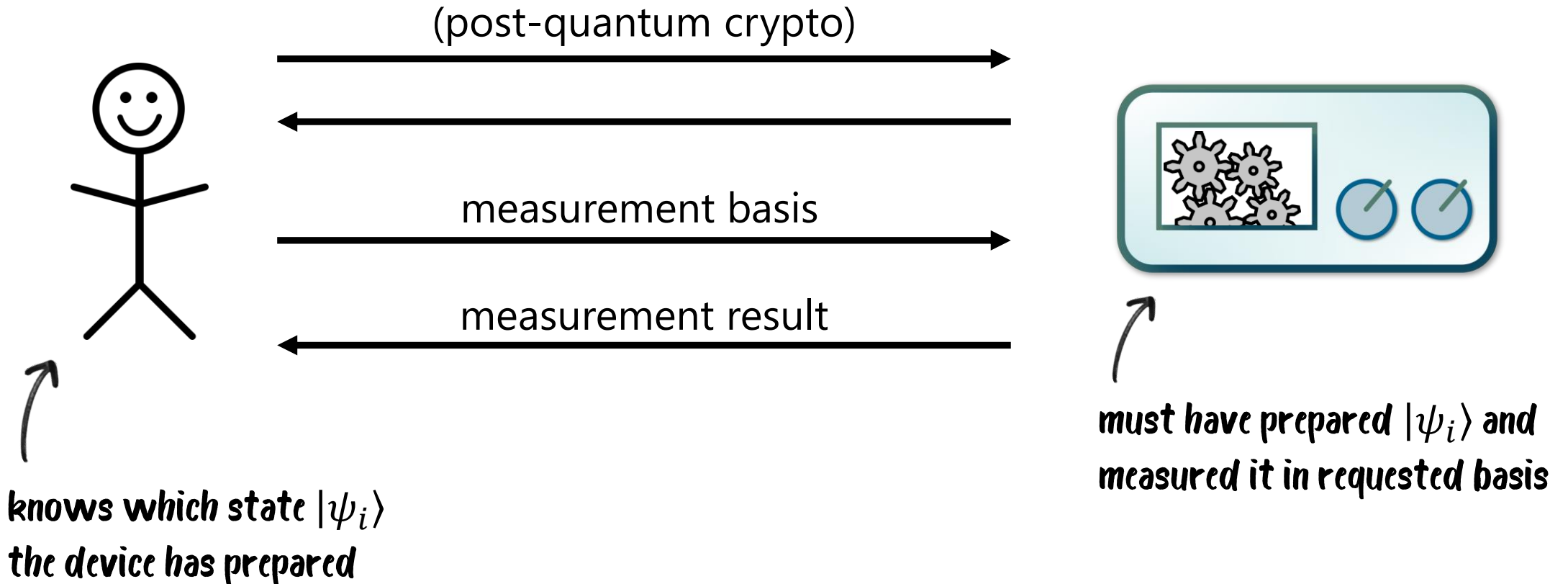
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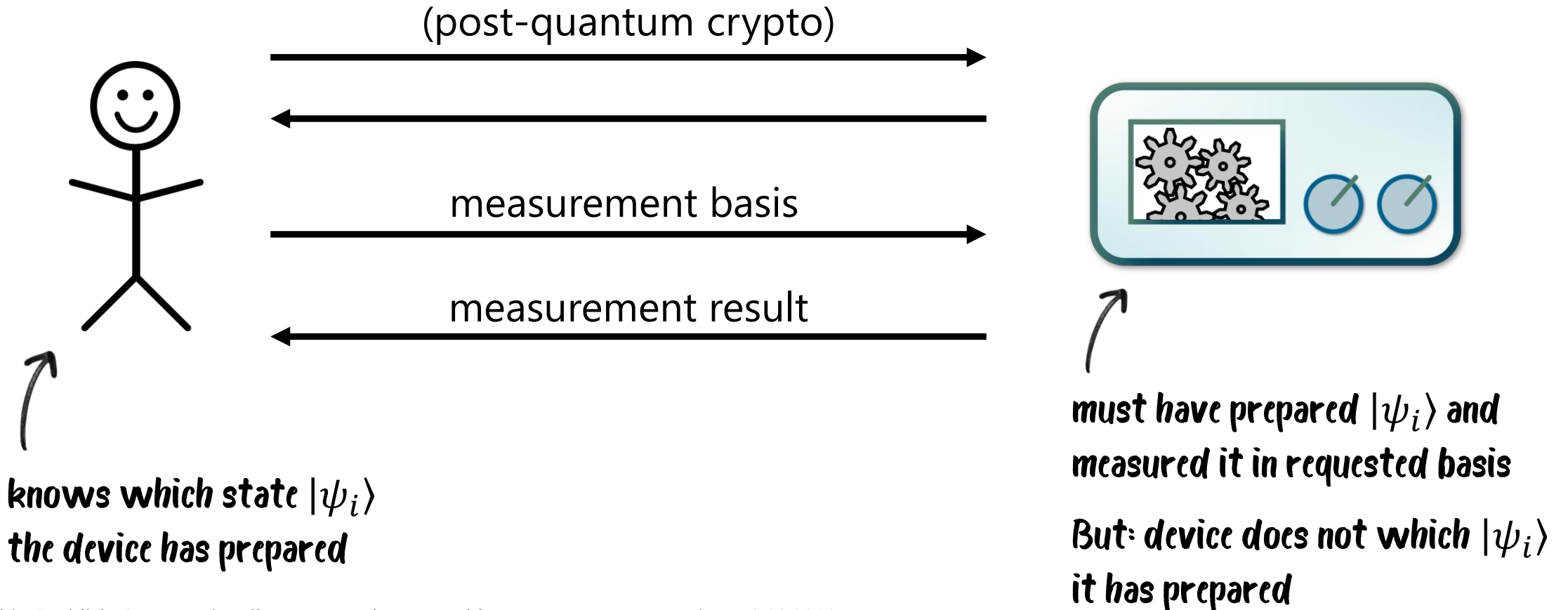
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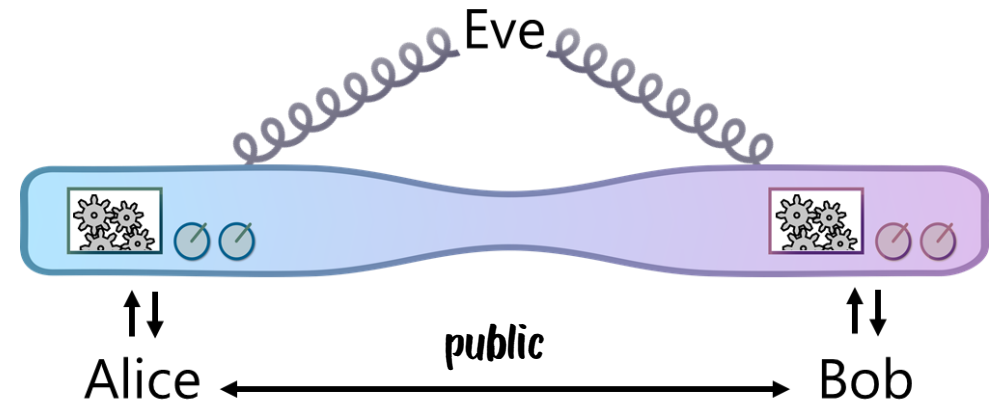
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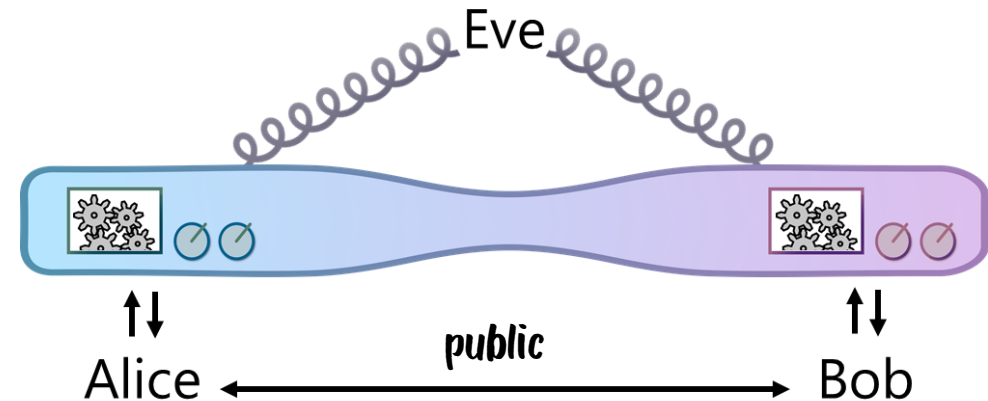
Main challenges for self-testing EPR states

- Device should prepare two qubits and perform single-qubit measurements
→ Alice and Bob need to enforce **tensor product structure** on device's global space



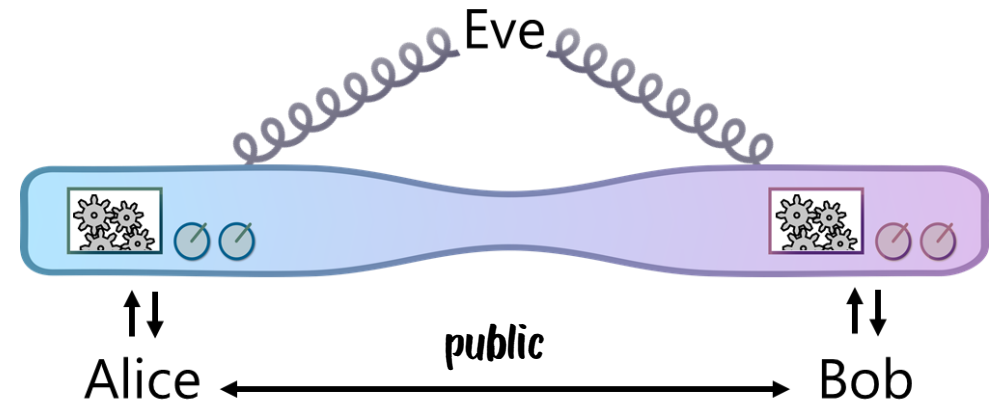
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Main challenges for self-testing EPR states

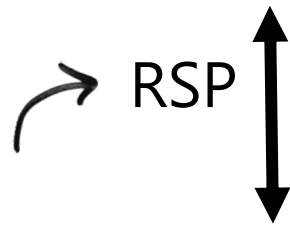
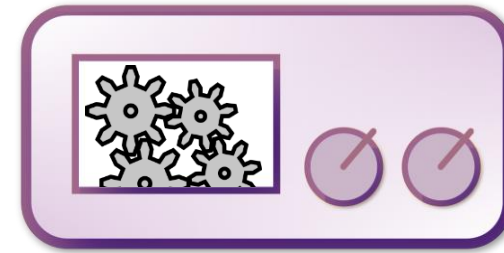
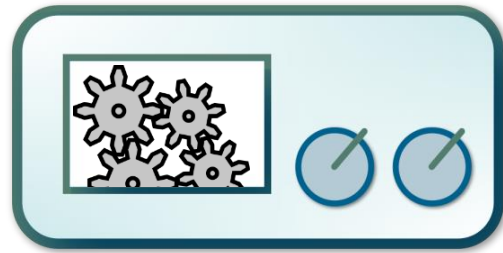
- Device should prepare two qubits and perform single-qubit measurements
→ Alice and Bob need to enforce **tensor product structure** on device's global space
- Device should **entangle** qubits with respect to this tensor product structure
- **Honest** device should only have to use **local operations** and pre-shared EPR pairs



Remote state preparation with two isolated devices

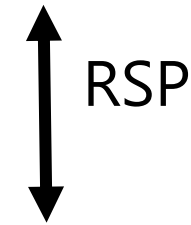
$\{|0\rangle, |1\rangle, |+\rangle, |-\rangle\}$

$\{|0\rangle, |1\rangle, |+\rangle, |-\rangle\}$



*Remote State
Preparation [GV'19]*

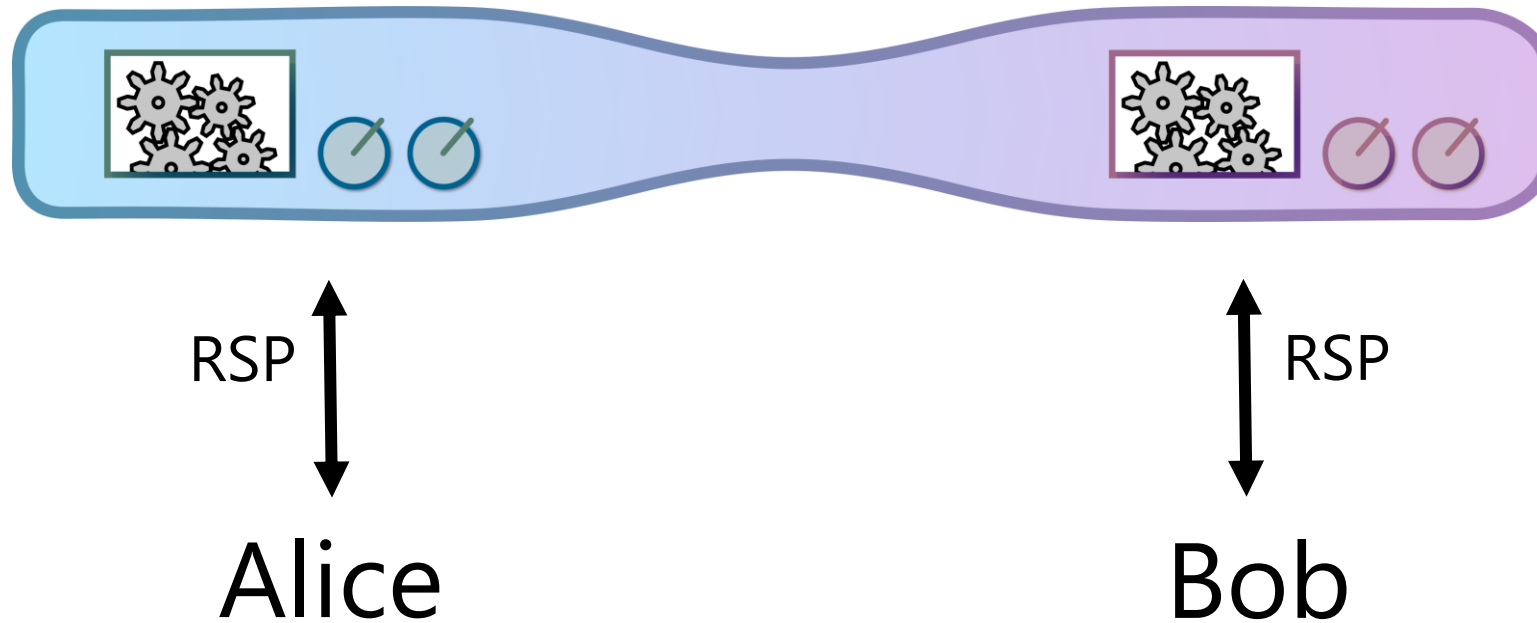
Alice



Bob

Parallel implementation with single device

$$\{|0\rangle, |1\rangle, |+\rangle, |-\rangle\} \times \{|0\rangle, |1\rangle, |+\rangle, |-\rangle\}$$

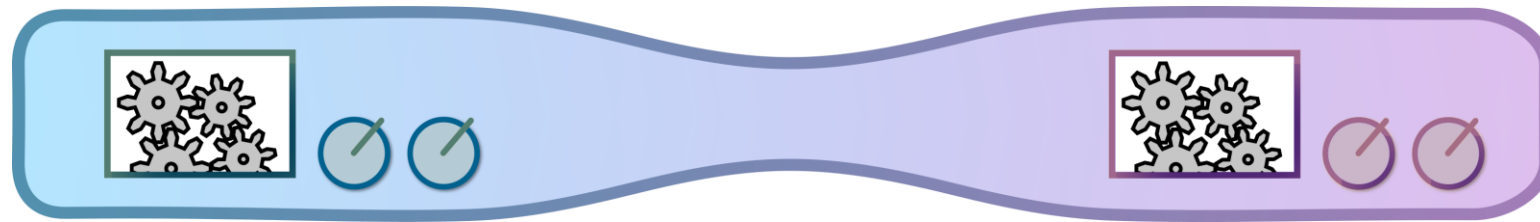


$|0/1\rangle|0/1\rangle$

$|0/1\rangle|\pm\rangle$

$|\pm\rangle|\pm\rangle$

$|\pm\rangle|0/1\rangle$



RSP



Alice

RSP



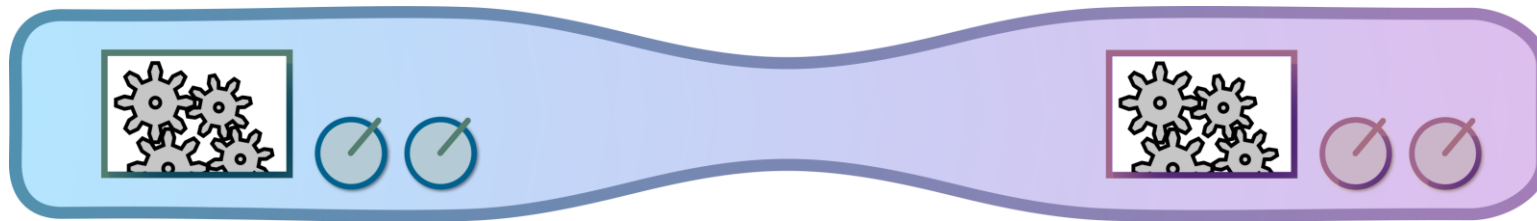
Bob

$|0/1\rangle|0/1\rangle$

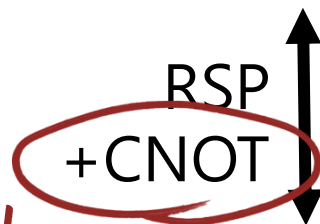
$|0/1\rangle|\pm\rangle$

$|\pm\rangle|\pm\rangle$

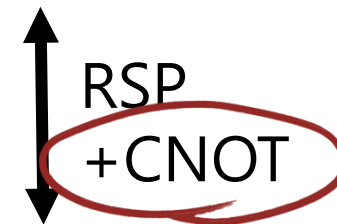
$|\pm\rangle|0/1\rangle$



non-local

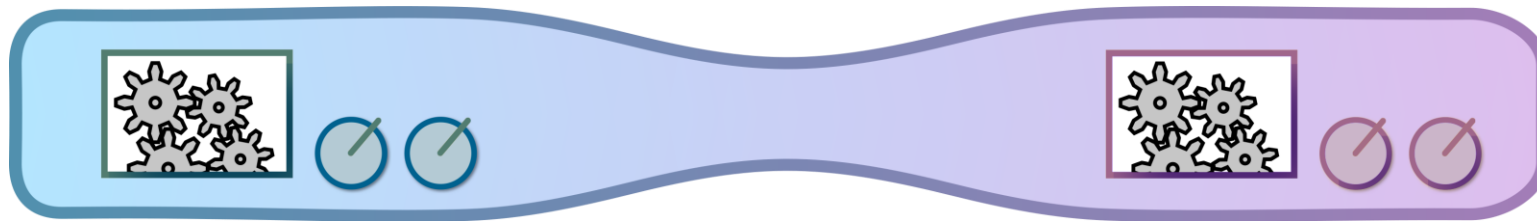


Alice



Bob

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$
CNOT
 \downarrow
 $|\pm\rangle|0/1\rangle$



non-local
RSP
+CNOT
Alice

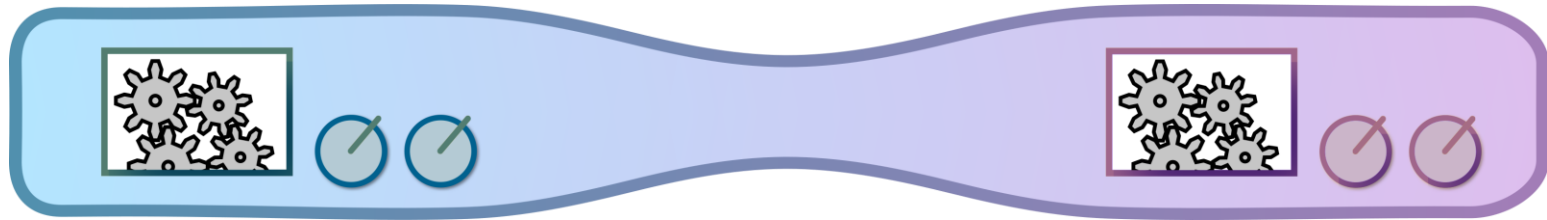
RSP
+CNOT
Bob

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

 $|\pm\rangle|0/1\rangle$

CNOT
→

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$



non-local

RSP
+CNOT

Alice

RSP
+CNOT

Bob

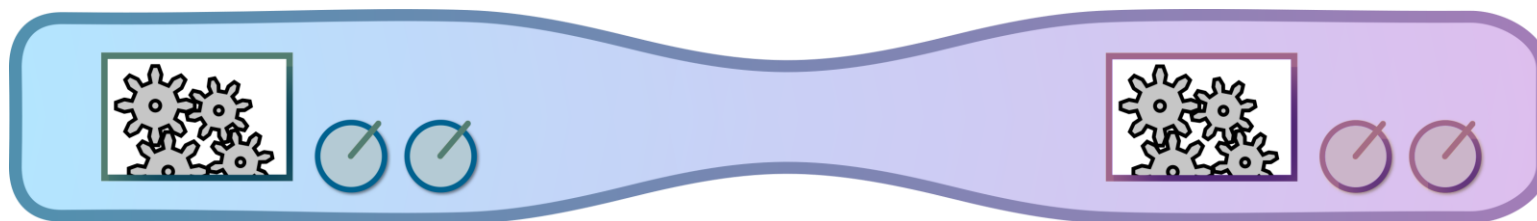
$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

CNOT
→

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

$|\pm\rangle|0/1\rangle$

$|00\rangle \pm |11\rangle, |01\rangle \pm |10\rangle$



non-local

RSP
+CNOT

Alice

RSP
+CNOT

Bob

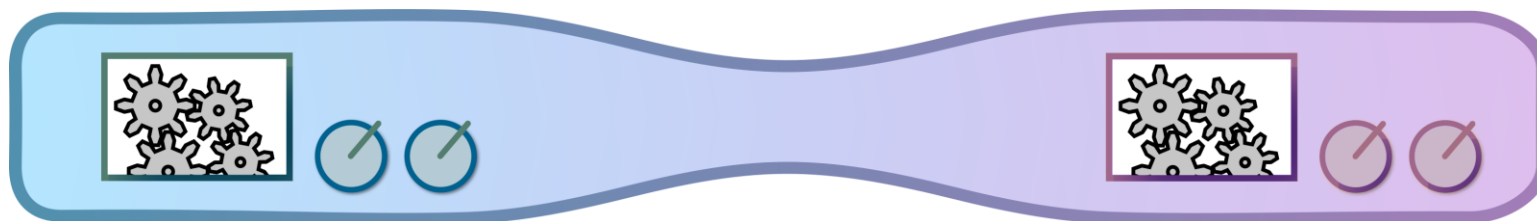
$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

CNOT
→

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

$|\pm\rangle|0/1\rangle$

$|00\rangle \pm |11\rangle, |01\rangle \pm |10\rangle$



non-local

RSP
+CNOT

Alice

RSP
+CNOT

Bob

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

CNOT
→

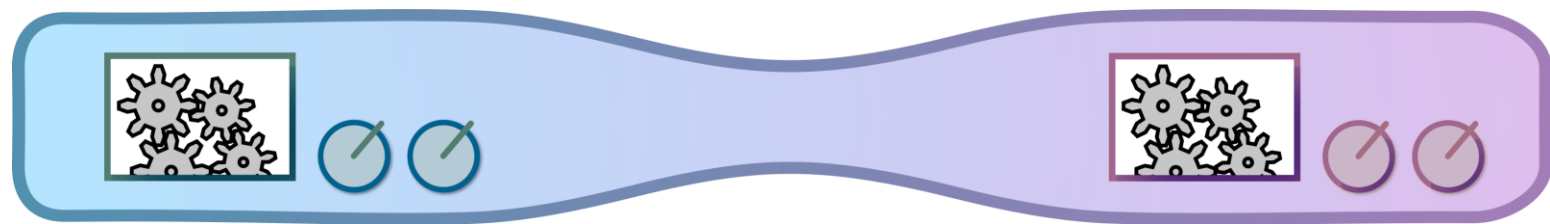
$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$



Certify **single-qubit** measurements

$|\pm\rangle|0/1\rangle$

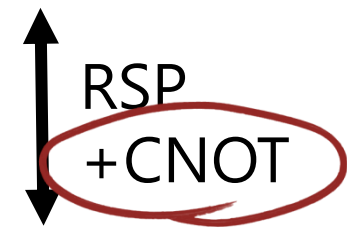
$|00\rangle \pm |11\rangle, |01\rangle \pm |10\rangle$



non-local



Alice



Bob

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

CNOT
→

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

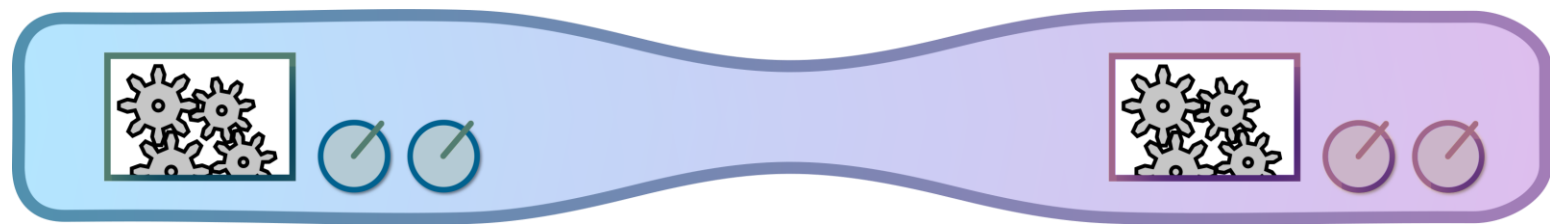


Certify **single-qubit** measurements

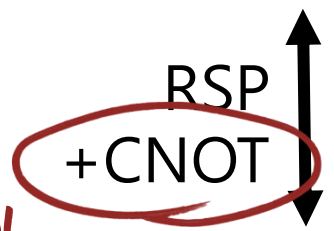
$|\pm\rangle|0/1\rangle$

$|00\rangle \pm |11\rangle, |01\rangle \pm |10\rangle$

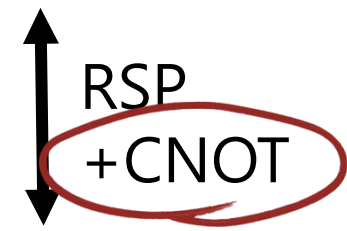
Certify **Bell-like** correlations



non-local



Alice



Bob

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

CNOT
→

$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
 $|\pm\rangle|\pm\rangle$

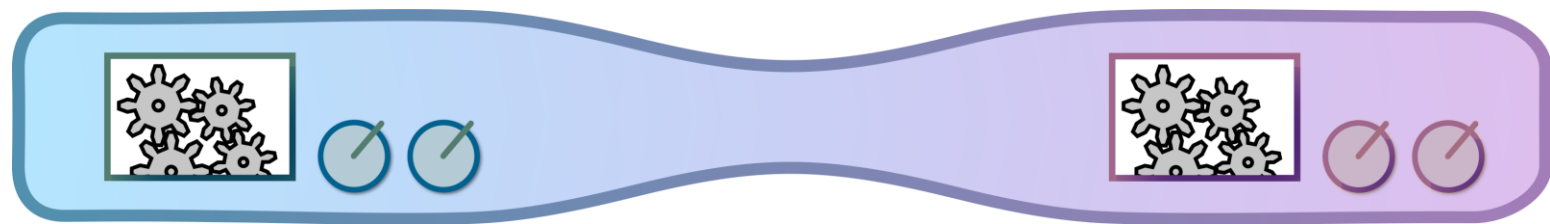
}

Certify **single-qubit** measurements

$|\pm\rangle|0/1\rangle$

$|00\rangle \pm |11\rangle, |01\rangle \pm |10\rangle$

Certify **Bell-like** correlations



non-local

RSP
+CNOT

Alice



RSP
+CNOT

Bob

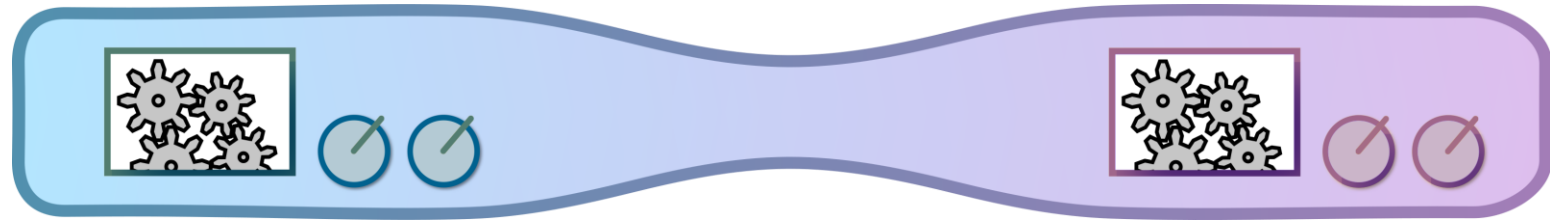
$|0/1\rangle|0/1\rangle$
 $|0/1\rangle|\pm\rangle$
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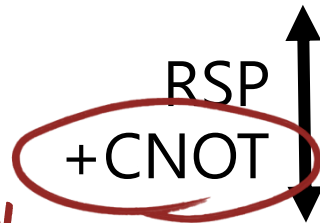
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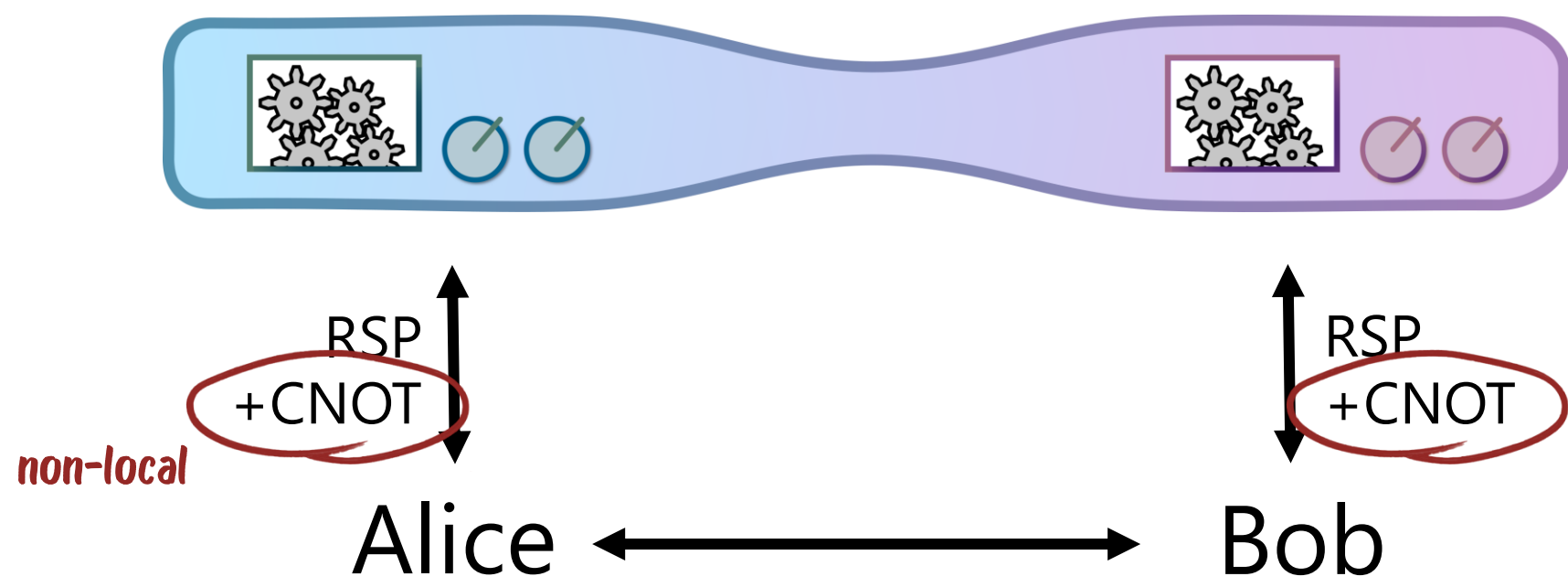
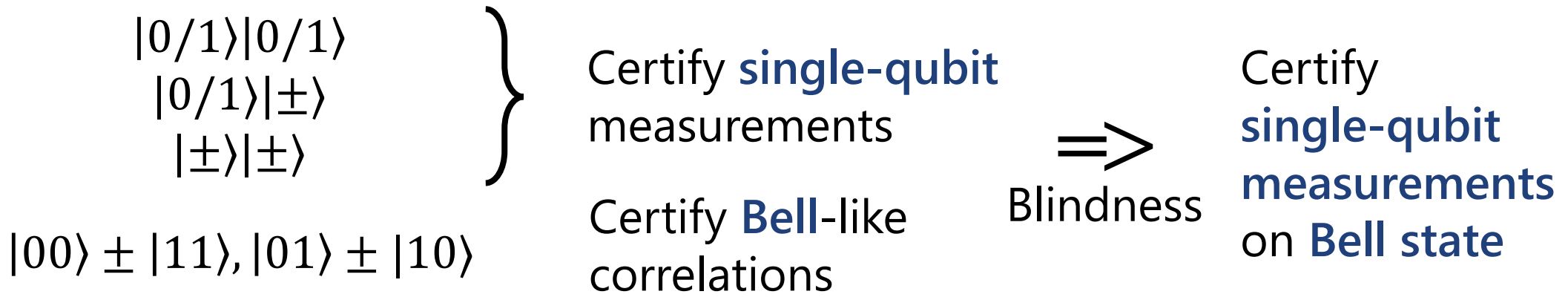
non-local

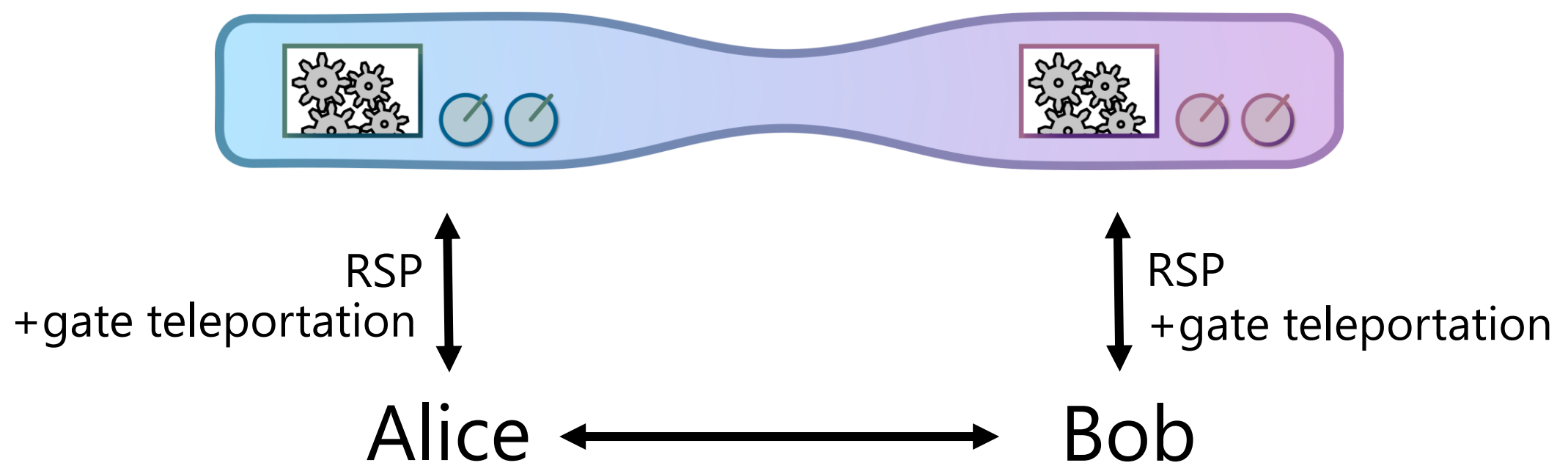


Alice



Bob





Honest **local** strategy with pre-shared EPR pairs

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non-local gate ↗ $CNOT|\phi\rangle_{Alice}|\psi\rangle_{Bob}$

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**send a to Alice,
 b to Bob**

**Alice and Bob adapt
checks to account
for correction
operator**

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Summary

T. Metger and T. Vidick, Self-testing of a single quantum device under computational assumptions, arXiv:2001.09161

T. Metger, Y. Dulek, A. Coladangelo, and R. Arnon-Friedman, Device-independent quantum key distribution from computational assumptions, arXiv:2010.04175

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